

be many neurons involved in a sequence depending upon the complexity of the predictive action. The layers of PEs could work in sequence, or they could work in parallel.

3. The processing logic of each neuron may assign different weights to the various incoming input streams. The processing logic may also use nonlinear transformation, such as a sigmoid function, from the processed values to the output value. This processing logic and the intermediate weight and processing functions are just what works for the system as a whole, in its objective of solving a problem collectively. Thus, neural net works are considered to be an opaque and a black-box system.

4. The neural network can be trained by making similar decisions over and over again with many training cases. It will continue to learn by adjusting its internal computation and communication based on feedback about its previous decisions. Thus, the neural networks become better at making a decision as they handle more and more decisions. Depending upon the nature of the problem and the availability of good training data, at some point the neural network will learn enough and begin to match the predictive accuracy of a human expert. In many practical situations, the predictions of ANN, trained over a long period of time with a large number of training data, have begun to decisively become more accurate than human experts. At that point ANN can begin to be seriously considered for deployment in real situations in real time.

Representation of a Neural Network

A neural network is a series of neurons that receive inputs from other neurons. They do a weighted summation function of all the inputs, using different weights (or importance) for each input. The weighted sum is then transformed into an output value using a transfer function.

Learning in ANN occurs when the various processing elements in the neural network adjust the underlying relationship (weights, transfer function, etc)between input and outputs, in response to the feedback on their predictions. If the prediction made was correct, then the weights would remain the same, but if the prediction was incorrect, then the parameter values would change. The Transformation (Transfer) Function is any function suitable for the task at hand.

The transfer function for ANNs is usually a non-linear sigmoid function. Thus, if the normalized computed value is less than some value (say0.5) then the output value will be zero. If the computed value is at the cut-off threshold, then the output value will be a 1. It could be a nonlinear hyperbolic function in which the output is either a -1 or a 1. Many other functions could be designed for any or all of the processing elements.

Thus, in a neural network, every processing element can potentially have a different number of input values, a different set of weights for those inputs, and a different transformation function. Those values support and compensate for one another until the neural network as a whole learns to provide the correct output, as desired by the user.

4 Create a decision tree for the following data set.

Solution:

The first thing we need to do is work out which attribute will be put into the node at the top of our tree: either weather, parents or money. To do this, we need to calculate:

 $Entropy(S) = -p_{\text{cinema}} \log_2(p_{\text{cinema}}) - p_{\text{tennis}} \log_2(p_{\text{tennis}}) - p_{\text{shopping}} \log_2(p_{\text{shopping}}) - p_{\text{stay_in}} \log_2(p_{\text{stay_in}})$ $= -(6/10) * log₂(6/10) - (2/10) * log₂(2/10) - (1/10) * log₂(1/10) - (1/10) *$ $log_2(1/10)$ $= -(6/10) * -0.737 - (2/10) * -2.322 - (1/10) * -3.322 - (1/10) * -3.322$

 $= 0.4422 + 0.4644 + 0.3322 + 0.3322 = 1.571$

and we need to determine the best of:

Gain(S, weather) = 1.571 - $(|S_{sun}|/10)^*$ Entropy(S_{sun}) - $(|S_{wind}|/10)^*$ Entropy(S_{wind}) - $(|S_{\text{rain}}|/10)^*$ Entropy (S_{rain}) $= 1.571 - (0.3)$ *Entropy(S_{sun}) - (0.4)*Entropy(S_{wind}) - (0.3)*Entropy(S_{rain}) $= 1.571 - (0.3)*(0.918) - (0.4)*(0.81125) - (0.3)*(0.918) = 0.70$

Gain(S, parents) = 1.571 - ($|S_{\text{ves}}|/10$)*Entropy(S_{ves}) - ($|S_{\text{no}}|/10$)*Entropy(S_{no}) $= 1.571 - (0.5) * 0 - (0.5) * 1.922 = 1.571 - 0.961 = 0.61$

Gain(S, money) = 1.571 - $(|S_{rich}|/10)^*$ Entropy(S_{rich}) - $(|S_{poor}|/10)^*$ Entropy(S_{poor}) $= 1.571 - (0.7) * (1.842) - (0.3) * 0 = 1.571 - 1.2894 = 0.2816$

This means that the first node in the decision tree will be the weather attribute. As an exercise, convince yourself why this scored (slightly) higher than the parents attribute remember what entropy means and look at the way information gain is calculated.

