

Internal Assessment Test - II

Sub:	POWER SYSTEM OPERATION AND CONTROL						Code:	15EE81	
Date:	16/04/2019	Duration:	90 mins	Max Marks:	50	Sem:	8th	Branch:	EEE

1. With a block diagram representation, explain tie-line bias control of a two area load frequency control.

TIE-LINE BIAS CONTROL FOR TWO-AREA SYSTEM:-

* Since the steady state change in frequency $\Delta f_{ss} \neq 0$, for two-area system, the control adopted should be modified.

* The modified control is called as TIE-LINE BIAS CONTROL.

* The required change in generation (called ACE) represents the shift in area's generation required to restore frequency and net tie-line power. i.e. Δf_{ss} and $\Delta P_{T,ss}$ must be zero.

Δf	ΔP_{12}	LOAD CHANGE	REQUIRED CONTROL ACTION
↓	↓	$\Delta P_{D1} = \uparrow$ $\Delta P_{D2} = 0$	Increase Generation in AREA-1
↓	↑	$\Delta P_{D1} = 0$ $\Delta P_{D2} = \uparrow$	Increase Generation in AREA-2
↑	↓	$\Delta P_{D1} = 0$ $\Delta P_{D2} = \downarrow$	Decrease Generation in AREA-2
↑	↑	$\Delta P_{D1} = \downarrow$ $\Delta P_{D2} = 0$	Decrease Generation in AREA-1

↑ - INCREASE || ↓ - DECREASE

Define Area Control Error of AREA 1;

$$ACE_1 = \Delta P_{12} + B_1 \Delta f_1$$

Area Control Error of AREA 2;

$$ACE_2 = \Delta P_{21} + B_2 \Delta f_2 \quad [\because \Delta P_{21} = a_{12} \Delta P_{12}]$$

$$ACE_2 = a_{12} \Delta P_{12} + B_2 \Delta f_2$$

For steady state change in frequency and steady state change in tie-line power to be zero

$$\text{i.e. } \Delta f_{ss} = 0 \text{ and } \Delta P_{12,ss} = 0$$

The speed changer setting of two areas should be:

$$\begin{aligned} \Delta P_{C1} &= -K_{i1} \int ACE_1 \cdot dt \\ &= -K_{i1} \int (\Delta P_{12} + B_1 \Delta f_1) \cdot dt \end{aligned}$$

Taking Laplace Transform;

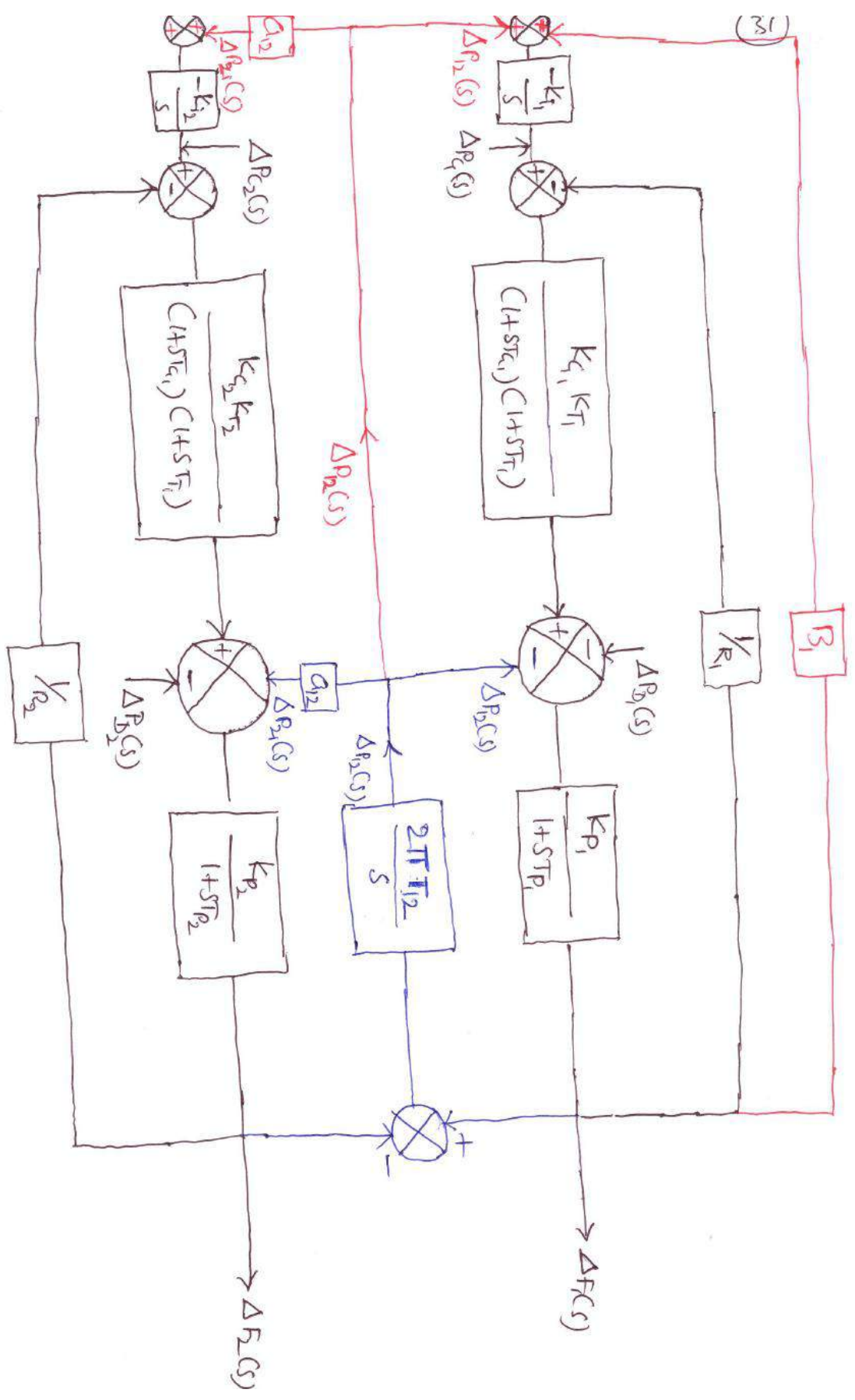
$$\Delta P_{C1}(s) = -\frac{K_{i1}}{s} [\Delta P_{12}(s) + B_1 \Delta F_1(s)] \quad \text{--- (7)}$$

