

CBCS SCHEME

15CS653



Sixth Semester B.E. Degree Examination, Jan./Feb. 2021 Operations Research

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. What is operations research? Briefly explain the various phases of operations research study. (08 Marks)
- b. A person requires minimum 10, 12 and 12 units of chemicals for A, B and C respectively for his garden. A liquid product contain 5, 2 and 1 units of A, B and C respectively per Jar. A dry product contains 1, 2 and 4 units of A, B and C per jar. If the liquid product sells for Rs.3 per jar and dry product sells for Rs.2 per jar, how many of each should be purchased in order to minimize the cost and meet requirement. (08 Marks)

OR

- 2 a. Briefly explain the assumptions of linear programming. (04 Marks)
- b. Use Graphical method to solve the following:
Maximize $Z = 100x_1 + 40x_2$
Subject to $5x_1 + 2x_2 \leq 1000$
 $3x_1 + 2x_2 \leq 900$
 $x_1 + 2x_2 \leq 500$
 $x_1, x_2 \geq 0$ (07 Marks)
- c. Mention the advantages and limitations of L.P. (05 Marks)

Module-2

- 3 a. Define the terms:
(i) Feasible solution (ii) Feasible region
(iii) Optimal solution (iv) Unbound solution (04 Marks)
- b. Explain the steps involved in setting up of a Simplex method. (08 Marks)
- c. Define and illustrate with examples slack variables and surplus variables. (04 Marks)

OR

- 4 a. Solve the following LPP by using Big-M method.
Maximize $Z = -2x_1 - x_2$
Subjected to $3x_1 + x_2 = 3$
 $4x_1 + 3x_2 \geq 6$
 $x_1 + 2x_2 \leq 4$
 $x_1, x_2 \geq 0$ (08 Marks)
- b. Solve the following LPP by using two phase method:
Maximize $Z = 5x_1 + 8x_2$
Subjected to $3x_1 + 2x_2 \geq 3$
 $x_1 + 4x_2 \geq 4$
 $x_1 + x_2 \leq 5$
 $x_1, x_2 \geq 0$ (08 Marks)

Module-3

- 5 a. Explain two phase technique to solve in Simplex methods. (08 Marks)
 b. Write 5 key relationship between the primal and the dual problems. (05 Marks)
 c. Write the dual of the following LPP:

$$\text{Maximize } Z = 7x_1 + 4x_2 + 5x_3$$

$$\text{Subject to the constraints } 2x_1 + 4x_2 + 3x_3 \leq 10$$

$$x_1 + 3x_2 + x_3 \leq 6$$

$$\text{and } x_1, x_2, x_3 \geq 0$$

(03 Marks)

OR

- 6 a. Explain the essence of duality theory. (05 Marks)
 b. Write the dual of the following LPP.

$$\text{Minimize } Z = 3x_1 + 2x_2 + x_3$$

$$\text{Subject to the constraints } 2x_1 - 3x_2 + x_3 \leq 5$$

$$4x_1 - 2x_2 \geq 9$$

$$-8x_1 + 4x_2 + 3x_3 = 8$$

$$\text{and } x_1, x_2 \geq 0, x_3 \text{ is unrestricted}$$

(03 Marks)

- c. Solve the following LPP by using dual simplex method.

$$\text{Minimize } Z = 10x_1 + 6x_2 + 2x_3$$

$$\text{Subject to } -x_1 + x_2 + x_3 \geq 1$$

$$3x_1 + x_2 - x_3 \geq 2$$

$$\text{and } x_1, x_2, x_3 \geq 0$$

(08 Marks)

Module-4

- 7 a. Find the initial solution to the following transportation problem using VAM. (08 Marks)

		Destination				Supply
		D ₁	D ₂	D ₃	D ₄	
Factory	F ₁	3	3	4	1	100
	F ₂	4	2	4	2	125
	F ₃	1	5	3	2	75
Demand		20	80	75	25	300

- b. Explain different steps in Hungarian algorithm to solve an assignment problem. (08 Marks)

OR

- 8 a. Solve the following assignment problem. (08 Marks)

		Machines				
		M ₁	M ₂	M ₃	M ₄	M ₅
Jobs	J ₁	11	17	8	16	20
	J ₂	9	7	12	6	15
	J ₃	13	16	15	12	16
	J ₄	21	24	17	28	26
	J ₅	14	19	12	11	13



- b. Find the optimal transportation cost of the following matrix by using least cost method.

	A	B	C	D	E	Supply
P	4	1	2	6	9	100
Q	6	4	3	5	7	120
R	5	2	6	4	8	120
Demand	40	50	70	90	90	

(08 Marks)

Module-5

- 9 a. Solve the game whose pay off matrix is given by

(04 Marks)

		A		
		I	II	III
B	I	2	-1	8
	II	-4	-3	4
	III	-8	-4	0
	IV	1	-6	-2

- b. Explain the following:
- Minimax and maximin principles
 - Pure and mixed strategies
 - Two person zero sum game
 - Dominance principles

(12 Marks)

OR

- 10 Write short notes on:
- Metaheuristics
 - Tabu search algorithm
 - Simulated Annealing algorithm
 - Genetic Algorithm

(16 Marks)



