

### Kinematics of Machines (15ME42) Solution for IAT - 1

1 (a) Data  $\Rightarrow S = 40 \text{ mm}$

$$\theta_a = 90^\circ \text{ (UARM)}$$

$$D_1 = 30^\circ$$

$$\theta_d = 60^\circ \text{ (SHM)}$$

$$D_2 = 360^\circ - (90^\circ + 30^\circ + 60^\circ) \\ = 180^\circ$$

$\Rightarrow$  Knife edge follower with 20mm offset to right

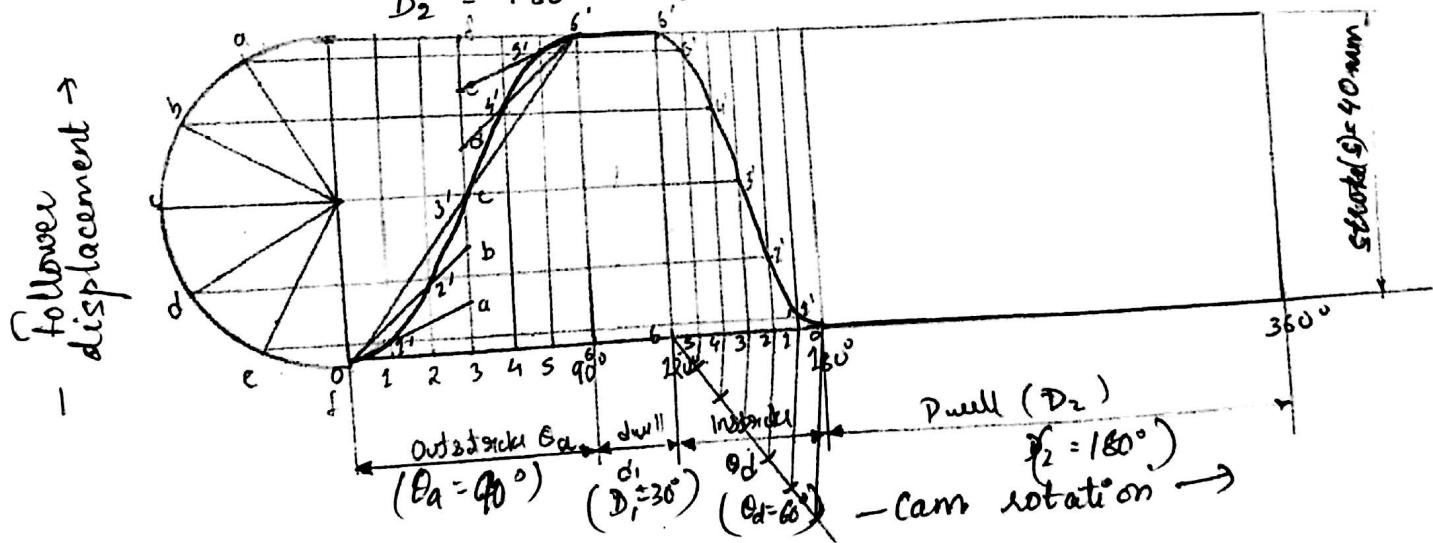
det 30° of cam rotation = 1 cm on displacement curve