Similarly $\Delta P_{C2}(s) = -K_{i2} \int ACE_2 \cdot dt$

$$= -K_{i2} \int (a_{12} \Delta P_{12} + B_2 \Delta f_2) \cdot dt$$

Taking Laplace Transform;

$$\Delta P_{C2}(s) = -\frac{K_{i2}}{s} [a_{12} \Delta P_{12}(s) + B_2 \Delta F_2(s)] \quad \text{--- (8)}$$



TIE-LINE BIAS CONTROL FOR TWO-AREA SYSTEM

STEADY STATE ANALYSIS (STATIC PERFORMANCE)

OF TIE-LINE BIAS CONTROL FOR TWO-AREA SYSTEM:—

If $B_1 = D_1 + \frac{1}{R_1}$ and $B_2 = D_2 + \frac{1}{R_2}$, from the steady

state analysis of two-area system, we know that;

$$\Delta f_{SS} = \frac{X_2 - a_{12}X_1}{a_{12}B_1 - B_2} \quad \text{and} \quad \Delta P_{12SS} = \frac{B_1X_2 - B_2X_1}{B_2 - a_{12}B_1}$$

Then Area Control Error of AREA1 @ steady state:

$$\begin{aligned} ACE_{1SS} &= \Delta P_{12SS} + B_1 \Delta f_{SS} \\ &= \left[\frac{B_1X_2 - B_2X_1}{B_2 - a_{12}B_1} \right] + B_1 \left[\frac{X_2 - a_{12}X_1}{a_{12}B_1 - B_2} \right] \\ &= -X_1 \end{aligned}$$

Since $\Delta P_{D_1} = X_1$, $ACE_{1SS} = -X_1$

Similarly $ACE_{2SS} = a_{12} \Delta P_{12SS} + B_2 \Delta f_{SS}$

$$\begin{aligned} &= a_{12} \left[\frac{B_1X_2 - B_2X_1}{B_2 - a_{12}B_1} \right] + B_2 \left[\frac{X_2 - a_{12}X_1}{a_{12}B_1 - B_2} \right] \\ &= -X_2 \end{aligned}$$

Since $\Delta P_{D_2} = X_2$, $ACE_{2SS} = -X_2$

\therefore Bias factors are adjusted such that change

in load of a particular area should be met by its area.

