

Department of Computer Applications

Scheme and Solutions for Internal Assessment Test – III

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17MCA442 – DATA WAREHOUSING AND DATA MINING Semester / Section: IV Date of Test: 14-05-2019

viii. Constraint-based clustering: Real-world applications may need to perform clustering under various kinds of constraints (Example: Choose a new ATM location)

ix. Interpretability and usability: clustering results to be interpretable, comprehensible, and usable

Scheme:

For all the individual requirements: 10 Marks

3. Explain how to find the dissimilarity for interval-scaled (10) variables and ratio-scaled variables.

(i) Interval-Scaled Variables: are continuous measurements of a roughly linear scale, like weight and height and weather temperature.

- The measurement unit used can affect the clustering analysis
- To help avoid dependence on the choice of measurement units, the data should be standardized.
- the dissimilarity (or similarity) between the objects described by interval-scaled variables is typically computed based on the distance between each pair of objects
- The most popular distance measure is Euclidean distance, which is defined as

$$
d(i, j) = \sqrt{(|x_{i1} - x_{j1}|^2 + |x_{i2} - x_{j2}|^2 + ... + |x_{ip} - x_{jp}|^2)}
$$

where $i=(x_{i1}, x_{i2},..., x_{in})$ and $j=(x_{i1}, x_{i2},..., x_{in})$ are two n-dimensional data objects.

 Another well-known metric is Manhattan (or city block) distance, defined as

$$
d(i,j) = |x_{i1} - x_{j1}| + |x_{i2} - x_{j2}| + ... + |x_{ip} - x_{jp}|
$$

• Both the Euclidean distance and Manhattan distance satisfy the following mathematic requirements of a distance function:

c. Ratio-Scaled Variables: a positive measurement on a nonlinear scale, approximately at exponential scale approximately following the formula: Ae^{Bt} or Ae^{-Bt} (Example: measure height in centimetres, metres, inches or feet, not possible to have negative ratio)

- **three methods to handle ratio-scaled variables for computing the** dissimilarity between objects:
- i. Treat ratio-scaled variables like interval-scaled variables
- ii. Apply logarithmic transformation to a ratio-scaled variable f having value x_{if} for object i by using the formula $y_{if} = log(x_{if})$. The y_{if} values can be treated as interval valued

CMR Institute of Technology, Bengalore – 560 037 Department of Computer Applications Scheme and Solutions for Internal Assessment Test – III 17MCA442 – DATA WAREHOUSING AND DATA MINING Semester / Section: IV Date of Test: 14-05-2019 -- iii. Treat x_{if} as continuous ordinal data and treat their ranks as intervalvalued **Scheme:** For Interval-scaled variable: 5 Marks For Ratio-Scaled variable: 5 Marks **4. Explain how to find the dissimilarity for binary variables and (10) variables of mixed type.** (i) Binary Variables A binary variable has only two states: 0 or 1 A binary variable is symmetric if both of its states are equally valuable and carry the same weight (Eg.) Gender Dissimilarity that is based on symmetric binary variables is called symmetric binary dissimilarity Its dissimilarity (or distance) measure can be used to assess the dissimilarity between objects i and j: we can measure the distance between two binary variables based on the notion of similarity instead of dissimilarity, by using Jaccard coefficient (ii) Variables of Mixed Types A database can contain all of the variables of mixed types compute the dissimilarity between objects of mixed variable types: group each kind of variable together, performing a separate cluster analysis for each variable type. o process all variable types together, performing a single cluster analysis. \circ combines the different variables into a single dissimilarity matrix, bringing all of the meaningful variables onto a common scale of the interval [0.0,1.0] The dissimilarity d(i, j) between objects i and j is defined as $\sin (i, j) = \frac{q}{q+r+s}$ (f) $\overline{f}(f)$ *f f* $\int_{f=1}^{p} \delta_{ij}^{(f)} dt$

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$$
d(i,j) = \frac{r+s}{q+r+s+t}
$$

- The dissimilarity based on such variables is called asymmetric binary dissimilarity where the number of negative matches, t, is considered unimportant and thus is ignored in the computation
- The contribution of variable f to the dissimilarity between i and j $(\mathcal S^{(f)}_{ij})$ is computed dependent on its type:

 $(i, j) = \frac{\sum_{f=1}^{j} c_{ij}}{\sum p} \frac{\delta(j)}{\delta(j)}$

 $d(i,j) = \frac{-f-1}{\sum_{i=1}^{p} \delta_i}$

 $=$

 \sum

 \circ f is binary or nominal: $\delta_{ij}^{(f)}$ = 0 if $x_{if} = x_{jf}$, or $\delta_{ij}^{(f)} = 1$ otherwise

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6. Given two objects represented by the tuples (22, 1, 42, 10) and (20, 0, 36, 8): (10)

(a) Compute the Euclidean distance between the two objects.

(b) Compute the Manhattan distance between the two objects.