$$\therefore \theta_a = 90^\circ = 3 \text{ cm}$$

$$D_1 = 30^\circ = 1 \text{ cm}$$

$$\theta_d = 60^\circ = 2 \text{ cm}$$

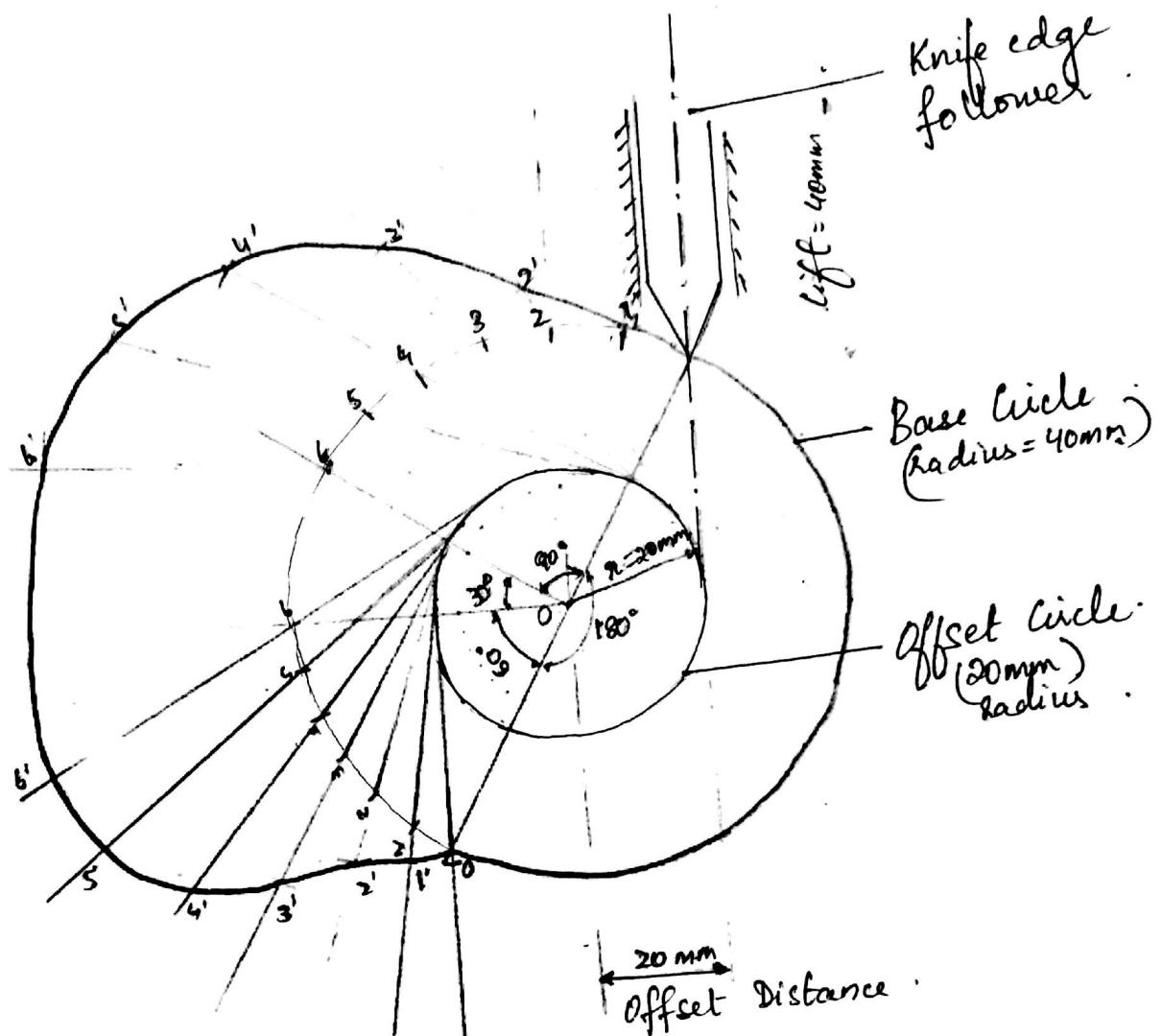
$$D_2 = 180^\circ = 6 \text{ cm}$$



Displacement Diagram

Assuming the base circle radius to be 40 mm.

