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Second Semester M.Tech. Degree Examination, Dec.2017/Jan.2018

Modern DSP

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions.

- 1 a. Define signals and system. Explain classifications of signals with example. (14 Marks)
 b. Consider the analog signal $x_a(t) = 3 \cos 2000\pi t + 5 \sin 6000\pi t + 10 \cos 12000\pi t$:
 i) What is the Nyquist rate for this signal?
 ii) Assume now that we sample this signal using a sampling rate $F_s = 5000$ samples/s. What is the discrete time signal obtained after sampling? (06 Marks)

- 2 a. Consider the signal $x(n) = a^n u(n)$, $0 < a < 1$. The spectrum of this signal is sampled at frequencies $\omega_k = 2\pi k/N$, $k = 0, 1, \dots, N-1$. Determine the reconstructed spectra for $a = 0.8$ when $N = 5$ and $N = 50$. (08 Marks)
 b. State and prove the following properties:
 i) Circular time shift of a sequence. (06 Marks)
 ii) Circular correlation. (06 Marks)
 c. Explain the use of the DFT in linear filtering. (06 Marks)

- 3 a. Explain characteristics of practical frequency-selective filters. (06 Marks)
 b. Explain the design of linear phase FIR filter using windows. (06 Marks)
 c. Determine the coefficients of a linear-phase FIR filter of length $M = 15$ which has a symmetric unit sample response and a frequency response that satisfies the conditions

$$H\left(\frac{2\pi k}{15}\right) = \begin{cases} 1, & K = 0, 1, 2, 3 \\ 0.4, & K = 4 \\ 0, & K = 5, 6, 7 \end{cases}$$
 (08 Marks)

- 4 a. Determine the order and the poles of a type 1 lowpass Chebyshev filter that has a 1 dB ripple in the passband, a cutoff frequency $\Omega_p = 1000 \pi$, a stop band frequency of 2000π , and an attenuation of 40 dB or more for $\Omega \geq \Omega_s$. (12 Marks)
 b. Explain the frequency transformation in digital domain. (08 Marks)

- 5 a. Explain the design and implementation for sampling rate conversion using polyphase filter structure. (10 Marks)
 b. Explain the sampling rate conversion of bandpass signals. (10 Marks)

- 6 a. Briefly explain the practical applications of multirate signal processing. (08 Marks)
 b. Explain the analysis and synthesis of uniform DFT filter banks. (12 Marks)

- 7 a. Write a note on two-channel quadrature mirror filter bank. (10 Marks)
 b. Define adaptive filter. Explain steps used to implement LMS algorithm. (10 Marks)

- 8 a. Describe the applications of adaptive filter. (08 Marks)
 b. Derive the filter coefficient updating equation using RLS algorithm. (12 Marks)

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