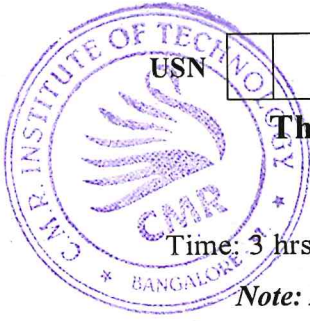


# CBCS SCHEME

17MATDIP31



USN

Third Semester B.E. Degree Examination, Dec.2019/Jan.2020

## Additional Mathematics – I

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

### Module-1

- 1 a. Find the modulus and amplitude of  $\frac{3+i}{2+i}$  (07 Marks)
- b. If  $x = \cos\theta + i \sin\theta$ , then show that  $\frac{x^{2n}-1}{x^{2n}+1} = i \tan n\theta$ . (07 Marks)
- c. Simplify  $\frac{(\cos 3\theta + i \sin 3\theta)^4 (\cos 4\theta + i \sin 4\theta)^5}{(\cos 4\theta + i \sin 4\theta)^3 (\cos 5\theta + i \sin 5\theta)^{-4}}$  (06 Marks)

OR

- 2 a. Find the sine of the angle between  $\vec{A} = 2\hat{i} + 2\hat{j} - \hat{k}$  and  $\vec{B} = 6\hat{i} - 3\hat{j} + 2\hat{k}$ . (07 Marks)
- b. Find the value of  $\lambda$ , so that the vectors  $\vec{a} = 2\hat{i} - 3\hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + 2\hat{j} - 3\hat{k}$  and  $\vec{c} = \hat{i} + \lambda\hat{k}$  are coplanar. (07 Marks)
- c. Prove that  $\vec{a} \times (\vec{b} \times \vec{c}) + \vec{b} \times (\vec{c} \times \vec{a}) + \vec{c} \times (\vec{a} \times \vec{b}) = 0$ . (06 Marks)

### Module-2

- 3 a. Find the  $n^{\text{th}}$  derivative of  $e^{ax} \cos(bx + c)$ . (07 Marks)
- b. If  $y = a \cos(\log x) + b \sin(\log x)$  prove that  $x^2 y_{n+2} + (2n+1)xy_{n+1} + (n^2+1)y_n = 0$ . (07 Marks)
- c. If  $u = \sin^{-1}\left(\frac{x^2+y^2}{x+y}\right)$ , prove that  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \tan u$ . (06 Marks)

OR

- 4 a. Find the pedal equation of  $r^n = a^n \cos n\theta$ . (07 Marks)
- b. Expand  $\log_e(1+x)$  in ascending powers of  $x$  as far as the term containing  $x^4$ . (07 Marks)
- c. If  $x = r \cos\theta$ ,  $y = r \sin\theta$ , find  $\frac{\partial(x,y)}{\partial(r,\theta)}$  (06 Marks)

### Module-3

- 5 a. Evaluate  $\int_0^1 \int_{y^2}^y (1+xy^2) dx dy$  (07 Marks)
- b. Evaluate  $\int_0^{2\pi} \sin^4 x \cos^6 x dx$  (07 Marks)
- c. Evaluate  $\int_0^2 \frac{x^4}{\sqrt{4-x^2}} dx$  (06 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any revealing of identification, appeal to evaluator and/or equations written eg, 42+8 = 50, will be treated as malpractice.

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OR

- 6 a. Evaluate  $\int_1^2 \int_3^4 (xy + e^y) dy dx$  (07 Marks)
- b. Evaluate  $\int_0^\pi x \sin^8 x dx$  (07 Marks)
- c. Evaluate  $\int_1^2 \int_0^1 \int_{-1}^1 (x^2 + y^2 + z^2) dx dy dz$  (06 Marks)

**Module-4**

- 7 a. If particle moves on the curve  $x = 2t^2$ ,  $y = t^2 - 4t$ ,  $z = 3t - 5$  where  $t$  is the time. Find the velocity and acceleration at  $t = 1$ . (07 Marks)
- b. Find the angle between the tangents to the curve  $\vec{r} = t^2 \hat{i} + 2t \hat{j} - t^3 \hat{k}$  at the point  $t = \pm 1$ . (07 Marks)
- c. If  $\vec{F} = (3x^2y - z)\hat{i} + (xz^3 + y^4)\hat{j} - 2x^3z^2 \hat{k}$  find  $\text{grad}(\text{div } \vec{F})$  at  $(2, -1, 0)$ . (06 Marks)

OR

- 8 a. Find the directional derivative of  $\phi = 4xz^3 - 3x^2y^2z$  at  $(2, -1, 2)$  along  $2\hat{i} - 3\hat{j} + 6\hat{k}$  (07 Marks)
- b. Find the unit normal to the surface  $x^2y + 2xz = 4$  at  $(2, -2, 3)$ . (07 Marks)
- c. Show that  $\vec{F} = (2xy^2 + yz)\hat{i} + (2x^2y + xz + 2yz^2)\hat{j} + (2y^2z + xy)\hat{k}$  is irrotational. (06 Marks)

**Module-5**

- 9 a. Solve  $\frac{dy}{dx} = \sin(x + y)$  (07 Marks)
- b. Solve  $\frac{dy}{dx} + y \cot x = \cos x$  (07 Marks)
- c. Solve  $(x - y + 1)dy - (x + y - 1)dx = 0$  (06 Marks)

OR

- 10 a. Solve  $(1 + e^{x/4})dx + e^{x/y} \left(1 - \frac{x}{y}\right)dy = 0$ . (07 Marks)
- b. Solve  $(x^3 \cos^2 y - x \sin 2y)dx = dy$ . (07 Marks)
- c. Solve  $(3x^2y^4 + 2xy)dx + (2x^3y^3 - x^2)dy = 0$  (06 Marks)

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