Cam Profile  $\Rightarrow$



$$N = 240 \text{ rpm}$$

$$\omega = \frac{2\pi N}{60} \text{ rad/s.} = \frac{2\pi \times 240}{60} \text{ rad/s.}$$

$$\Rightarrow \omega = 8\pi \text{ rad/s.}$$

$$v_a = \frac{2\omega s}{\theta_a}$$

$$\theta_a = 90^\circ = \frac{\pi}{2} \text{ rad.}$$

$$v_a = \frac{2 \times 8\pi \times 40}{\pi/2} = 1280 \text{ mm/s} = 1.28 \text{ m/s.}$$

$$180^\circ = \pi \text{ rad.}$$

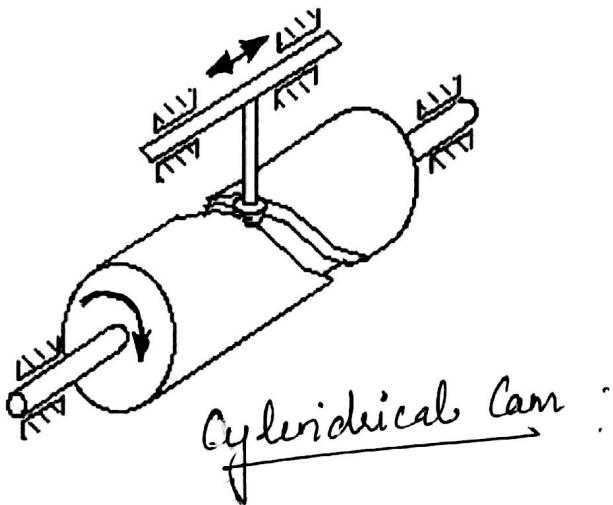
$$90^\circ = \frac{\pi}{2} \text{ rad.}$$

$$\Rightarrow \boxed{\omega_a = 1.28 \text{ rad/s}} \quad (\text{ans})$$

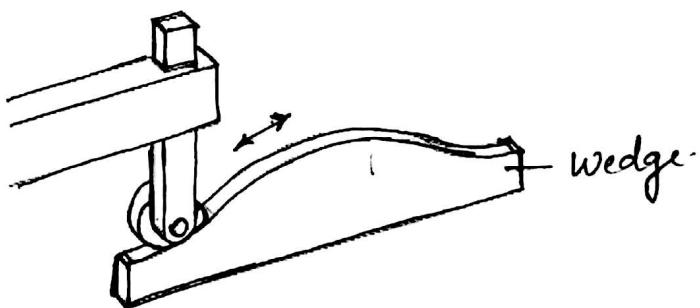
$$a_a = \frac{4w^2 S}{\theta_a^2} = \frac{4 \times 8\pi \times 8\pi \times 40}{(\pi/2)^2} = 40960 \text{ mm/s}^2$$

$$\Rightarrow \boxed{a_a = 40.96 \text{ m/s}^2} \quad (\text{ans})$$

1 (b) (i)



(ii).

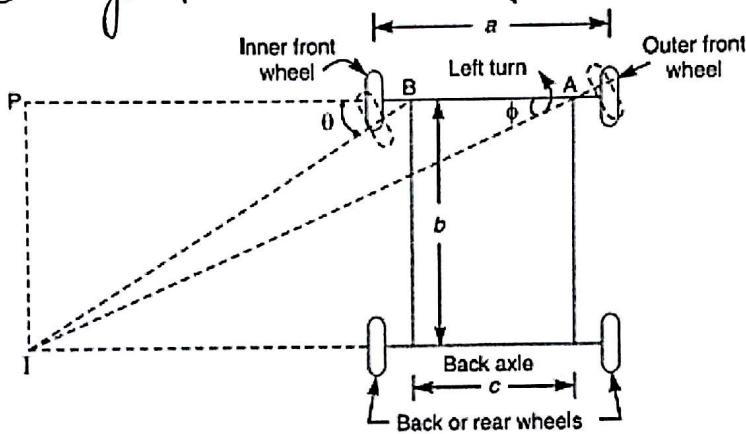


2

2 (a) The steering gear mechanism is used for changing the direction of two or more of the wheel axles with reference to the chassis, so as to move the automobile in any desired path.

