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**Internal Assessment Test 2 – April. 2019**

Sub:	Wireless Cellular and LTE 4G Broadband				Sub Code:	15EC81	Branch:	ECE
Date:	15/04/2019	Duration:	90 min's	Max Marks:	50	Sem / Sec:	VIII A,B,C & D	OBE

Answer any FIVE FULL Questions

	MARKS	CO	RBT
1. Explain the key steps in OFDM communication system with the help of block diagram.	[10]	CO1	L1
2. What is meant by PAR? Derive the equation for analog and discrete representation of PAR. Explain any one method for the reduction of PAR.	[10]	CO1	L2
3. Illustrate the use of Cyclic Prefix in OFDM and derive the formula for rate loss	[10]	CO1	L3
4. Describe the principle of OFDMA in LTE Downlink with relevant block diagrams	[10]	CO1	L2
5. Show that the received SNR increase linearly with the number of receiver antennas in the concept of Spatial Diversity.	[10]	CO1	L3
6. Distinguish between Selection combining and maximal ratio combining in terms of average received SNR.	[10]	CO1	L2
7. Analyze Open-Loop Transmit diversity with the help of 2x2 SFBC, 4X2 Stacked STBCs and 4X2 in LTE.	[10]	CO1	L4

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**Scheme Of Evaluation**  
**Internal Assessment Test 2 – April.2019**

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**Note:** Answer Any Five Questions

Question #	Description	Marks Distribution	Max Marks
1	<p><b>Explain the key steps in OFDM communication system with the help of block diagram.</b></p> <ul style="list-style-type: none"> <li>Block Diagram</li> <li>Explanation</li> <li>OFDM in LTE</li> </ul>	<p>4 M</p> <p>4 M</p> <p>2 M</p>	10 M
2	<p><b>What is meant by PAR? Derive the equation for analog and discrete representation of PAR. Explain any one method for the reduction of PAR.</b></p> <ul style="list-style-type: none"> <li>Definition of PAR</li> <li>Equations of PAR</li> <li>Method for reduction of PAR</li> </ul>	<p>2 M</p> <p>5 M</p> <p>3 M</p>	10 M
3	<p><b>Illustrate the use of Cyclic Prefix in OFDM and derive the formula for rate loss</b></p> <ul style="list-style-type: none"> <li>Cyclic Prefix added Input diagram</li> <li>Explanation with equations</li> <li>Formula for Rate Loss</li> </ul>	<p>2 M</p> <p>6 M</p> <p>2 M</p>	10 M
4	<p><b>Describe the principle of OFDMA in LTE Downlink with relevant block diagrams</b></p> <ul style="list-style-type: none"> <li>Block Diagram</li> <li>Explanation</li> </ul>	<p>4 M</p> <p>6 M</p>	10 M
5	<p><b>Show that the received SNR increase linearly with the number of receiver antennas in the concept of Spatial Diversity.</b></p> <ul style="list-style-type: none"> <li>Explanation of</li> </ul>	<p>2 M</p> <p>6 M</p>	10 M

		<p>Array Gain</p> <ul style="list-style-type: none"> <li>• Equations for Array Gain</li> <li>• Performance Graph</li> </ul>	2 M	
6		<p><b>Distinguish between Selection combining and maximal ratio combining in terms of average received SNR.</b></p> <ul style="list-style-type: none"> <li>• Selection Combining</li> <li>• Maximal Ratio Combining</li> </ul>	5 M 5 M	10 M
7		<p><b>Analyze Open-Loop Transmit diversity with the help of 2x2 SFBC, 4X2 Stacked STBCs and 4X2 in LTE.</b></p> <ul style="list-style-type: none"> <li>• Explanation of 2x2 SFBC with equations</li> <li>• Explanation of 4x2 stacked STBC with equations</li> <li>• Explanation of 4x2 in LTE</li> </ul>	3 M 4 M 3 M	10 M

1. Explain the key steps in OFDM communication system with the help of block diagram. – 10 Marks



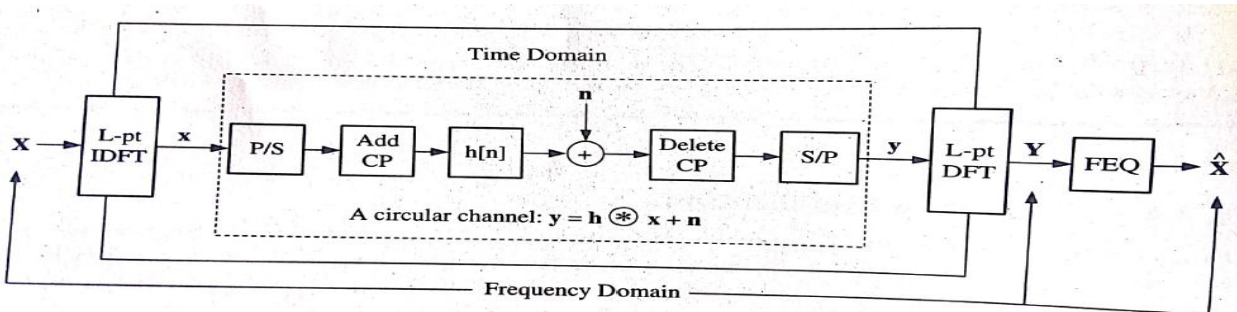
## OFDM Block Diagram

- 1<sup>st</sup> step in OFDM is to break a wideband signal of BW  $B$  into  $L$  narrowband signals (subcarriers) each of BW  $B/L$ .
- **Symbol rate is maintained** but each subcarrier experiences flat fading or ISI free communication – as long as **cyclic prefix**  $\gg$  **delay spread** is used.
- The  $L$  subcarriers for a given OFDM symbol are represented by a vector  $\mathbf{X}$ , which contains the  $L$  current symbols.
- To use a single wideband radio instead of  $L$  independent narrow band radios, the subcarriers are created digitally using an IFFT operation.
- In order for the IFFT/FFT to decompose the ISI channel into orthogonal subcarriers, a cyclic prefix of length  $\nu$  must be appended after the IFFT operation.

