

USN

--	--	--	--	--	--	--	--	--	--	--

14ELD21

**Second Semester M.Tech. Degree Examination, Dec.2018/Jan.2019**  
**Modern DSP**

Time: 3 hrs.

Max. Marks:100

**Note: Answer any FIVE full questions.**

- 1
  - a. How are discrete – time signals and systems classified? (08 Marks)
  - b. Define N-point DFT and IDFT of a sequence. (04 Marks)
  - c. Find the 8-point DFT of  $x(n) = \{1, 1, 0, 0, 0, 0, 0, 0\}$  use the property of conjugate symmetry. (08 Marks)
- 2
  - a. Let  $x(n) = (1, 2, 0, 3, -2, 4, 7, 5)$ . Evaluate the following :
    - i)  $X(0)$       ii)  $X(4)$       iii)  $\sum_{k=0}^7 X(k)$       iv)  $\sum_{k=0}^7 |x(k)|^2$ . (10 Marks)
  - b. If DFT of  $x(n)$  is  $X(K)$ , then prove the following properties.
    - i)  $\text{DFT}\{w_N^{-\ell n} x(n)\} = X((K - \ell))_N$  (03 Marks)
    - ii)  $\text{DFT}\{x((-n))_N\} = X((-K))_N$  (03 Marks)
    - iii)  $\text{DFT}\{x((n - m))_N\} = w_N^{mk} X(K) \quad 0 \leq K \leq N - 1$ . (04 Marks)
- 3
  - a. Design a digital FIR low-pass filter with
 
$$H_d(e^{j\omega}) = \begin{cases} e^{-j\omega} & -\frac{\pi}{4} \leq \omega \leq \frac{\pi}{4} \\ 0 & \frac{\pi}{4} \leq |\omega| \leq \pi \end{cases}$$
 using a Hamming window with  $N=7$ . (20 Marks)
- 4
  - a. Explain how an analog filter is mapped on to a digital using impulse invariance method. What are the limitations of the method? (10 Marks)
  - b. Convert the analog filter with transfer function :
 
$$H(s) = \frac{(s + a)}{(s + a)^2 + b^2}$$
 into a digital filter using the impulse invariant transformation. (10 Marks)
- 5
  - a. Design a low-pass Butterworth filter using the bilinear transformation method for satisfying the following constraints.
 

Passband	: 0 – 400 Hz	stopband	: 2.1 KHz
passband ripple	: 2dB	stopband attenuation	: 20 dB
sampling frequency	: 10 KHz.		

(10 Marks)
  - b. Design a Chebyshev IIR digital low-pass filter to satisfy the constraints :
 
$$0.707 \leq |H(\omega)| \leq 1 \quad 0 \leq \omega \leq 0.2\pi$$

$$|H(\omega)| \leq 0.1 \quad 0.5\pi \leq \omega \leq \pi$$
 using bilinear transformation and assuming  $T = 1s$ . (10 Marks)

- 6 a. Explain the decimation process for an integer factor  $D$ . (10 Marks)  
b. Consider the signal  $x(n) = n u(n)$   
i) Determine the spectrum of the signal  
ii) The signal is applied to a decimator that reduces the sampling rate by a factor 3 determine the output spectrum. (10 Marks)
- 7 a. Describe the polyphase structure for decimation and interpolation filters. (10 Marks)  
b. Explain clearly two applications of multi-rate digital signal processing. (10 Marks)
- 8 a. Derive the expression of direct form Recursive least Square (RLS) algorithm. (10 Marks)  
b. Explain four applications of adaptive filters. (10 Marks)

\* \* \* \* \*

CMRIT LIBRARY  
BANGALORE - 560 037