

OR

- 6 a. If $\vec{f} = (x + y + 1)\hat{i} + \hat{j} - (x + y)\hat{k}$ show that $\vec{f} \cdot \text{curl } \vec{f} = 0$. (06 Marks)
- b. If $\vec{f} = \text{grad}(x y^3 z^2)$ find $\text{div } \vec{f}$ and $\text{curl } \vec{f}$. (07 Marks)
- c. Prove that $\text{div}(\text{curl } \vec{A}) = 0$ (07 Marks)

Module-4

- 7 a. Evaluate $\int_0^a x \sqrt{ax - x^2} dx$ (06 Marks)
- b. Solve $r \sin \theta - \cos \theta \frac{dr}{d\theta} = r^2$ (07 Marks)
- c. Show that the family of parabolas $y^2 = 4a(x + a)$ is self orthogonal. (07 Marks)

OR

- 8 a. Obtain the reduction formula for $\int_0^{\pi/2} \cos^n x dx$. (06 Marks)
- b. Solve $(x^2 + y^2 + x) dx + xy dy = 0$. (07 Marks)
- c. Water at temperature 10°C takes 5 minutes to warm upto 20°C in a room temperature 40°C . Find the temperature after 20 minutes. (07 Marks)

Module-5

- 9 a. Find the rank of the matrix

$$\begin{bmatrix} 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 3 & 1 & 0 & 2 \\ 1 & 1 & -2 & 0 \end{bmatrix}$$
 by reducing it to echelon form. (06 Marks)
- b. Find the largest eigen value and the corresponding eigen vector for

$$A = \begin{bmatrix} 2 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 2 \end{bmatrix}$$
 taking $(1 \ 0 \ 0)^T$ as initial vector by using power method. (Carry out six iterations) (07 Marks)
- c. Show that the transformation $y_1 = 2x - 2y - z$, $y_2 = -4x + 5y + 3z$ and $y_3 = x - y - z$ is regular and find the inverse transformation. (07 Marks)

OR

- 10 a. Solve the equations $20x + y - 2z = 17$; $3x + 20y - z = -18$, $2x - 3y + 20z = 25$ by using Gauss-Seidel method. (Carry out 3 iterations) (06 Marks)
- b. Diagonalise the matrix $A = \begin{bmatrix} -1 & 3 \\ -2 & 4 \end{bmatrix}$ (07 Marks)
- c. Reduce the quadratic form $3x^2 - 2y^2 - z^2 + 12yz + 8xz - 4xy$ into canonical form, using orthogonal transformation. (07 Marks)