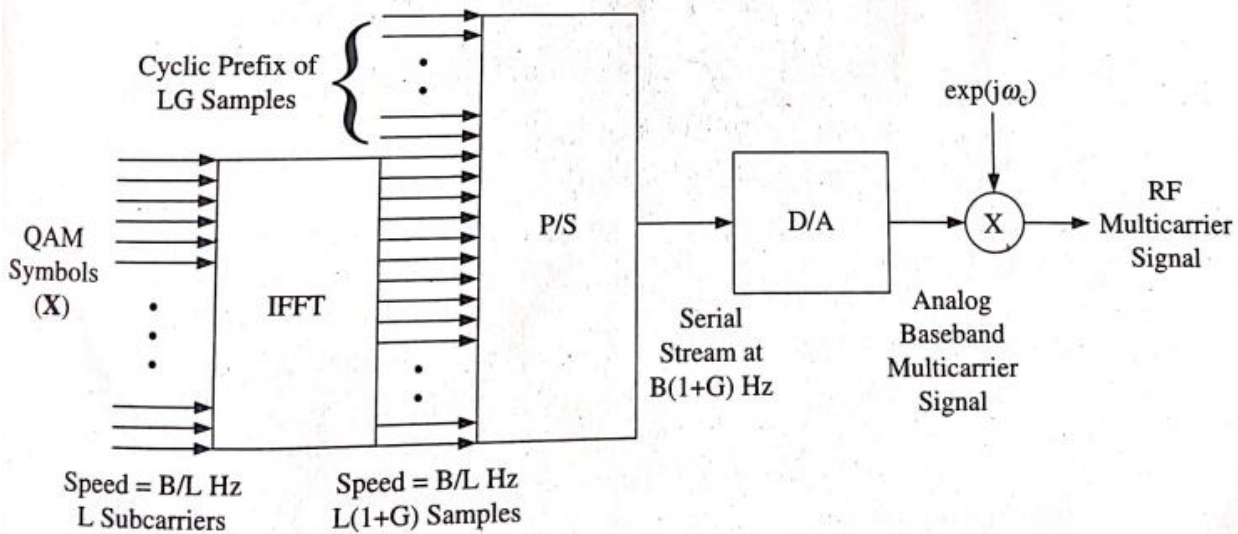


## OFDM Block Diagram

- $L+\nu$  symbols are sent **serially** through the **wideband channel**.
- At the RX the cyclic prefix is discarded and the  $L$  received symbols are demodulated using FFT operation - giving  $L$  data symbols, each of the form  $Y_\ell = H_\ell X_\ell + N_\ell$  for subcarrier  $\ell$
- Each subcarrier is equalized by FEQ – by dividing by  $H_\ell$
- Result is  $\hat{X}_\ell = X_\ell + N_\ell / H_\ell$ .



## OFDM in LTE



### 3.3 - OFDM in LTE

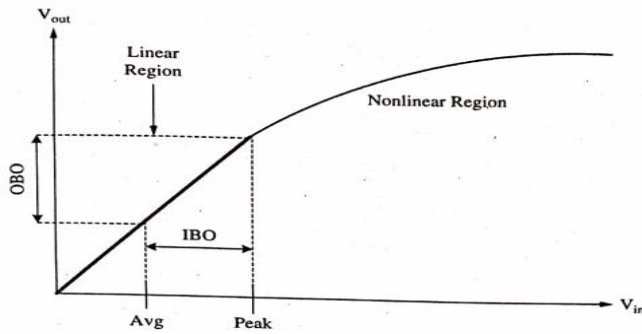
- Inputs are  $L$  independent QAM symbols (vector  $X$ ), these  $L$  symbols are treated as separate subcarriers.
- These  $L$  data-bearing symbols can be created from a bit stream by a **symbol mapper** and **serial-to-parallel converter**.
- $L$  point IFFT then creates a time domain  $L$ -vector  $X$  that is cyclic extended to have a length  $L(1+G)$ ,  $G$ - fractional overhead.  $G = 0.07$  - normal cyclic prefix,  $G = 0.25$  - extended cyclic prefix.
- This vector is then parallel-to-serial converted into a wideband digital signal, that can be amplitude modulated at a carrier frequency  $\omega_c/2\pi$ .
- **Data rate of LTE system** with 16QAM

$$\begin{aligned}
 R &= \frac{B L_d \log_2(M)}{L (1+G)} \\
 &= \frac{10^7 \text{ MHz } 600 \log_2(16)}{1024 \cdot 1.07} = 21.9 \text{ Mbps.}
 \end{aligned}$$

2. What is meant by PAR? Derive the equation for analog and discrete representation of PAR. Explain any one method for the reduction of PAR. – 10 Marks

- OFDM signals have high PAR – peak-to-average power ratio (PAPR).
- Because – in the time domain a multicarrier signal is **the sum of many narrowband signals** – this value can be large and small – **larger than average value**.
- High PAR is an important challenge as it reduces efficiency and increases cost of **RF power amplifier**.
- Same power amplifier can be used with reduced input power – **input backoff IBO** – causes lower average SNR at the Rx.
- When high-peak signal is transmitted through nonlinear device – HPA / DAC – generates **in-band distortion** – severely degrading the system performances.
- Typical Power amplifier response with input & output backoff regions

- **To avoid distortion** - High peak power signals are transmitted in the **Linear region** – by decreasing average power of input signal.
- Input backoff IBO resulting in proportional output backoff OBO.



