# Ffith Semester B.E. Degree Examination, June/July 2018

## Modern Control Theory

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

### PART - A

- Mention five advantages of modern control theory (MCT), over classical control theory.
  - Consider a system given by  $G(s) = \frac{s+3}{s^2+3s+2}$ , obtain the state space representation in:
    - i) Controllable canonical form
    - ii) Observable canonical form

(05 Marks)

Write the state variable formulation of the network shown in Fig.Q1(c), where all components are of unity magnitude.

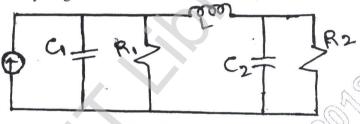


Fig.Q1(c)

(10 Marks)

Derive the transfer function from state model.

(05 Marks)

- Consider a system having state model  $\dot{X} = AX + BU$  and Y = CX + DU $B = \begin{bmatrix} 3 \\ 5 \end{bmatrix}$ ,  $C = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$ ,  $D = \begin{bmatrix} 0 \end{bmatrix}$ , obtain its transfer function.
- Reduce the given state model into its canonical form by diagonalising matrix A.

$$\dot{X} = AX + BU$$
;  $Y = CX + DU$  where  $A = \begin{bmatrix} 0 & 1 & -1 \\ -6 & -11 & 6 \\ -6 & -11 & 5 \end{bmatrix}$ ,  $B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$ ,  $C = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$ ,  $D = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$ 

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(10 Marks)

- Diagonalize the matrix A where  $A = \begin{bmatrix} 4 & 1 & -2 \\ 1 & 0 & 2 \end{bmatrix}$ . (06 Marks) 3
  - canonical form For the transfer function T(S), obtain the state model in  $T(S) = \frac{s(s+2)(s+3)}{(s+1)^2(s+4)}$ (08 Marks)
  - A system is described by the following differential equations. Represent the system in state space  $X^{(3)} + 3X^{(2)} + 4\dot{X} + 4X = U_1 + 3U_2 + 4U_3$  and the outputs are  $Y_1 = 4\dot{X} + 3U_1$ ;  $Y_2 = X^{(2)} + 4U_2 + U_3.$ (06 Marks)

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(06 Marks)

- What is STM? State atleast five properties of STM.
- Find the STM of  $A = \begin{bmatrix} 0 & 0 & -2 \\ 0 & 1 & 0 \\ 1 & 0 & 3 \end{bmatrix}$  by Caley Hamilton method. (06 Marks)
- Given the state model of the system X = AX + BU and Y = CX + DU where A =  $\begin{bmatrix} 0 & 1 \\ -4 & -5 \end{bmatrix}$  B =  $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$  C =  $\begin{bmatrix} 1 & 0 \end{bmatrix}$ , D =  $\begin{bmatrix} 0 \end{bmatrix}$  with initial conditions  $X(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$ . Determine:
  - i) The state transition matrix (STM)
  - ii) The state and output X(t) and Y(t) for a unit step input.
  - iii) Inverse state transition matrix.

(08 Marks)

## PART - B

Determine the controllability and observability of  $\dot{X} = AX + BU$  and Y = CX + DU where 5

$$A = \begin{bmatrix} -3 & 1 & 0 \\ 1 & -2 & 1 \\ 1 & 1 & 0 \end{bmatrix} \quad B = \begin{bmatrix} 0 \\ 2 \\ 2 \end{bmatrix} \quad C = \begin{bmatrix} 1 & 2 & -1 \end{bmatrix}, \quad D = \begin{bmatrix} 0 \end{bmatrix} \text{ using (i) Kalman's test and}$$

- (10 Marks) (ii) Gilbert's test.
- b. For a homogeneous equation  $\dot{X} = AX$  the following three different initial conditions are  $\begin{bmatrix} e^{t} \\ -e^{-t} \\ 2e^{-t} \end{bmatrix}; \begin{bmatrix} e^{-2t} \\ -2e^{-2t} \\ 0 \end{bmatrix}; \begin{bmatrix} -2e^{-3t} \\ -6e^{-3t} \\ 0 \end{bmatrix}.$ 
  - i) Identify the initial conditions ii) Find the system matrix A iii) Find STM. (10 Marks)
- Consider a system defined by  $\dot{X} = AX + BU$  where  $A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & 5 & -6 \end{bmatrix}$ ;  $B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$ . It is

desired to have closed loop poles at -1±j2 and -10. Determine the state feedback gain matrix K using (i) Direct substitution method and (ii) Ackerman's method.

- b. For a system defined by  $\dot{X} = AX + BU$  and Y = CX + DU where  $A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}$ ;
  - $B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}; C = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}.$  Determine the observer gain matrix by (i) Direct substitution method
- and (ii) Ackerman's method.

(10 Marks)

- a. Mention five properties of non linear systems and explain (i) dead zone (ii) backlash. (10 Marks)
  - Explain the concept of limit cycles used in non linear systems. (10 Marks)
- Determine the stability of a nonlinear system governed by the equations  $\dot{X}_1 = -X_1 + 2X_1^2X_2$ ,  $\dot{X}_2 = -X_2$  using Lyapunov's method. (08 Marks)
  - Determine the stability of a system described by  $A = \begin{bmatrix} -1 & 1 \\ -2 & -4 \end{bmatrix}$ . (08 Marks)
  - Explain: i) Asymptotic stability, ii) Stability in the sense of Lyapunov. (04 Marks)