From the weather node, we draw a branch for the values that weather can take: sunny, windy

 $CO5$ L₃

and rainy:

Now we look at the first branch. $S_{\text{sumny}} = \{W1, W2, W10\}$. This is not empty, so we do not put a default categorization leaf node here. The categorizations of W1, W2 and W10 are Cinema, Tennis and Tennis respectively. As these are not all the same, we cannot put a categorization leaf node here. Hence we put an attribute node here, which we will leave blank for the time being.

Looking at the second branch, $S_{windy} = \{W3, W7, W8, W9\}$. Again, this is not empty, and they do not all belong to the same class, so we put an attribute node here, left blank for now. The same situation happens with the third branch, hence our amended tree looks like this:

Now we have to fill in the choice of attribute A, which we know cannot be weather, because we've already removed that from the list of attributes to use. So, we need to calculate the values for Gain(S_{sumy} , parents) and Gain(S_{sumy} , money). Firstly, Entropy(S_{sumy}) = 0.918. Next, we set S to be $S_{\text{sumny}} = \{W1, W2, W10\}$ (and, for this part of the branch, we will ignore all the other examples). In effect, we are interested only in this part of the table:

Hence we can calculate:

Gain(S_{sunny}, parents) = 0.918 - ($|S_{yes}|/|S|$)*Entropy(S_{yes}) - ($|S_{no}|/|S|$)*Entropy(S_{no}) $= 0.918 - (1/3)*0 - (2/3)*0 = 0.918$

 $Gain(S_{\text{sunny}}, \text{money}) = 0.918 - (|S_{\text{rich}}|/|S|)^* \text{Entropy}(S_{\text{rich}}) - (|S_{\text{poor}}|/|S|)^* \text{Entropy}(S_{\text{poor}})$ $= 0.918 - (3/3)*0.918 - (0/3)*0 = 0.918 - 0.918 = 0$

Notice that Entropy(S_{ves}) and Entropy(S_{no}) were both zero, because S_{ves} contains examples which are all in the same category (cinema), and S_{no} similarly contains examples which are all in the same category (tennis). This should make it more obvious why we use information gain to choose attributes to put in nodes.

Given our calculations, attribute A should be taken as parents. The two values from parents are yes and no, and we will draw a branch from the node for each of these. Remembering that we replaced the set S by the set S_{Sunny} , looking at S_{yes} , we see that the only example of this is W1. Hence, the branch for yes stops at a categorisation leaf, with the category being

1. Decision Trees: They help classify populations into classes. It is said that 70%of all data mining work is about classification solutions; and that 70% of all classification work uses decision trees. Thus, decision trees are the most popular and important data mining technique. There are many popular algorithms to make decision trees. They differ in terms of their mechanisms and each technique work well for different situations. It is possible to try multiple decision-tree algorithms on a data set and compare the predictive accuracy of each tree.

*2. Regression***:** This is a well-understood technique from the field of statistics. The goal is to find a best fitting curve through the many data points. The best fitting curve is that which minimizes the (error) distance between the actual data points and the values predicted by the curve. Regression models can be projected into the future for prediction and forecasting purposes.

3. *Artificial Neural Networks***:** Originating in the field of artificial intelligence and machine learning, ANNs are multi-layer non-linear information processing models that learn from past data and predict future values. These models predict well, leading to their popularity. The model's parameters may not be very intuitive. Thus, neural networks are opaque like a black-box. These systems also require a large amount of past data to adequate train the system.

*4. Cluster analysis***:** This is an important data mining technique for dividing and conquering large data sets. The data set is divided into a certain number of clusters, by discerning similarities and dissimilarities within the data. There is no one right answer for the number of clusters in the data. The user needs to make a decision by looking at how well the number of clusters chosen fit the data. This is most commonly used for market segmentation. Unlike decision trees and regression, there is no one right answer for cluster analysis.