(a) Euclidean distance:

$$
d(i,j) = \sqrt{(|x_{i1} - x_{j1}|^2 + |x_{i2} - x_{j2}|^2 + \dots + |x_{ip} - x_{jp}|^2)}
$$

$$
d(i,j) = \sqrt{|(20-22)|^2 + |(0-1)|^2 + |(36-42)|^2 + |(8-10)|^2}
$$

$$
= \sqrt{(2)^2 + (1)^2 + (6)^2 + (2)^2} = \sqrt{4+1+36+4}
$$

$$
= \sqrt{45} = 6.71
$$

(b) Manhattan Distance:

$$
d(i,j) = |x_{i1} - x_{j1}| + |x_{i2} - x_{j2}| + \dots + |x_{ip} - x_{jp}|
$$

$$
d(i,j) = |20-22| + |(0-1)| + |36-42| + |(8-10)|
$$

= 2+1+6+2=11

Scheme:

Each distance measure carries 5 Marks (2X5 = 10 Marks)

7. Explain the BIRCH and ROCK clustering. (10)

(i) BIRCH: Balanced Iterative Reducing and Clustering Using Hierarchies

- Incrementally construct a CF (Clustering Feature) tree, a hierarchical data structure for multiphase clustering
- A clustering feature (CF) is a three-dimensional vector summarizing information about clusters of objects.
- Given n d-dimensional objects or points in a cluster, {xi}, then the CF of the cluster is defined as: $CF = . LS, SS> where$
- o n is the number of points in the cluster
- o LS is the linear sum of the n points
- \circ SS is the square sum of the data points
- **Two phases:**
- o Phase-1: scan DB to build an initial in-memory CF tree (a multi-level compression of the data that tries to preserve the inherent clustering structure of the data)
- o Phase-2: use an arbitrary clustering algorithm to cluster the leaf nodes of the CF-tree
- o Advantage: Scales linearly finds a good clustering with a single scan and improves the quality with a few additional scans
- o Weakness: handles only numeric data, and sensitive to the order of the data record.

(ii) ROCK (RObust Clustering using linKs)

• A Hierarchical Clustering Algorithm for Categorical Attributes

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- two points, p_i and p_i , are neighbors if sim(p_i , p_i) $\geq \theta$, where
- o sim is a similarity function and
- \circ θ is a user-specified threshold
- If the number of links between two points is large, then it is more likely that they belong to the same cluster
- ROCK is more robust than standard clustering methods that focus only on point similarity
- Computational complexity: $O(n^2 + n m_m m_a + n^2 \log n)$ where m_m and m_a are the maximum and average number of neighbors, respectively, and n is the number of objects

Scheme:

For BIRCH clustering: 5 Marks For ROCK clustering: 5 Marks

- point
- $N_s(p)$: {q belongs to D | dist(p,q) <= ε}
- Directly density-reachable: A point p is directly density-reachable from a point q with respect to: ε, MinPts if
- \circ p belongs to N_ε(q)
- \circ core point condition: $|N_{\epsilon}(a)| \geq M$ MinPt
- o Density-reachable: A point p is density-reachable from a point q w.r.t ε, MinPts if there is a chain of points p_1 , ..., p_n , $p_1 = q$, $p_n = p$ such that p_{i+1} is directly density-reachable from p_i

(ii) OPTICS: Ordering Points to Identify the Clustering Structure

- Disadvantage of DBSCAN: selecting parameter values, ε and MinPts, that will lead to the discovery of acceptable clusters
- OPTICS computes an augmented cluster ordering for automatic and interactive cluster analysis
- Produces a special order of the database with respect to its densitybased clustering structure

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- **---** BCubed precision and recall metrics, which satisfy all four criteria
- The precision of an object indicates how many other objects in the same cluster belong to the same category as the object.
- The recall of an object reflects how many objects of the same category are assigned to the same cluster.

(ii) Intrinsic Methods

- intrinsic methods evaluate a clustering by examining how well the clusters are separated and how compact the clusters are
- For a data set, D, of n objects, suppose D is partitioned into k clusters, C_1 ,, C_k .
- For each object $o \in D$, we calculate a(o) as the average distance between o and all other objects in the cluster to which o belongs.
- Similarly, b(o) is the minimum average distance from o to all clusters to which o does not belong.
- The silhouette coefficient of o is then defined as:

$$
s(\boldsymbol{o}) = \frac{b(\boldsymbol{o}) - a(\boldsymbol{o})}{\max\{a(\boldsymbol{o}), b(\boldsymbol{o})\}}
$$

- o *a*(o) as the average distance between *o* and all other objects in the cluster to which o belongs
- \circ b(o) is the minimum average distance from o to all clusters to which o does not belong.

Scheme:

Each method carries equal marks (2 x 5 = 10 Marks)

- **10. Data cubes and multidimensional databases contain (10) categorical, ordinal, and numerical data in hierarchical or aggregate forms. Based on what you have learned about the clustering methods, which clustering method would you choose that finds clusters in large data cubes effectively and efficiently. Justify your answer.**
- We first need to pre-process and discretize existing data (such as ordinal and numerical data) to obtain a single dimensional discretization. We then can perform the multidimensional clustering in two steps:

i. The first step involves partitioning of the n-dimensional data space into non-overlapping rectangular units, identifying the dense units among them. This is done in 1-D for each dimension. We then can generate candidate dense units in k-dimensional space from the dense units found in $(k \mid 1)$ -dimensional space.

ii. In the second step, a minimal description for each cluster is generated. For each cluster, this determines the maximal region that covers the cluster of connected dense units. It then determines a minimal cover for each cluster.

 Using such a method, we can effectively find clusters from the data that are represented as a data cube.

Scheme: 10 Marks can be awarded for the above answer or any alternate answer with reference to the context and justification.

Scheme Of Evaluation Internal Assessment Test 3 – May 2019