## Quantifying the PAR

- Since multicarrier systems transmit data over a no. of parallel frequency channels, resulting waveform is superposition of L narrowband signals.
- Each of the output samples from an L-point IFFT operation involves sum of L complex numbers.
- Due to Central Limit Theorem resulting output values  $\{x_1, x_2, \dots, x_L\}$  can be accurately modelled as complex Gaussian random variables with zero mean & variance  $\sigma^2 = \mathcal{E}_x/2$ ,
- Amplitude of the output signal  $|x[n]| = \sqrt{(\Re\{x[n]\})^2 + (\Im\{x[n]\})^2}$ ,
- $|x[n]|$  is complex Gaussian like narrowband fading the envelop  $|x[n]|$  is Rayleigh distributed.
- Output power  $|x[n]|^2 = (\Re\{x[n]\})^2 + (\Im\{x[n]\})^2$ , which is exponentially distributed with mean  $2\sigma^2$ .



## Quantifying the PAR

$$PAR \triangleq \frac{\max_t |x(t)|^2}{E[|x(t)|^2]}$$

- PAR of the transmitted signal is defined as :
- Usually PAR is considered for a single OFDM symbol, consisting of  $L+N_g$  samples or a time duration of  $T$ .
- Discrete PAR for IFFT output : 
$$PAR \triangleq \frac{\max_{l \in (0, L+N_g)} |x_l|^2}{E[|x_l|^2]} = \frac{\mathcal{E}_{\max}}{\mathcal{E}_x}$$
- Complementary cumulative distribution function CCDF= 1-CDF of the PAR is the most commonly used measure.
- Van Nee and de Wild introduced a simple and accurate approximation of the CCDF for large L ( $\geq 64$ )
- $$CCDF(L, \mathcal{E}_{\max}) = 1 - F(L, \mathcal{E}_{\max})^{\beta L} = 1 - \left(1 - \exp\left(-\frac{\mathcal{E}_{\max}}{2\sigma^2}\right)\right)^{\beta L}$$



## Clipping and Other PAR Reduction Techniques

- To avoid HPA operating in the nonlinear region, input power is reduced to an amount equal to PAR – this will reduce SNR by the same amount.
- PAR reduction –
- Some highest PAR values can be clipped off – reducing some amount of distortion – still some amount of distortion remains.
- **Clipping** – also called soft limiting – truncates the amplitude of the signal that exceed the clipping level as  $\tilde{x}[n] = \begin{cases} Ae^{j\angle x[n]}, & \text{if } |x[n]| > A \\ x[n], & \text{if } |x[n]| \leq A \end{cases}$
- Original signal is  $x[n]$ , output after clipping  $\tilde{x}[n]$
- A = clipping level.
- Clipping ratio is defined as  $\gamma \triangleq \frac{A}{\sqrt{E\{|x[n]|^2\}}} = \frac{A}{\sqrt{\mathcal{E}_x}}$
- Clipping reduces PAR at the expense of distorting the desired signal.

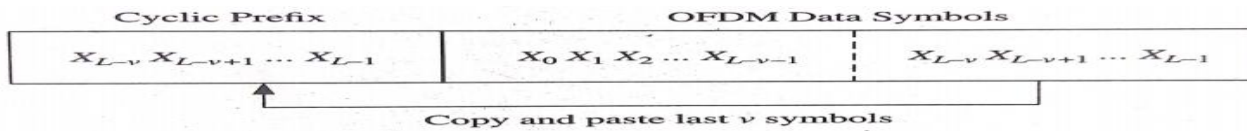
3. Illustrate the use of Cyclic Prefix in OFDM and derive the formula for rate loss – 10 Marks



## Cyclic Prefix

- To realize OFDM in practice – FFT algorithm is utilized for computing DFT and IFFT algorithm for computing IDFT – *reduces no. of multiplication & addition.*
- IFFT operation at the transmitter allows all the subcarriers to be created in the digital domain and **requires a single radio link.**
- Channel must provide circular convolution for IFFT/FFT to create ISI free channel –  $y[n] = x[n] \circledast h[n]$
- If maximum delay spread has a duration – **v+1** samples, then by adding a **guard band of v samples** between OFDM symbols, each OFDM symbol is made **independent** of those coming before and after it.
- Such OFDM symbol is represented in time domain as a length **L** vector  **$X=[x_1, x_2, \dots, x_L]$**





- After applying a cyclic prefix of length  $v$  – transmitted signal

$$\mathbf{x}_{cp} = \left[ \underbrace{x_{L-v} \ x_{L-v+1} \ \dots \ x_{L-1}}_{\text{Cyclic prefix}} \ \underbrace{x_0 \ x_1 \ \dots \ x_{L-1}}_{\text{Original data}} \right].$$

- Channel output is  $\mathbf{y}_{cp} = \mathbf{h} * \mathbf{x}_{cp}$ ,
- Where  $\mathbf{h}$  – is a length  $v+1$  vector describing the impulse response of the channel during the OFDM symbol.
- Output  $\mathbf{y}_{cp}$  has  $(L+v) + (v+1) - 1 = L+2v$  samples – input  $(L+v)$  impulse response  $(v+1)$
- 1st  $v$  samples of  $\mathbf{y}_{cp}$  has interference from the preceding OFDM symbol - discarded. Last  $v$  samples disperse into the subsequent OFDM symbol – discarded.
- This leaves exactly  $L$  samples for the desired output  $\mathbf{Y}$ .

## Cyclic Prefix

- Consider only the 1<sup>st</sup> element of  $\mathbf{y}$  –  $y_0$ . Due to cyclic prefix  $y_0$  depends on  $\mathbf{x}_0$  and the circularly wrapped values  $x_{L-v} \dots x_{L-1}$ .