2. Explain with block diagram modelling of Generator and Load.

GENERATOR-LOAD MODEL :

for incremental change in load demand (ΔP_D), there's going to be change in system frequency (Δf). To get the system frequency back to base frequency ($f^0 = 50\text{Hz}$), there should be change in generation (ΔP_G)

Define; $\Delta P_G - \Delta P_D =$ the net surplus power (MW) in the system
This surplus power is absorbed in the system in two ways :

1. The surplus power is stored in the rotor in the form of kinetic energy (K.E.) i.e. $\frac{dW}{dt}$

Let, $W^0 =$ kinetic energy in the rotor prior to load change.

$W =$ kinetic energy in the rotor post load change.

$f^0 =$ system base frequency.

$f^0 + \Delta f =$ system frequency post load change.

Since the K.E. is proportional to the square of the speed of the generator, we can write

$$W^0 \propto (f^0)^2 \quad \text{--- (1)}$$

$$W \propto (f^0 + \Delta f)^2 \quad \text{--- (2)}$$

$$\frac{(2)}{(1)} \Rightarrow \frac{W}{W^0} = \left[\frac{f^0 + \Delta f}{f^0} \right]^2 = \left[1 + \frac{\Delta f}{f^0} \right]^2 = 1 + \frac{2\Delta f}{f^0}$$

$\therefore \frac{\Delta f}{f^0}$ is small, (17)
ignoring $(\frac{\Delta f}{f^0})^2$

$$\therefore \frac{dW}{dt} = \frac{2W^0}{f^0} \cdot \frac{d}{dt} (\Delta f) \quad \text{--- (3)}$$

2. The load on the system being mostly motor load, the rate of change of load with respect to frequency can be considered as constant i.e.

\rightarrow Damping coefficient

$$D = \frac{\partial P_D}{\partial f} \quad \text{--- (4)}$$

\rightarrow Power system parameter.

The net power surplus at the bus bar is given by

$$\Delta P_G - \Delta P_D = \frac{2W^0}{f^0} \cdot \frac{d}{dt}(\Delta f) + D \cdot \Delta f \quad [\text{from } (3), (4)]$$

If H is the inertia constant of the generator in MW-sec/MVA and P is the rating in MVA, then $W^0 = HP$

$$\Delta P_G - \Delta P_D = \frac{2HP}{f^0} \cdot \frac{d}{dt}(\Delta f) + D \cdot \Delta f$$

Dividing throughout by P we get

$$\begin{aligned} \Delta P_G(\text{p.u.}) - \Delta P_D(\text{p.u.}) &= \frac{2H}{f^0} s \Delta F(s) + D \Delta F(s) \quad [D \rightarrow D(\text{p.u.})] \\ &= \Delta F(s) \left[\frac{2H}{f^0} s + D \right] \end{aligned}$$

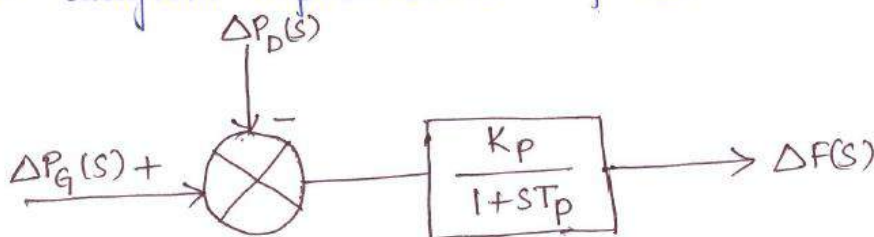
$$\text{or } \Delta F(s) = \frac{\Delta P_G(s) - \Delta P_D(s)}{\left[\frac{2H}{f^0} s + D \right]}$$

$$\frac{\Delta F(s)}{\Delta P_G(s) - \Delta P_D(s)} = \frac{1}{\left[\frac{2H}{f^0} s + D \right]} = \frac{1/D}{\left[1 + \frac{2H}{f^0 D} \cdot s \right]} = \frac{K_p}{1 + sT_p} \quad (5)$$

