HSN

Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice

Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.

(ii)

18CS36

(06 Marks)

(07 Marks)

(07 Marks)

(06 Marks)

(07 Marks)

(06 Marks)

(07 Marks)

(07 Marks)

Two particular persons will not attend separately. Two particular persons will not attend together.

1 of 3

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4 a. Prove that every positive integer $n \ge 24$ can be written as a sum of 5's and / or 7's.

(06 Marks)

- b. Find the number of permutations of the letters of the word MASSASAUGA. In how many of these all four A's are together? How many of them begin with S? (07 Marks)
- c. In how many ways can one distribute eight identical balls into four distinct containers, so that, (i) No containers is left empty.
 - (ii) The fourth container gets an odd number of balls.

(07 Marks)

Module,3

- 5 a. For any non empty sets A, B, C prove that,
 - (i) $A \times (B \cup C) = (A \times B) \cup (A \times C)$

(ii) $(A \times (B-C)) = (A \times B) - (A \times C)$

(06 Marks)

b. Let $f: R \to R$ be defined by $f(x) = \begin{cases} 3x-5 & \text{for } x > 0 \\ -3x+1 & \text{for } x \le 0 \end{cases}$

(i) Determine f(0), $f(\frac{5}{3})$ (ii) Find $f^{-1}([-5,5])$

(07 Marks)

c. Let f, g, h be functions form z to z defined by f(x) = x - 1, g(x) = 3x, $h(x) = \begin{cases} 0 & \text{if } x \text{ is even} \\ 1 & \text{if } x \text{ is odd} \end{cases}$ Verify that $(f \circ g) \circ h(x) = f \circ (g \circ h)(x)$. (07 Marks)

OR

- 6 a. Let A = \{1,2,3,4,6\} and R be a relation on A defined by aRb if and only if "a is a multiple of b". Represent the relation R as a matrix and draw its diagraph. (06 Marks)
 - b. Draw the Hasse diagram representing the positive divisors of 36.

(07 Marks)

- c. Let $A = \{1,2,3,4,5\}$, define a relation R on A A, by $(x_1,y_1)R(x_2,y_2)$ if and only if $x_1 + y_1 = x_2 + y_2$
 - (i) Verify that R is an equivalence relation.
 - (ii) Find the partition of A×A induced by R.

(07 Marks)

Module-4

- 7 a. There are eight letters to eight different people to be placed in eight different addressed envelopes. Find the number of ways of doing this so that at least one letter gets to the right person.

 (06 Marks)
 - b. In how many ways can the 26 letters of the English alphabet be permuted so that none of the patterns CAR, DOG, PUN or BYTE occurs? (07 Marks)
 - c. By using the expansion formula, obtain the rook polynomial for the board C. (07 Marks)

- a. An apple, a banana, a mango and an orange are to be distributed to four boys B₁, B₂, B₃, B₄. The boys B₁ and B₂ do not wish to have apple. The boy B₃ does not want banana or mango, and B₄ refuses orange. In how many ways the distribution can be made so that no boy is displeased? (06 Marks)
 - b. If $a_0 = 0$, $a_1 = 1$, $a_2 = 4$ and $a_4 = 37$ satisfy the recurrence relation $a_{n+2} + ba_{n+1} + ca_n = 0$, for $n \ge 0$, find the constants b and c, and solve the relation a_n . (07 Marks)
 - c. How many integers between 1 and 300 (inclusive) are,
 - (i) Divisible by at least one of 5, 6, 8?
 - (ii) Divisible by none of 5, 6, 8?

(07 Marks)

Module-5

9 a. Show that the following two graphs shown in Fig. Q9 (a) – (i) and Fig. Q9 (a) – (ii) are isomorphic, (06 Marks)



Fig. Q9 (a) - (i)

- Fig. Q9 (a) (ii)
- b. Define the following with example of each,
 - (i) Simple graph
- (ii) Sub graph
- (iii) Compliment of a graph
- (iv) Spanning sub graph

(07 Marks)

Construct an optimal profix code for the symbols a, o, q, u, y, z that occurs with frequencies 20, 28, 4, 17, 12, 7 respectively.

OR

- 10 a. Prove that two simple graphs G_1 and G_2 are isomorphic if and only if their complements are isomorphic. (06 Marks)
 - b. Let G = (V, E) be a simple graph of order |V| = n and size |E| = m, if G is a bipartite graph. Prove that $4m \le n^2$. (07 Marks)
 - c. Construct an optimal prefix code for the letters of the word ENGINEERING. Hence deduce the code for this word. (07 Marks)