- That is  $y_0 = h_0 x_0 + h_1 x_{L-1} + \dots + h_v x_{L-v}$

$$y_1 = h_0 x_1 + h_1 x_0 + \dots + h_v x_{L-v+1}$$

⋮

$$y_{L-1} = h_0 x_{L-1} + h_1 x_{L-2} + \dots + h_v x_{L-v-1}$$

- Due to circular convolution – a cyclic prefix that is at least as long as the **channel duration** allows the channel output  $\mathbf{y}$  to be decomposed into a simple multiplication of the channel frequency response  $\mathbf{H} = \text{DFT}\{\mathbf{h}\}$  and the channel frequency domain input  $\mathbf{X} = \text{DFT}\{\mathbf{x}\}$ .
- Rate Loss = Power Loss =  $L/(L+v)$** . If  $L \gg v$  – inefficiency can be reduced.

### 4. Describe the principle of OFDMA in LTE Downlink with relevant block diagrams – 10 Marks

#### 4.2- Orthogonal Frequency Division Multiple Access (OFDMA)

- OFDMA system allocates users time-frequency slices consisting of  $M$  sub-carriers over some no. of consecutive OFDM symbols.
- The  $M$  sub-carriers can be arranged as :
  - Bunched together** in  $M$  contiguous sub-carriers –
    - Band AMC – uses subcarriers with almost equal SINR and chooses the best coding and modulation scheme for it.
    - If accurate SINR information is available at the RX, band AMC gives better performance.
  - Spread out over the band** – distributed allocation -
    - Provides frequency diversity over the entire band and uses interleaving and coding to correct errors.
    - For a highly mobile system distributed allocation provides maximum diversity.

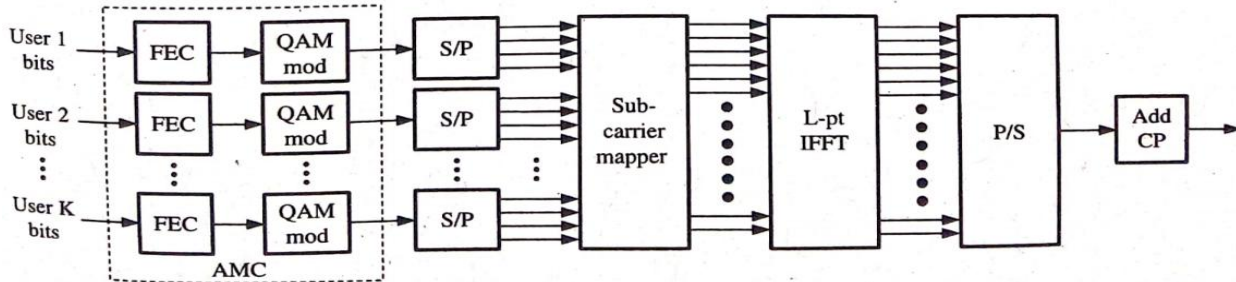




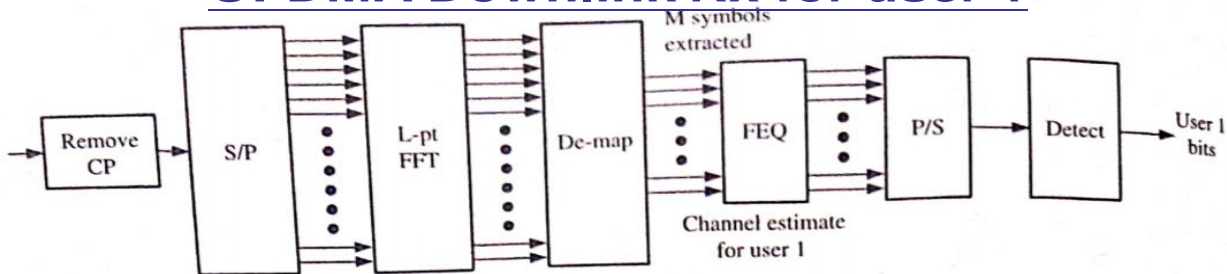
## OFDMA : How it works

- Basic flow of OFDMA is similar to OFDM system – except for now  $K$  users share the  $L$  subcarriers, with each user being allocated  $M_k$  subcarriers.
- In practise each user have one subcarrier assigned to them.
- At each Rx, user is concerned only about its **own  $M_k$  subcarrier**, but it applies  $L$  point FFT on the entire received signal to extract the desired subset of subcarriers.
- OFDMA downlink Rx must demodulate the entire received signal – wastes power.
- Digital separation of users is simple to implement at the Rx .
- Interferences are low in OFDMA compared to CDMA, FDMA.