Where $K_p = \frac{1}{D} = \text{power system gain.}$

$T_p = \frac{2H}{Df^0} = \text{power system time constant.}$

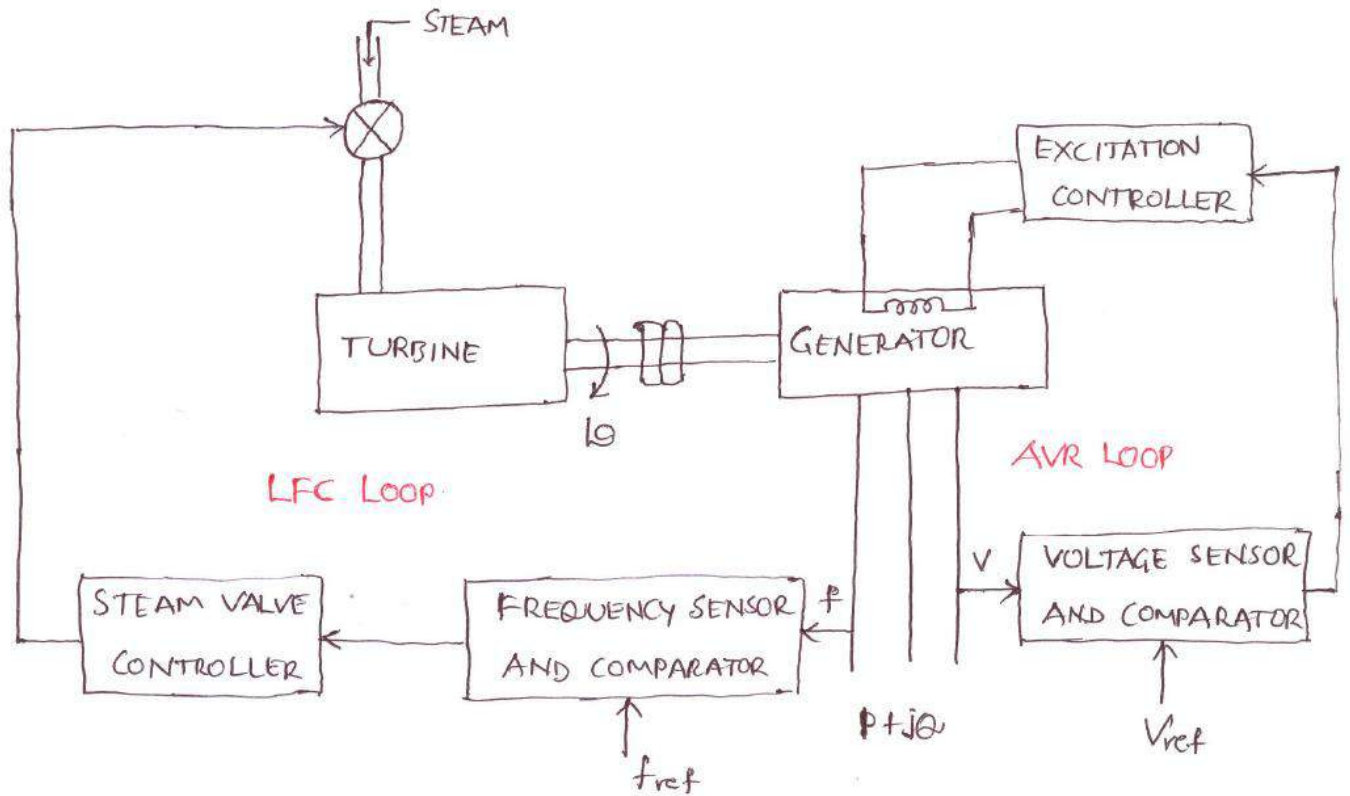
Block diagram representation of (5)



GENERATOR LOAD MODEL.

3a. Explain basic generator control loops and cross-coupling between control loops.

BASIC GENERATOR CONTROL LOOPS:



SCHEMATIC DIAGRAM OF LOAD FREQUENCY AND EXCITATION

VOLTAGE REGULATOR OF A TURBO-GENERATOR

The two control loops are:

The two control loops are:

— Control of turbine input also called as:

→ Load Frequency Control (LFC)

→ Automatic Generation Control (AGC)

→ Automatic Load Frequency Control (ALFC)

→ MW-f control loop

→ Power-frequency control loop

— Excitation control (or) MVAR-Voltage (Q-V) Control

(2)

CROSS-COUPLING BETWEEN CONTROL LOOPS:

- * Active power change is dependent on internal machine angle ' δ ' and is independent of bus voltage. Change in angle ' δ ' is caused by momentary change in generator speed.
- * While bus voltage is dependent on machine excitation and therefore on reactive power generation and is independent of machine angle ' δ '.
- * Therefore, load frequency and excitation voltage controls are non-interactive and can be modelled, analysed independently.
- * Excitation voltage control is fast acting in which the major time constant is that of generator field.
- * Power-frequency control is slow acting with major time constant contributed by the turbine and generator moment of inertia. This time constant is much larger than that of the generator field.
- * Thus the transients in excitation voltage control vanish much faster and do not affect the dynamics of power frequency control.

