# Fourth Semester B.E. Degree Examination, June/July 2019 Electromagnetic Field Theory

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

## Module-1

a. Obtain the relationship between rectangular and cylindrical co-ordinate system. (06 Marks)

b. Find dot product, cross product and unit vector of A for the following vectors:

$$\overline{A} = 3\overline{ax} + 4\overline{ay} - 5\overline{az}$$

 $\overline{B} = -6 \overline{ax} + 2 \overline{ay} + 4 \overline{az}$ 

c. State and explain Coulomb's law in vector form.

(06 Marks)

(08 Marks)

OR

2 a. Give the Cartesian coordinates of the vector field  $\overline{H} = 20\overline{ap} - 10\overline{aQ} + 3\overline{az}$  at the point P(x=5, y=2, z=-1). (08 Marks)

b. State the prove Gauss divergence theorem.

(06 Marks)

c. If  $D = (2y^2z - 8xy)ax + (4xyz - 4x^2)ay + (2xy^2 - 4z)az$ . Determine div of D at P(1, -2, 3).

(06 Marks)

# Module-2

3 a. Prove that electric-field intensity is expressed as negative gradient of scalar potential.

(07 Marks)

b. Derive current continuity equation with usual notation.

(06 Marks)

c. Obtain the boundary conditions between Dielectric and Conductors.

(07 Marks)

OR

- 4 a. Given  $V = 2x^2y 5z$  at point P(-4, 3, 6) find potential, electrified intensity and volume charge density. (05 Marks)
  - b. Derive the expression for capacitor of a parallel plate capacitor containing 2 dielectrics.

    (07 Marks)

c. Obtain the expression for energy density in free space for electrostatic field.

(08 Marks)

### Module-3

- 5 a. Derive Laplace equation and Poisson's equation from point form of gauss law in all the three co-ordinate system. (06 Marks)
  - b. Prove the uniqueness of solution using uniqueness theorem.

(08 Marks)

c. State and explain Biot-Savart's law and Ampere's circuit law.

(06 Marks)

2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.

important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.

#### OR

6 a. Verify the potential field given satisfies the Laplace's equation  $V = 2x^2 - 3y^2 + z^2$ .

(05 Marks)

- b. Obtain the equation for  $curl(\nabla \times \overline{H}) = \overline{J}$  by considering differential surface element and equations. (08 Marks)
- c. If a field given  $\overline{F} = (x + 2y + az)\overline{ax} + (bx 3y z)\overline{ay} + (4x + cy + 2z)\overline{az}$ , find the constants a, b, c such that the field is irrotational. (07 Marks)

#### Module-4

7 a. State and explain Lorentz force equation.

(05 Marks)

- b. A point charge Q = 18nc has a velocity of  $5 \times 10^6$ m/s in the direction  $\overline{au} = 0.6\overline{ax} + 0.75\overline{ay} + 0.3\overline{az}$ . Calculate the magnitude of the force exacted on the charge by the field:
  - i)  $\overline{E} = -3\overline{ax} + 4\overline{ay} + 6\overline{az} \text{ KV/m}$
  - ii)  $\overline{B} = -3\overline{ax} + 4\overline{ay} + 6\overline{az} \text{ mT}$
  - iii)  $\overline{B}$  and  $\overline{E}$  together acting.

(08 Marks)

c. Derive the boundary conditions at the interface between two magnetic materials of different permeabilites. (07 Marks)

#### OR

- 8 a. Derive the equation for magnetic force between two differential current elements. (07 Marks)
  - b. Derive the expression for the inductance of a solenoid and torroid.

(07 Marks)

c. Consider an air core torroid with 500 turns cross sectional area of  $6 \text{cm}^2$  and mean radius of 15cm and carries current of 4amps. Find reluctance,  $\overline{B}$ ,  $\overline{H}$ . (06 Marks)

#### Module-5

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9 a. State and explain Faraday's law.

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- b. List Maxwell's equations for time varying fields in integral form and point form. (08 Marks)
- c. Explain skin depth and skin effect. Derive the expression for skin depth.

(07 Marks)

#### OR

10 a. State and explain Pointing theorem with derivation  $\overline{P} = \overline{E} \times \overline{H}$ .

(07 Marks)

b. Derive expression for displacement current density for time varying fields.

(07 Marks)

c. A 300MHz uniform plane wave propagates through fresh water for which  $\sigma = 0$ ,  $\mu_r = 1$ ,  $\epsilon_r = 78$ . Calculate attenuation constant, phase constant, wavelength intrinsic impedance  $(\alpha, \beta, \lambda, \eta)$ .

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