Condition for correct steering:

All the four wheels must turn about the same instantaneous centre (I). The axis of the inner wheel makes a larger turning angle ' $\theta$ ' than the angle ' $\phi$ ' subtended by the axis of outer wheel.



Let  $a$  = wheel track.

$b$  = wheel base

$c$  = Distance between the pivots A and B of the front axle.

Now from triangle,  $\triangle IBP$ ;

$$\text{let } \theta = \frac{BP}{IP}$$

and from  $\triangle IAP$ ;

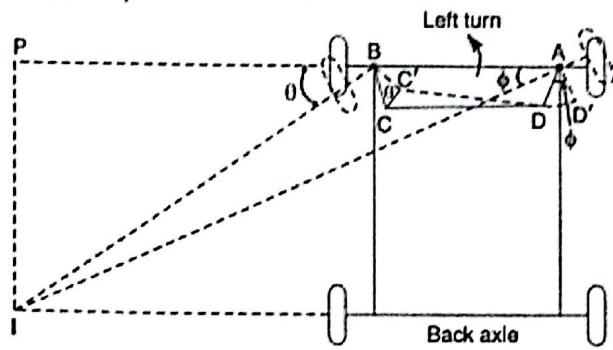
$$\cot \phi = \frac{AP}{IP} = \frac{AB + BP}{IP} = \frac{AB}{IP} + \frac{BP}{IP}$$

$$\Rightarrow \cot \phi = \frac{c}{b} + \cot \theta \Rightarrow \boxed{\cot \phi - \cot \theta = \frac{c}{b}}$$

This is the fundamental equation for correct steering.

## 2 (b) Ackerman Steering Gear Mechanism : $\Rightarrow$

- The Ackerman Steering Gear mechanism consists of turning pairs only. Hence, the maintenance of such mechanism is reduced as there are no sliding pairs that would contribute to



rubbing or friction.

- The whole of the mechanism is on back of the front wheels.
  - In Ackerman steering gear, the mechanism ABCD is a four bar crank chain as is shown in the figure.
  - The shorter links BC and AD are of equal length and are connected by hinge joints with front wheel axles.
  - The longer links AB and CD are of unequal length.
  - The following are the only three positions for correct steering :  $\Rightarrow$
- (i) When the vehicle moves along a straight path, the longer links AB and CD are parallel and the shorter links BC and AD are equally inclined to the longitudinal axis of the vehicle, as shown by the firm lines in the above figure.
- (ii) When the vehicle is steering to the left, the position

(b)

of the gear is shown by dotted lines in the figure.  
In this position, the lines of the front wheel axle intersect on the back wheel axle at I for correct steering.

(iii) When the vehicle is steering to the right, the similar position may be obtained.

3(a). The mechanisms used for permitting only relative motion of an oscillatory nature along a straight line is called a straight line motion mechanism.

Condition for straight line mechanism :-

$$AQ \times OP = \text{constant}.$$

(b). The ~~link~~ mechanism consists of 8 links.

Geometric relation :-

$$OA = OQ$$

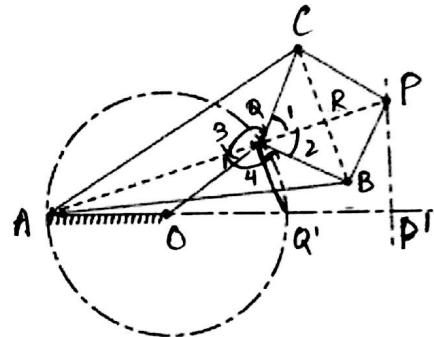
$$AB = AC$$

$$BP = PC = CQ = QB \quad (\text{sides of rhombus})$$

Trace Point is P.

(c) OA is the fixed link and OQ is a rotating link or crank.

To prove :- As the link OQ moves around O; P moves in a straight line  $\perp$  to OA. All the joints are pin-jointed.