3b. Mention functions of AGC.

Objectives of AGC:

- * Sustaining frequency as close as possible to the specified range.
- * Maintenance of appropriate level of interchange power.
- * Maintenance of economic unit's generation.

4a. Two machines operate in parallel to supply a load of 400 MW, the capacities of the machines are 200 MW and 500 MW. Each has a droop characteristic of 4%. Their governors are adjusted so that frequency is 100% on Full Load. Calculate the load supplied by each unit and the frequency at this load. The system frequency is 50 Hz.

$$\Delta P_L = 400 \text{ MW} \quad | \quad R_1 = R_2 = 0.04 \quad | \quad P_{1\text{RATE}} = 200 \text{ MW} \quad | \quad P_{2\text{RATE}} = 500 \text{ MW}$$

* @ 100% Load = 200 MW + 500 MW = 700 MW, they are supposed to operate @ 50 Hz.

* But we have connected just $\Delta P_L = 400 \text{ MW}$ across generators. So operating frequency is going to be greater than 50 Hz.

$$\text{System Regulation; } R_{\text{SYS}} = \frac{\Delta f}{\Delta L} = \frac{1}{\frac{P_{1\text{RATE}}}{R_1} + \frac{P_{2\text{RATE}}}{R_2}} = 0.0000571 \text{ Hz/MW}$$

$$\text{Change in frequency } \Delta f = R_{\text{SYS}} * \Delta L = 0.0228 \text{ Hz.}$$

$$\therefore \text{Frequency @ 400 MW load} = f^0 + \Delta f = 50.0228 \text{ Hz.}$$

$$\Delta P_1 = \frac{\Delta f}{R_1} * P_{1\text{RATE}} = 114 \text{ MW}$$

$$\Delta P_2 = \frac{\Delta f}{R_2} * P_{2\text{RATE}} = 285 \text{ MW}$$

$$\text{CHECK } \Delta P_L = \Delta P_1 + \Delta P_2$$

4b. Determine primary ALFC loop parameters for control area having the following data. Total rated capacity, $P_r = 2000$ MW; Inertia Constant, $H = 5.0$ S; Frequency $f_0 = 50$ Hz, Normal Operating Load, $P_D = 1000$ MW.

Assume that the load frequency dependency is linear, meaning that the load would increase 1% for 1% frequency change.

$$\Delta P_D = 1\% \text{ of } 1000 = 10 \text{ MW}$$

$$\Delta f = 1\% \text{ of } 50 = 0.5 \text{ Hz}$$

$$D = \frac{\Delta P_D}{\Delta f} = \frac{10}{0.5} = 20 \text{ MW/Hz} = \frac{20}{2000} = 0.01 \text{ pu MW/Hz}$$

$$K_p = \frac{1}{D} = 100 \text{ Hz/pu MW} \text{ — Power system gain}$$

$$T_p = \frac{2H}{f_0 D} = 20 \text{ Sec.} \text{ — power system time constant}$$

$$G_p(s) = \frac{K_p}{1+sT_p} = \frac{100}{1+20s}$$

↳ Power System Transfer Function

5. A single area consists of two generators as follows:

$G_1 = 200$ MW, $R = 4\%$ (on machine base)

$G_2 = 400$ MW, $R = 5\%$ (on machine base)

They are connected in parallel and share a load of 600 MW in proportion to their rating, at 50 Hz. 200 MW of load is tripped. What is the generation to meet the new load if $D=0$. What is the frequency at new load? Repeat for $D = 1.5$ pu.

Choose a base of 200 MW. $D=0$

$R_1 = 0.04$ pu (on 200 MW base)

$R_2 = 0.05 \times \frac{200}{400} = 0.025$ pu (on 200 MW base)

$$\Delta P_L = -200 \text{ MW (decrease)}$$

$$= -1 \text{ pu}$$

$$\Delta \omega_M = \frac{-\Delta P_L}{\frac{1}{R_1} + \frac{1}{R_2}} = \frac{-(-1)}{\frac{1}{0.04} + \frac{1}{0.025}} = 0.01538 \text{ pu}$$

