

15EE45

Fourth Semester B.E. Degree Examination, Dec.2019/Jan.2020

Electromagnetic Field Theory

Time: 3 hrs.

EANGALORE

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. What is a unit vector? Illustrate its significance in the vector representation. (02 Marks)
  - b. Explain Cartesian coordinate system and differential elements in Cartesian coordinate system. (04 Marks)
  - c. Define:
    - i) Dot product and cross product of two vectors.
    - ii) Gradient of a scalar field
    - iii) Divergence and curl of a vector field.

(10 Marks)

OR

- 2 a. State and explain Coulomb's law of force between the two point charges. (05 Marks)
  - b. A point charge Q = 30nc is located at the origin in Cartesian co-ordinates. Find the electric flux density  $\overline{D}$  at (1, 3, -4) m. (05 Marks)
  - c. State and explain Gauss law in electrostatics.

(06 Marks)

Module-2

- 3 a. Derive an expression for energy expanded in making a point charge in an electric field.
  (08 Marks)
  - b. Derive an expression for the electric intensity at any point in the negative of the potential gradient at that point or  $E = -\nabla V$ . (08 Marks)

OR

- 4 a. With necessary relations, define current and current density. (03 Marks)
  - b. Explain the boundary conditions for a boundary between two di-electric materials.

(08 Marks)

- c. A capacitor consists of two metal plates each 100cm<sup>2</sup> placed parallel and 2mm apart. The whole of space between the plates is filled with a di-electric having a relative permittivity of 3.5. A potential difference of 500V is maintained between the plates. Calculate:
  - i) The capacitance
  - ii) The charge on capacitor
  - iii) Electric flux density
  - iv) Potential gradient.

(05 Marks)

Module-3

- 5 a. Derive Poisson's and Laplace equations starting from point form of Gauss law. (06 Marks)
  - b. Verify that the potential field given below satisfies the Laplace's equation  $V = 2x^2 3y^2 + z^2$
  - c. State and prove Unigueness theorem.

(08 Marks)

OR

6 a. State and explain Biot-Savart's law.
b. State and explain Stoke's theorem.
c. Derive an expression for vector magnetic potential.
(06 Marks)
(06 Marks)

## Module-4

- 7 a. Derive an expression for the force between differential current elements. (08 Marks)
  - b. A point chart of Q = -1.2C has velocity  $\sqrt{v} = (5ax + 2ay 3az)m/s$ . Find the magnitude of the force exerted on the charge if,
    - i)  $\overline{E} = -18\overline{a}x + 5\overline{a}y 10\overline{a}z \text{ v/m}$
    - ii)  $\overline{B} = -4\overline{a}x + 4\overline{a}y + 3\overline{a}z$  T
    - iii) Both are present simultaneously

(08 Marks)

## OR

- 8 a. Derive the boundary conditions at the interface between two magnetic materials of different permeabilities. (08 Marks)
  - b. Calculate the inductance of a solenoid of 200 turns wound tightly on a cylindrical tube of 6cm diameter. The length of the tube is 60cm and the solenoid is in air. (02 Marks)
  - c. Define mutual inductance. Derive an expression for mutual inductance of two different coils.

    (06 Marks)

## Module-5

- 9 a. Explain briefly Faraday's law and displacement current for time varying fields. (07 Marks)
  - b. In a given lossy dielectric medium conduction current density  $J_c = 0.02 Sin 10^9 \, t(A/m^2)$ . Find the displacement current density if  $\sigma = 10^3 \, s/m$  and  $\epsilon_r = 6.5$ . (03 Marks)
  - Write Maxwell's equations in point form and in integral form for time varying fields.

(06 Marks)

## OR

- 10 a. Discuss the propagation of uniform plane waves in a lossless medium. (06 Marks)
  - b. Define poynting vector and explain the power flow associated with it.

(06 Marks)

- c. A 300MHz uniform plane wave propagates through fresh water for which  $\sigma = 0$ ,  $\mu_r = 1$  and  $\epsilon_r = 78$ . Calculate:
  - i) The attenuation constant
  - ii) The phase constant
  - iii) The wave length.

(04 Marks)