(7)

∴ BPCQ is a rhombus;

QP always bisects  $\angle BQC$ ;

$$\Rightarrow \angle 1 = \angle 2 \quad \text{--- } ① \text{ in all positions.}$$

In  $\triangle AQC$  and  $\triangle AQB$ ;

AQ is common;

$$AC = AB.$$

$$QC = QB.$$

Hence  $\triangle AQC \cong \triangle AQB$ ; in all positions.

$$\Rightarrow \angle 3 = \angle 4 \quad \text{--- } ②.$$

Adding Eqn ① & ②;

$$\angle 1 + \angle 3 = \angle 2 + \angle 4.$$

$$\text{But } \angle 1 + \angle 2 + \angle 3 + \angle 4 = 360^\circ.$$

$$\Rightarrow \angle 1 + \angle 3 = \angle 2 + \angle 4 = 180^\circ \Rightarrow A, Q \& P \text{ lie}$$

on a straight line.  
Let  $PP'$  be the  $\perp^{\circ}$  on  $AO$  produced.

From  $\triangle AQQ'$  &  $\triangle APP'$

$$\angle S is common; \angle AAQ' = \angle APP' = 90^\circ.$$

$$\Rightarrow \triangle AQQ' \sim \triangle APP'.$$

$$\therefore \frac{AQ}{AP'} = \frac{AQ'}{AP}$$

$$\Rightarrow AQ' \times AP' = AQ \times AP = (AR - RQ)(AR + RP)$$

$$= (AR - RQ)(AR + RQ).$$

$$\Rightarrow AQ' \times AP' = AR^2 - RQ^2$$

$$= (AC^2 - CR^2) - (CQ^2 - CR^2).$$

$$\Rightarrow \boxed{AP' = \frac{AC^2 - CQ^2}{AQ'}}$$

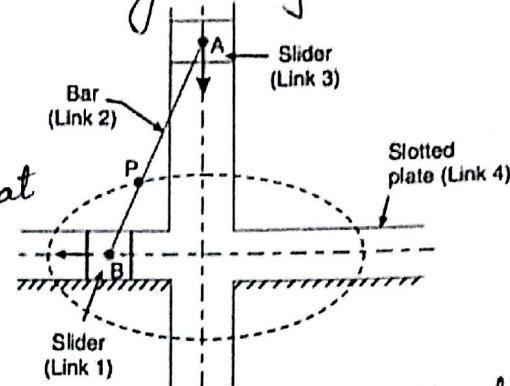
= Constant as  $AC, CQ$  and  $AQ'$  are always fixed.

This means that the projection of P and AQ produced is constant for all the configurations.

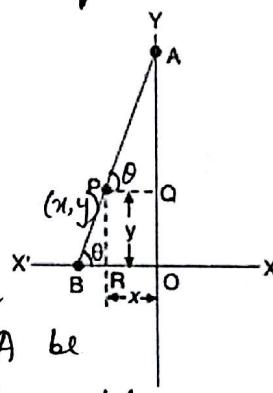
Thus,  $PP'$  is always a normal to  $AO$  produced or P moves in a straight line  $\perp^{\circ}$  to  $AO$ .

4(a). Elliptical trammel is an inversion of Double slider crank mechanism.

- This inversion is obtained by fixing the slotted plate (link 4).
- The fixed plate has two straight grooves cut in it, at right angles to each other.
- The link 1 and link 3 are known as sliders and form sliding pairs with link 4.
- The link AB (link 2) is a bar which forms turning pair with links 1 and 3.
- It is an instrument used for drawing ellipses.
- When the links 1 and 3 slide along their respective grooves, any point on the link 2 such as P traces out an ellipse on the surface of link 4.
- AP and BP are the semi-major axis and semi-minor axis of the ellipse respectively.