### OFDMA Downlink Tx



### OFDMA Downlink Rx for user 1



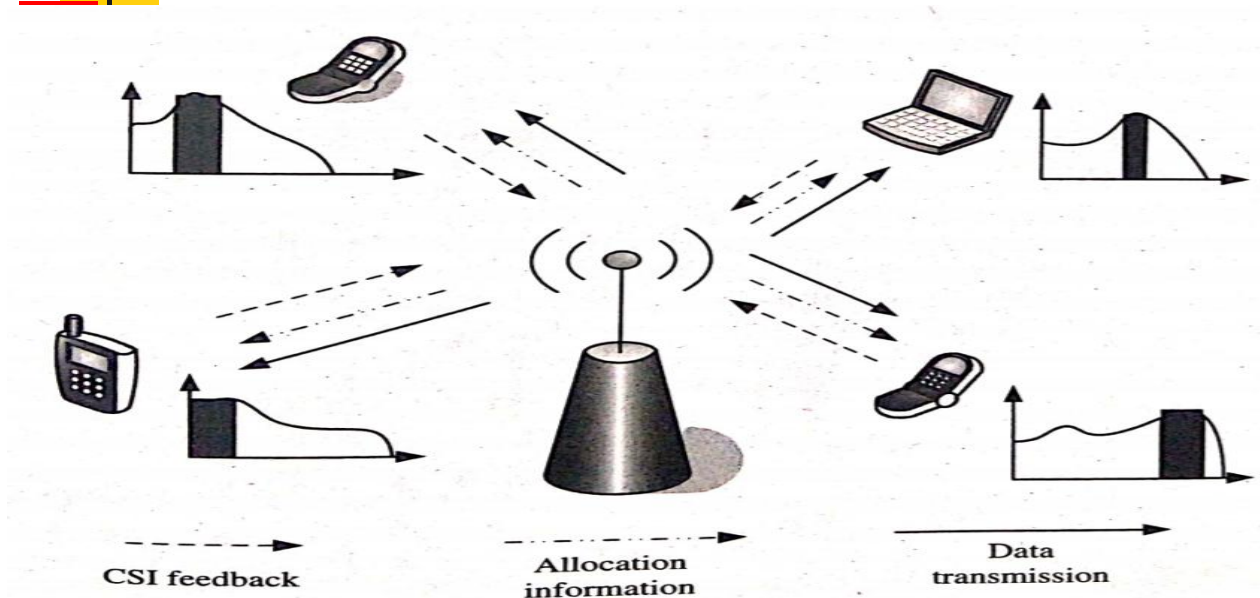


## OFDMA : How it works

- Base station is transmitting a **band AMC type OFDMA** signal to 4 different devices simultaneously.
- 3 arrows of each user – **signaling** that must happen for band AMC to work.
- 1<sup>st</sup> the MS measures and **feedback their channel quality** – **CSI channel state information (SINR)** to the BS.
- **BS then allocates subcarriers** to the 4 users and send this **subcarrier allocation information** to the 4 users in a **overhead message**.
- Finally actual data is transmitted over the subcarriers assigned to each users.



## OFDMA : How it works



5. Show that the received SNR increase linearly with the number of receiver antennas in the concept of Spatial Diversity. – 10 Marks

5. Show that the received SNR increase linearly with the number of receiver antennas in the concept of Spatial Diversity.



- Spatial diversity is achieved by 2 or more antennas, separated by some distance. No additional BW or power is needed.
- **Array Gain** - combination of energy of each antenna. For  $N_t \times N_r$  system, where  $N_t$  &  $N_r$  are Tx & Rx array gain.
- Each antenna  $i$  receives a signal characterized by:  
 $y_i = h_i x + n_i = h x + n_i$ , SNR on single antenna  $\gamma_i = \frac{|h|^2}{\sigma^2}$
- $h_i = h$  for all the correlated antennas,  $\sigma^2 =$  noise power
- Resulting signal after adding all the received paths  

$$y = \sum_{i=1}^{N_r} y_i = N_r h x + \sum_{i=1}^{N_r} n_i$$
- Combined SNR  $\gamma_\Sigma = \frac{|N_r h|^2}{N_r \sigma^2} = \frac{N_r |h|^2}{\sigma^2}$  for correlated channels - received SNR increases linearly with no. of Rx antenna – no diversity gain.

5. Show that the received SNR increase linearly with the number of receiver antennas in the concept of Spatial Diversity.



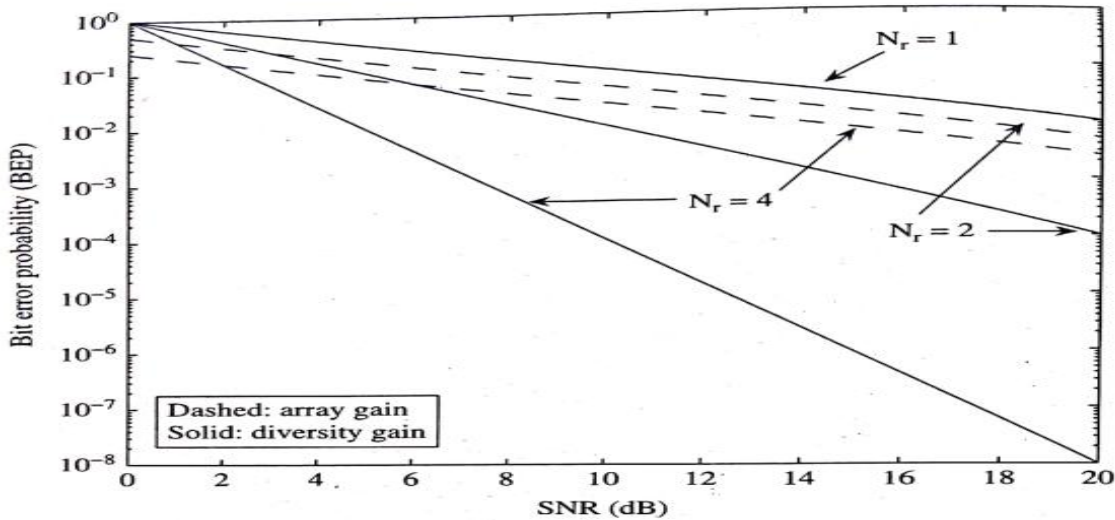
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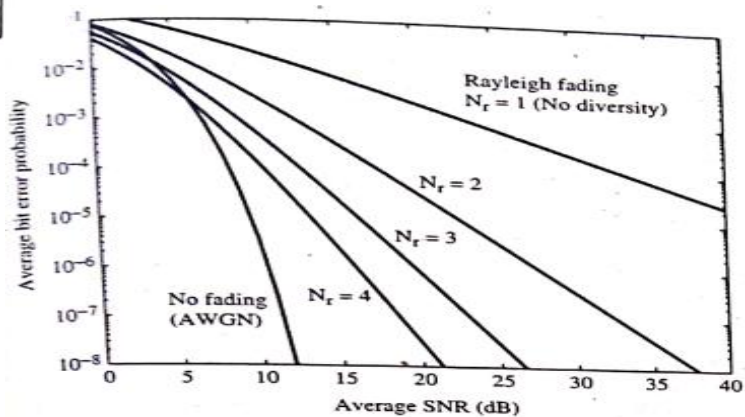
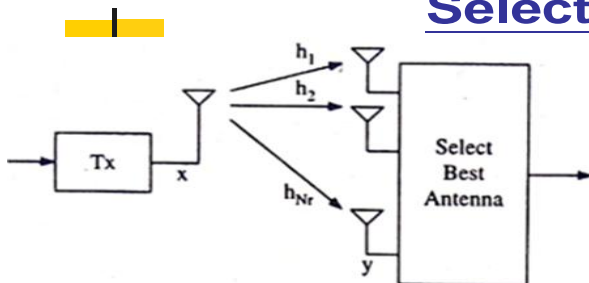
## Relative BEP for $N_t=1$ , $N_r=1, 2, 4$

