Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.



## Fourth Semester B.E. Degree Examination, June/July 2016

## **Field Theory**

Max. Marks: 100



ote: Answer any FIVE full questions, selecting atleast TWO questions from each part.

## PART - A

- a. State Gauss theorem of electrostatics. List characteristics of Gaussian surface. (05 Marks)
  - b. Determine electric flux density 'D' in Cartesian coordinates caused at p(6, 8, -10) by i) a point charge of 30 mc at origin ii) infinite line charge with  $\rho_r = 40 \,\mu\text{c/m}$  ii) A surface charge with  $\rho_s = 57.2 \,\mu\text{c/m}^2$  on a plane z = -9m.
  - c. Evaluate both side of divergence theorem for the region  $r \le a$  (spherical coordinates) having flux density  $D = \frac{5r}{3} a_r c/m^2$  (07 Marks)
- 2 a. Prove that :  $E = -\nabla V$

(05 Marks)

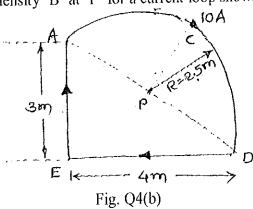
- b. Determine work done in carrying a charge of -2C from (2, 1, -1) to (8, 2, -1) in an electric field  $E = ya_x + xa_y$  v/m along the path  $x = 2y^2$ . (07 Marks)
- Three point charges 3 coul, 4 coul and 5 coul are to be situated at corner of an equilateral triangle of side 5 m. Find energy density at the centre of triangle. (08 Marks)
- 3 a. Derive Poisson's and Laplace equation.

(06 Marks)

- b. A potential field is given by  $v = x^2yz + Ay^3z$  volts determine of 'A' such that v satisfies Laplace equation and hence find electric field E at p(2, 1, -1). (06 Marks)
- c. A spherical capacitor has a capacitance of 54 pF. It consists of two concentric spheres with inner and outer radii differing by 4 cm. Dielectric in between is air. Determine inner and outer radii. (08 Marks)
- 4 a. State and explain Ampere's circuital law.

(05 Marks)

b. Determine magnetic flux density 'B' at 'P' for a current loop shown in Fig.Q4(b). (09 Marks)



c. Clearly distinguish between scalar magnetic potential and vector magnetic potential.

## PART - B

- 5 a. Derive Lorentz force equation for a moving change placed in a combined electric and magnetic field. (06 Marks)
  - b. A point charge Q = 18 nc moves with a velocity of  $5 \times 10^6$  m/sec in the direction of  $0.06a_x + 0.75a_y + 0.3a_z$ . Determine magnitude of force experienced by the charge when placed in i) electric field  $E = -3a_x + 4a_y + 6a_z$  kv/m ii) magnetic field  $E = -3a_x + 4a_y + 6a_z$  mT iii) combined E and B. (08 Marks)
  - c. An air cored toroid has a cross sectional area of 6 cm<sup>2</sup>, a mean radius of 15 cm and is wound with 500 turns and carries a current of 4A. Find the magnetic field intensity at the mean radius.

    (06 Marks)
- 6 a. Explain Faraday's laws applied to: i) stationary path, changing field and ii) steady field, moving circuit. (06 Marks)
  - b. List Maxwell's equations for both: i) steady and ii) Time varying fields in differential and integral form, also mention the relevant laws they demonstrate. (08 Marks)
  - c. A straight conductor of length 0.2m, lies on x-axis with one end at origin. The conductor is subjected to a magnetic flux density  $B = 0.04a_y$  Tesla and the velocity  $v = 2.5 \sin 10^3$  ta<sub>z</sub> m/sec. Determine motional emf induced in the conductor. (06 Marks)
- 7 a. Derive wave equation for E in a general medium.

(06 Marks)

b. State and explain Poynting theorem.

(06 Marks)

- c. A lossless dielectric medium has  $\sigma = 0$ ,  $\mu_r = 1$   $\epsilon_r = 1$ . A electromagnetic wave has field as  $H = -0.1 \cos(\omega t z)a_x + 0.5 \sin(\omega t z)a_y$  A/m. Find: i) phase constant, ii) angular velocity iii) the wave impedance iv) components of electric field intensity of the wave. (08 Marks)
- 8 a. Derive an expression for transmission coefficient and reflection coefficient and relate them.

  (08 Marks)
  - b. Define standing wave ratio. Write an expression for it. (04 Marks)
  - c. Determine the amplitude of reflected and transmitted 'E' and 'H' at the interface between two regions. Characteristics of region 1 are  $\varepsilon_{r_1} = 8$ ,  $\mu_{r_1} = 0$ ;  $\sigma_1 = 0$  and region 2 is free space. The incident  $E_0^i$  in region 1 is of 1.5 V/m. Assume normal incidence. Also find average power in two regions. (08 Marks)

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