(b). Let us take OX and OY as horizontal and vertical axes and let the link BA be inclined at an angle  $\theta$  with the horizontal. P has the coordinates as  $(x, y)$ .



$$\text{From } \triangle PAQ; \cos \theta = \frac{x}{AP} \quad \text{--- (1)}$$

$$\triangle PBR; \sin \theta = \frac{y}{BP} \quad \text{--- (2)}$$

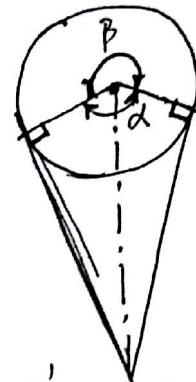
Squaring and adding Eq<sup>n</sup> (1) & (2) :

$$\frac{x^2}{AP^2} + \frac{y^2}{BP^2} = \sin^2 \theta + \cos^2 \theta = 1.$$

This is the equation of an ellipse. Hence the path traced by point P is an ellipse whose semimajor axis is AP and semi-minor axis is BP.

5 a.) A quick return motion mechanism is one in which the return stroke takes appreciably lesser time than the forward stroke.

- The forward stroke takes place when the crank rotates by an angle  $\beta$  and the return stroke takes place when the crank rotates by an angle ' $\alpha$ '.
- ~~The~~ angle  $\beta$  made by the forward or cutting stroke is greater than the angle ' $\alpha$ ' described by the return stroke.
- Since the crank rotates with uniform angular speed, therefore the return stroke is completed within a shorter time. Thus, such a mechanism is called as a quick return motion mechanism.



b.) Data:  $\rightarrow AC = 300 \text{ mm}$ .

$$CB_1 = 120 \text{ mm}.$$

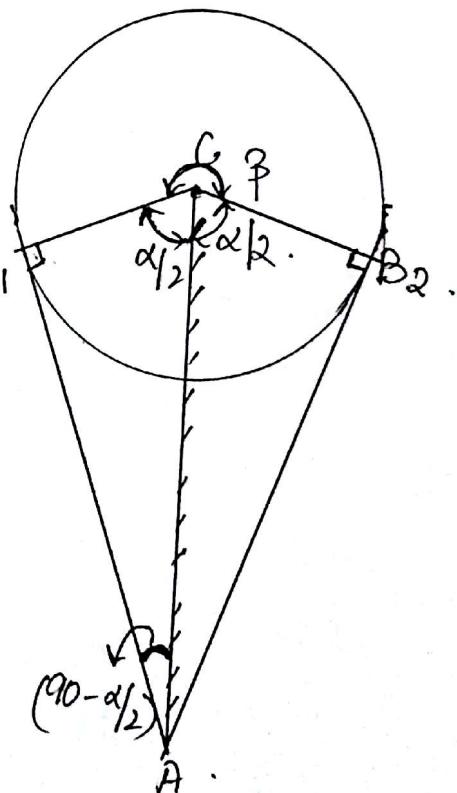
$$\begin{aligned} \sin \angle CAB_1 &= \sin(90^\circ - \alpha/2) = \frac{CB_1}{AC} \\ &= \frac{120}{300} = 0.4. \end{aligned}$$

$$\Rightarrow \angle CAB_1 = 90 - \alpha/2.$$

$$= \sin^{-1}(0.4) = 23.6^\circ.$$

$$\alpha/2 = 90 - 23.6^\circ = 66.4^\circ$$

$$\Rightarrow \alpha = 2 \times 66.4^\circ \Rightarrow \boxed{\alpha = 132.8^\circ}$$

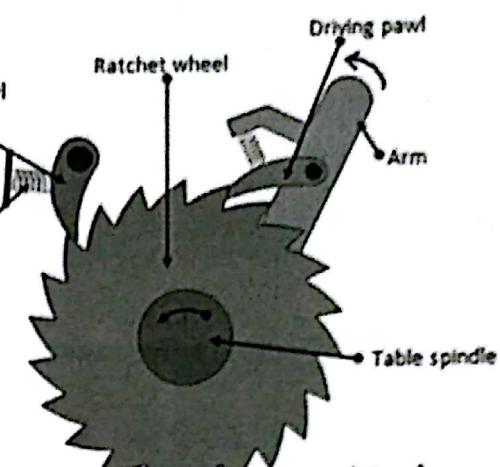


$$\text{Time Ratio (T.R)} = \frac{\text{Time of cutting stroke}}{\text{Time of return stroke}} = \frac{360^\circ - \alpha}{\alpha} = \frac{360^\circ - 132.8^\circ}{132.8^\circ}.$$