- For LOS channel average BEP decreases.  $\bar{P}_b \approx c_5(N_d\gamma)^{-1}$ ,
- Sufficient spacing for the antenna is critical for increasing the system reliability.



6. Distinguish between Selection combining and maximal ratio combining in terms of average received SNR. – 10 Marks

## Selection Combining





## Selection Combining

- Simplest type- ***estimates the instantaneous strengths of each of  $N_r$  streams and selects the highest one.***
- Simple as its reduces hardware and power requirements. Used mostly in narrowband channels.
- SC ignores the useful energy of other streams so it's a suboptimal type.
- Wideband channels have different coherence bands with different SNR and requires all the antennas to be active – mostly used in MRC.
- Diversity gain can be confirmed by **outage probability** – defined as the probability that the **received SNR drops below some required threshold**  $P_{out} = P[\gamma < \bar{\gamma}_0] = p$ .



## Selection Combining

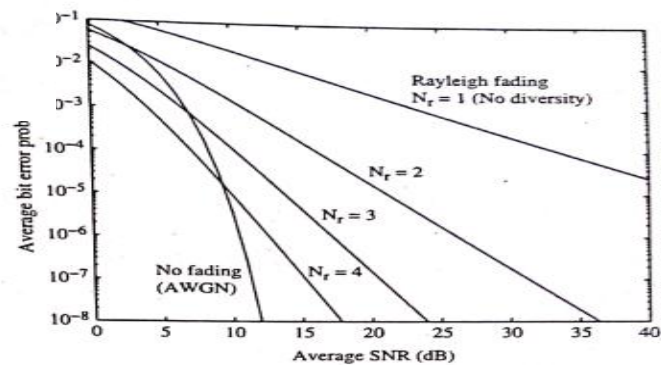
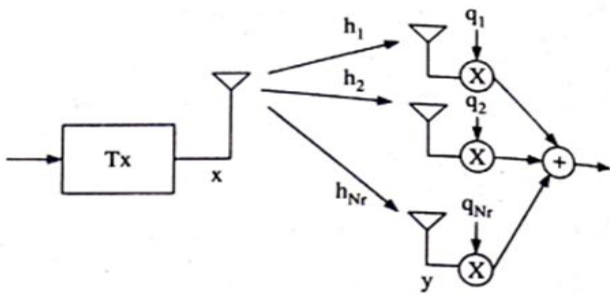
- For  **$N_r$**  uncorrelated received signals

$$\begin{aligned} P_{out} &= P[\gamma_1 < \gamma_0, \gamma_2 < \gamma_0, \dots, \gamma_M < \gamma_0], \\ &= P[\gamma_1 < \gamma_0]P[\gamma_2 < \gamma_0] \dots P[\gamma_M < \gamma_0], \\ &= p^{N_r}. \end{aligned}$$

- For a Rayleigh fading channel  $p = 1 - e^{-\gamma_0/\bar{\gamma}}$ , where  $\bar{\gamma}$  = average received SNR.
- SC decreases the outage probability to  $P_{out} = (1 - e^{-\gamma_0/\bar{\gamma}})^{N_r}$ .
- Average received SNR for  $N_r$ -branch SC can be derived in Rayleigh fading

$$\begin{aligned} \gamma_{sc} &= \bar{\gamma} \sum_{i=1}^{N_r} \frac{1}{i}, \\ &= \bar{\gamma} \left( 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{N_r} \right). \end{aligned}$$

## Maximal Ratio combining - MRC



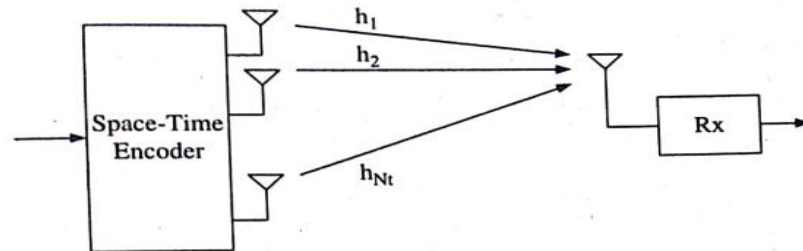
## Maximal Ratio combining - MRC

- MRC combines the information from all the received branches to maximize SNR.
  - MRC works by weighing each branch by a complex factor**  $q_i = |q_i|e^{j\phi_i}$ ; and then **adding up the branches**.
  - Received signal on each branch can be written as  $\mathbf{x}(t)h_i$  assuming flat fading with a complex value of  $h_i = |h_i|e^{j\theta_i}$  on the  $i$ th branch.
  - Combined signal is  $y(t) = x(t) \sum_{i=1}^{N_r} |q_i||h_i| \exp\{j(\phi_i + \theta_i)\}$ .
  - SNR of  $\mathbf{y}(t)$  is  $\mathcal{E}_x =$  transmit signal energy
- $$\gamma_{\text{mrc}} = \frac{\mathcal{E}_x (\sum_{i=1}^{N_r} |q_i||h_i|)^2}{\sigma^2 \sum_{i=1}^{N_r} |q_i|^2}$$
- Branches with higher SNR are enhanced and branches with lower SNR are given less weight.