Frequency at new load = 1.01538 pu
= 50.769 Hz

$$\Delta P_1 = \frac{-\Delta f}{R_1} = \frac{-0.01538}{0.04} = -0.3845 \text{ pu}$$

$$= -0.3845 \times 200$$

$$= -76.9 \text{ MW}$$

$$P_1 = 200 - 76.9 = 123.1 \text{ MW}$$

$$\Delta P_2 = \frac{-\Delta f}{R_2} = \frac{-0.01538}{0.025} = -0.6152 \text{ pu}$$
$$= -123.04 \text{ MW}$$

$$P_2 = 400 - 123.04 = 276.96 \text{ MW}$$

$$P_1 + P_2 = P_L = 400 \text{ MW.}$$

Now $D = 1.5$

$$\Delta \omega_M = \frac{-\Delta P_L}{\frac{1}{R_1} + \frac{1}{R_2} + D} = \frac{1}{\frac{1}{0.04} + \frac{1}{0.025} + 1.5} = 0.01504 \text{ pu}$$

Frequency at new load = 1.01504 pu
= 50.752 Hz

$$\Delta P_1 = \frac{-0.01504}{0.04} \times 200 = -75.2 \text{ MW}$$

$$P_1 = 200 - 75.2 = 124.8 \text{ MW}$$

$$\Delta P_2 = \frac{-0.01504}{0.025} \times 200 = -120.32 \text{ MW}$$

$$P_2 = 279.68 \text{ MW}$$

$\Delta \omega =$ increase in load ^{due to} frequency change

$$\begin{aligned}
 &= 1.5 \times 0.01504 \\
 &= 0.02256 \text{ pu} \\
 &= 0.02256 \times 200 \\
 &= 4.512 \text{ MW}
 \end{aligned}$$

$$\begin{aligned}
 P_1 + P_2 &= 404.5 \text{ MW} \\
 &= P_L + \Delta \omega
 \end{aligned}$$

The sum of the two generators should meet the load plus any increase in load because of frequency.

6. Obtain an expression for steady state change in system frequency Δf_{ss} for a step change in the load demand. Assume free governor operation.

CASE (I): [FREE GOVERNOR OPERATION]

Let the speed changer setting be fixed i.e. $\Delta P_c = 0$ and the load demand changes. This is known as free governor operation. Let the load on the system be changing in a step manner.

$$\therefore \Delta P_D(s) = \frac{\Delta P_D}{s} \quad [\because \text{Laplace Transform of step function is } 1/s]$$

Now the mathematical model for the above block diagram (Primary ALFC) with $\Delta P_c(s) = 0$.

$$\begin{aligned}
 &\left[-\Delta F(s) \cdot \frac{1}{R} \cdot \frac{K_G}{1+sT_G} \cdot \frac{K_T}{1+sT_T} - \frac{\Delta P_D}{s} \right] \frac{K_P}{1+sT_P} = \Delta F(s) \\
 &-\Delta F(s) \left[1 + \frac{1}{R} \cdot \frac{K_G}{1+sT_G} \cdot \frac{K_T}{1+sT_T} \cdot \frac{K_P}{1+sT_P} \right] = \frac{\Delta P_D}{s} \cdot \frac{K_P}{1+sT_P}
 \end{aligned}$$

$$S\Delta f(s) = - \frac{\left(K_p / (1 + sT_p) \right) \cdot \Delta P_D}{\left[1 + \frac{1}{R} \cdot \frac{K_g}{1 + sT_g} \cdot \frac{K_T}{1 + sT_T} \cdot \frac{K_p}{1 + sT_p} \right]}$$

From final value theorem;

The steady state change in system frequency;

$$\Delta f_{ss} = \lim_{s \rightarrow 0} S\Delta f(s) = - \frac{K_p}{\left[1 + \frac{1}{R} \cdot K_g K_T K_p \right]} \cdot \Delta P_D \quad \text{Let } K_g \cdot K_T = 1$$

$$= - \Delta P_D \cdot \left[\frac{K_p}{1 + \frac{1}{R} \cdot K_p} \right]$$

$$\Delta f_{ss} = - \Delta P_D \left[\frac{1}{\frac{1}{R} + \frac{1}{K_p}} \right] \quad \left[\because K_p = \frac{1}{D} \right]$$

$$= - \Delta P_D \left[\frac{1}{D + \frac{1}{R}} \right] \quad \text{--- (1)}$$

Define $B = D + \frac{1}{R} = \text{frequency Bias}$

$$\Delta f_{ss} = - \frac{1}{B} \cdot \Delta P_D \quad \text{--- (2)}$$

\therefore For rise in Load; $\Delta P_D = +ve \rightarrow \Delta f_{ss} = -ve$

for fall in load; $\Delta P_D = -ve \rightarrow \Delta f_{ss} = +ve$