*5. Association Rule Mining***:** Also called Market Basket Analysis when used in retail industry, these techniques look for associations between data values. An analysis of items frequently found together in a market basket can help cross-sell products, and also create product bundles.

6 Consider the following dataset.

[10] CO5 L3

a) What linear regression equation best predicts statistics performance, based on math aptitude scores?

b) If a student made an 80 on the aptitude test, what grade would we expect her to make in statistics?

c) How well does the regression equation fit the data?

Solution:

In the table below, the x_i column shows scores on the aptitude test. Similarly, the yi column shows statistics grades. The last two columns show deviations scores - the difference between the student's score and the average score on each test. The last two rows show sums and mean scores that we will use to conduct the regression analysis.

And for each student, we also need to compute the squares of the deviation scores (the last two columns in the table below).

And finally, for each student, we need to compute the product of the deviation scores.

The regression equation is a linear equation of the form: $\hat{y} = b_0 + b_1x$. To conduct a regression analysis, we need to solve for b_0 and b_1 . Computations are shown below. Notice that all of our inputs for the regression analysis come from the above three tables.

First, we solve for the regression coefficient (b_1) :

$$
b_1 = \sum [(x_i - x)(y_i - y)] / \sum [(x_i - x)^2]
$$

$$
b_1 = 470/730
$$

$$
b_1 = 0.644
$$

Once we know the value of the regression coefficient (b_1) , we can solve for the regression slope (b_0) :

> $b_0 = y - b_1 * x$ $b_0 = 77 - (0.644)(78)$ $b_0 = 26.768$

Therefore, the regression equation is: $\hat{y} = 26.768 + 0.644x$.

b) In our example, the independent variable is the student's score on the aptitude test. The dependent variable is the student's statistics grade. If a student made an 80 on the aptitude test, the estimated statistics grade (\hat{y}) would be:

$$
\hat{y} = b_0 + b_1 x
$$

$$
\hat{y} = 26.768 + 0.644x = 26.768 + 0.644 * 80
$$

$$
\hat{y} = 26.768 + 51.52 = 78.288
$$

c) Whenever you use a regression equation, you should ask how well the equation fits the data. One way to assess fit is to check the coefficient of determination, which can be computed from the following formula.

$$
R^2 \!= \! \left\{\,(\;1\;/\;N\;)\;*\;\!\Sigma\;[\;(x_i \mathsf{\textcolor{red}{\cdot}}\;x)\;*\; (y_i \mathsf{\textcolor{red}{\cdot}}\;y)\;]\,/\,(\sigma_x \;*\; \sigma_y\;)\;\right\}^2
$$

where N is the number of observations used to fit the model, Σ is the summation symbol, x_i is the x value for observation i, x is the mean x value, y_i is the y value for observation i, y is the mean y value, σ_x is the standard deviation of x, and σ_y is the standard deviation of y.

Computations for the sample problem of this lesson are shown below. We begin by computing the standard deviation of x (σ_x) :

$$
\sigma_{\rm x} = \text{sqrt} \left[\sum (x_{\rm i} - x)^2 / N \right]
$$

 $\sigma_x =$ sqrt(730/5) = sqrt(146) = 12.083

Next, we find the standard deviation of y, (σ_v) :

$$
\sigma_{y} = \text{sqrt} [\Sigma (y_i - y)^2 / N]
$$

$$
\sigma_y
$$
 = sqrt(630/5) = sqrt(126) = 11.225

And finally, we compute the coefficient of determination (R^2) :

$$
R^{2} = \{ (1/N)^{*} \Sigma [(x_{i} - x) * (y_{i} - y)] / (\sigma_{x} * \sigma_{y}) \}^{2}
$$

$$
R^2 = [(1/5) * 470 / (12.083 * 11.225)]^2
$$

DEPARTMENT OF INFORMATION SCIENCE & ENGINEERING

Date:

Sem & Sec : 8^{th} A,B

CO's to PO's & PSO's mapping

Name of the course : Big Data Analytics Sub Code : 15CS82 Name of the Faculty/s : Mrs. Vaishali M Deshmukh Sem& Sec : 8