## Transmit Diversity

- Transmit diversity is more useful in downlink as BS can accommodate more antennas than MS.
- Multiple antenna transmit schemes:
- Open-loop** – systems that don't require the knowledge of the channel at the TX.
- Closed-loop** – systems that require the channel knowledge at the Tx through a feedback channel from the Rx.
- Open-loop transmit diversity is shown – no feedback.



## Open-loop Transmit Diversity: 2x1 Space-Frequency Block Coding

- Most popular open-loop transmit diversity scheme is space-time coding – a code known to the Rx is also applied to the Tx.
- 1990 – space-time block code (STBC) also called Alamouti code / orthogonal space-time block code.
- $s_1$  transmitted by Tx1 and  $s_2$  transmitted by Tx2 over subcarriers  $f_1$  &  $f_2$ .

		Antenna	
		1	2
Subcarrier	$f_1$	$s_1$	$s_2$
	$f_2$	$-s_2^*$	$s_1^*$

- 2x1 Alamouti code is a rate 1 code as there is no increase/decrease in data rates.
- $h_1(f_1)$  &  $h_2(f_2)$  are the complex channel gains of Tx antenna 1 & 2 to the Rx antenna
- Assuming constant channels  $h_1(f_1) = h_2(f_2) = h_1$ .



## Open-loop Transmit Diversity: 2x1 Space-Frequency Block Coding



- Received signal  $r(f)$  is
 
$$\begin{aligned} r(f_1) &= h_1 s_1 + h_2 s_2 + n(f_1), \\ r(f_2) &= -h_1 s_2^* + h_2 s_1^* + n(f_2), \end{aligned}$$
- Assuming channel is known to Rx
 
$$\begin{aligned} y_1 &= h_1^* r(f_1) + h_2 r^*(f_2), \\ y_2 &= h_2^* r(f_1) - h_1 r^*(f_2). \end{aligned}$$

$$\begin{aligned} y_1 &= h_1^* (h_1 s_1 + h_2 s_2 + n(f_1)) + h_2 (-h_1^* s_2 + h_2^* s_1 + n^*(f_2)), \\ &= (|h_1|^2 + |h_2|^2) s_1 + h_1^* n(f_1) + h_2 n^*(f_2), \\ y_2 &= (|h_1|^2 + |h_2|^2) s_2 + h_2^* n(f_1) - h_1 n^*(f_2). \end{aligned}$$
- Resulting SNR
- Each TX antenna halves its Tx Power as total TX power per data symbol is  $\epsilon x$ .
 
$$\begin{aligned} \gamma_{\Sigma} &= \frac{(|h_1|^2 + |h_2|^2)^2 \frac{\epsilon x}{2}}{|h_1|^2 \sigma^2 + |h_2|^2 \sigma^2}, \\ &= \frac{(|h_1|^2 + |h_2|^2) \frac{\epsilon x}{2}}{\sigma^2}, \\ &= \frac{\sum_{i=1}^2 |h_i|^2 \frac{\epsilon x}{2}}{\sigma^2}. \end{aligned}$$
- **2x1 Alamouti code gives same Diversity as 1x2 with MRC**

## Open-loop Transmit Diversity with more Antennas



- **2x2 SFBC** – represented as 2x2 matrix  $\mathbf{H} = \begin{bmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{bmatrix}$ .
- Resulting signals at
- subcarriers  $f_1$  &  $f_2$ 

$$\begin{aligned} r_1(f_1) &= h_{11} s_1 + h_{21} s_2 + n_1(f_1), \\ r_1(f_2) &= -h_{11} s_2^* + h_{21} s_1^* + n_1(f_2), \\ r_2(f_1) &= h_{12} s_1 + h_{22} s_2 + n_2(f_1), \\ r_2(f_2) &= -h_{12} s_2^* + h_{22} s_1^* + n_2(f_2). \end{aligned}$$
- on antenna 1 & 2
- Using the following combining scheme
 
$$\begin{aligned} y_1 &= h_{11}^* r_1(f_1) + h_{21} r_1^*(f_2) + h_{12}^* r_2(f_1) + h_{22} r_2^*(f_2), \\ y_2 &= h_{21}^* r_1(f_1) - h_{11} r_1^*(f_2) + h_{22}^* r_2(f_1) - h_{12} r_2^*(f_2) \end{aligned}$$
- Giving the following decision :
 
$$\begin{aligned} y_1 &= (|h_{11}|^2 + |h_{12}|^2 + |h_{21}|^2 + |h_{22}|^2) s_1 + 4 \text{ noise terms}, \\ y_2 &= (|h_{11}|^2 + |h_{12}|^2 + |h_{21}|^2 + |h_{22}|^2) s_2 + 4 \text{ noise terms}, \end{aligned}$$

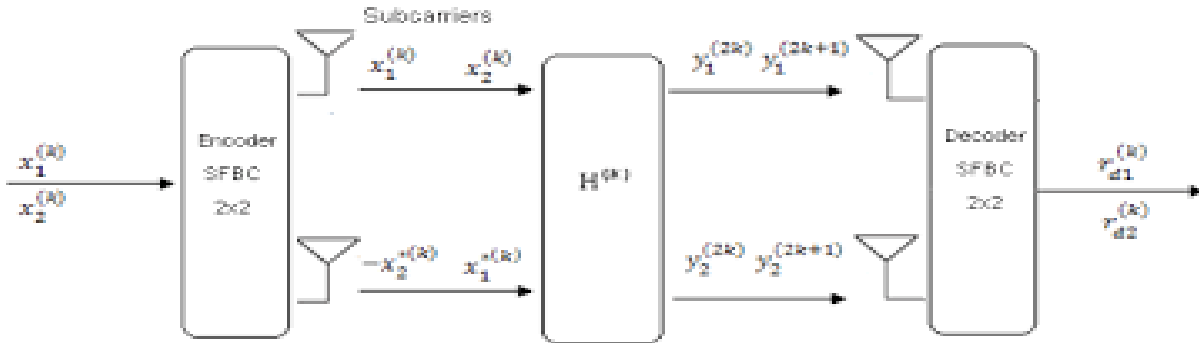
## Open-loop Transmit Diversity with more Antennas