$$\Rightarrow \boxed{\text{Time Ratio} = 1.72} \quad (\text{Ans})$$

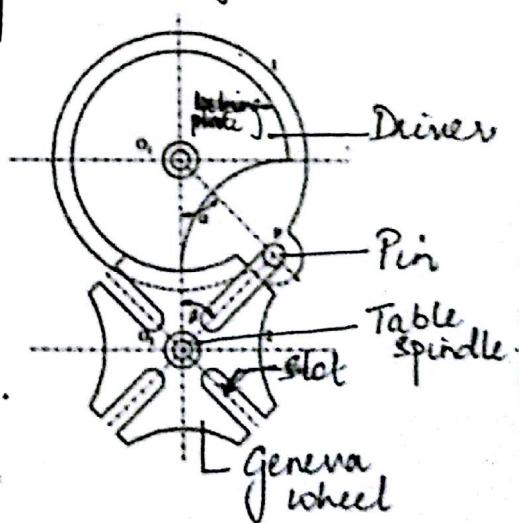
## 6 (i) Ratchet and Pawl Mechanism : $\Rightarrow$

- A ratchet is a device that allows linear or rotary motion in only one direction.
- The figure besides is a ratchet and pawl mechanism.
- Ratchet consists of a gearwheel and a pivoting sprung loaded pawl that engages the teeth.
- The teeth or the pawl, are at an angle so that when the teeth are moving in one direction, the pawl slides in between the teeth.
- The spring forces the pawl back into the depression between the next teeth.
- The ratchet and pawl are not mechanically interlocked hence easy to set-up. But the reverse motion of the ratchet is stopped by the locking pawl.
- It is an example of an intermittent motion mechanism.
- It finds its application in currency counting machines, indexing, etc.



## (ii) Geneva Wheel Mechanism : $\Rightarrow$

- The geneva wheel mechanism translates a continuous rotation into an intermittent rotary motion.
- The rotating drive wheel has a pin that reaches into the slot of the driver wheel or the geneva wheel.
- The drive wheel also has a raised circular blocking disc that locks the driver wheel in position between



steps as shown in the above.

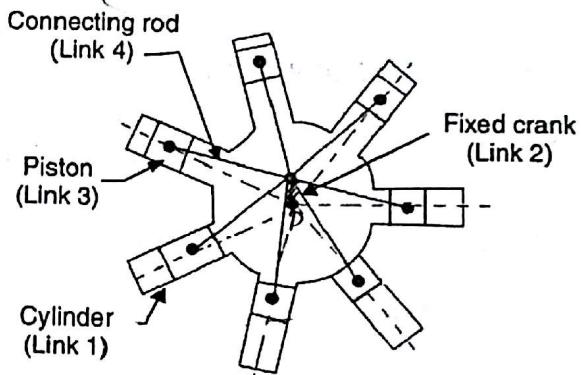
- In the simplest form, the driven wheel has four slots and hence for each rotation of the drive wheel, it advances by one step of  $90^\circ$ .
- If the driven wheel has 'n' slots, it advances by  $360/n$  per full rotation of the drive wheel.

(iii) Gnome Engine  $\Rightarrow$

- Gnome engine is rotary internal combustion engine.

- Previously Gnome engines were used in aviation.

. But now-a-days gas turbines are used in its place because of its high weight to power ratio and vibrations associated.



- It consists of seven cylinders in one plane and all revolves about a fixed centre, D, as shown in the figure.

- In this mechanism, as the connecting rod (link 4) rotates, the piston (link 3) reciprocates inside the cylinders forming link 1 thereby producing power continuously.