- Resulting SNR

$$\gamma_{\Sigma} = \frac{\left( \sum_j \sum_i |h_{ij}|^2 \right)^2}{\sigma^2 \sum_j \sum_i |h_{ij}|^2} \frac{\mathcal{E}_x}{2} = \frac{\sum_{j=1}^2 \sum_{i=1}^2 |h_{ij}|^2}{\sigma^2} \frac{\mathcal{E}_x}{2}$$

- 2x2 Alamouti achieves full diversity gain.



## Open-loop Transmit Diversity with more Antennas



- 4x2 Stacked STBC** – LTE will have 4 TX antenna. 2 data streams are sent using double space-time transmit diversity scheme (DSTTD)
- Similar to operating two 2x1 Alamouti code systems in parallel.
- Received signals at subcarrier  $f_1$  &  $f_2$  on antenna 1 & 2 are represented with equivalent channel models:

$$\begin{bmatrix} r_1(f_1) \\ r_1^*(f_2) \\ r_2(f_1) \\ r_2^*(f_2) \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} & h_{14} \\ h_{12}^* & -h_{11}^* & h_{14}^* & -h_{13}^* \\ h_{21} & h_{22} & h_{23} & h_{24} \\ h_{22}^* & -h_{21}^* & h_{24}^* & -h_{23}^* \end{bmatrix} \begin{bmatrix} s_1 \\ s_2 \\ s_3 \\ s_4 \end{bmatrix} + \begin{bmatrix} n_1(f_1) \\ n_1^*(f_2) \\ n_2(f_1) \\ n_2^*(f_2) \end{bmatrix}$$

- Equivalent matrix channel model of DSTTD

$$\begin{bmatrix} \mathbf{r}_1 \\ \mathbf{r}_2 \end{bmatrix} = \begin{bmatrix} \mathbf{H}_{11} & \mathbf{H}_{12} \\ \mathbf{H}_{21} & \mathbf{H}_{22} \end{bmatrix} \begin{bmatrix} \mathbf{s}_1 \\ \mathbf{s}_2 \end{bmatrix} + \begin{bmatrix} \mathbf{n}_1 \\ \mathbf{n}_2 \end{bmatrix}$$

## Open-loop Transmit Diversity with more Antennas



- Using linear combining scheme for decision :

$$\begin{aligned}
 y_1 &= (|h_{11}|^2 + |h_{12}|^2 + |h_{21}|^2 + |h_{22}|^2)s_1 + I_3 + I_4 + 4 \text{ noise terms,} \\
 y_2 &= (|h_{11}|^2 + |h_{12}|^2 + |h_{21}|^2 + |h_{22}|^2)s_2 + I_3 + I_4 + 4 \text{ noise terms,} \\
 y_3 &= (|h_{13}|^2 + |h_{14}|^2 + |h_{23}|^2 + |h_{24}|^2)s_3 + I_1 + I_2 + 4 \text{ noise terms,} \\
 y_4 &= (|h_{13}|^2 + |h_{14}|^2 + |h_{23}|^2 + |h_{24}|^2)s_4 + I_1 + I_2 + 4 \text{ noise terms,}
 \end{aligned}$$

- $I_i$  is the interference from the  $i$ th Tx antenna due to transmitting 2 simultaneous data streams.

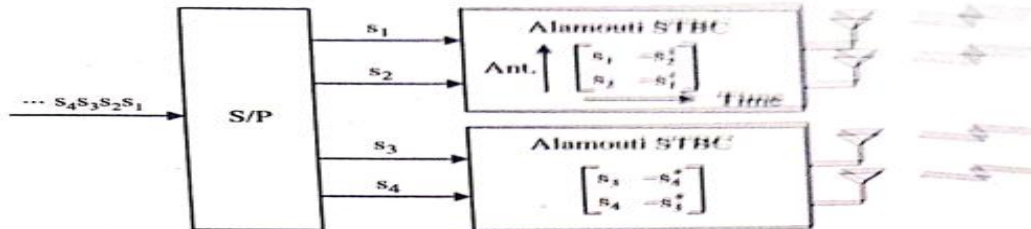


Figure 5.5  $4 \times 2$  stacked STBC transmitter.

## Open-loop Transmit Diversity with more Antennas



- 4x2 in LTE** – a combination of SFBC and frequency switched transmit diversity FSTD is used. Rate 1 encoder.
- This combination is a rate 1 diversity scheme – 2 modulation symbols are sent over 4 OFDM symbols, using the following space-time encoder.
- Rows are Tx antennas and columns are subcarrier index.
- 1<sup>st</sup> & 2<sup>nd</sup> symbols  $s_1$  &  $s_2$  are sent over antenna ports 0 & 2 on the first 2 OFDM subcarriers in the block.
- On the other 2 subcarriers 3<sup>rd</sup> & 4<sup>th</sup> symbols are sent using antenna port 1 & 3.

$$\frac{1}{\sqrt{2}} \begin{bmatrix} s_1 & s_2 & 0 & 0 \\ 0 & 0 & s_3 & s_4 \\ -s_2^* & s_1^* & 0 & 0 \\ 0 & 0 & -s_4^* & s_3^* \end{bmatrix}$$