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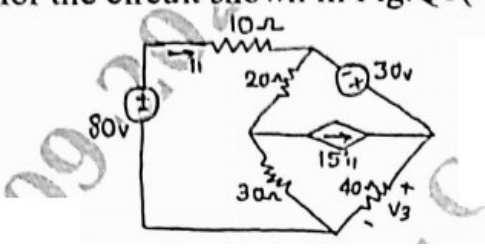
CMR INSTITUTE OF TECHNOLOGY

Internal Assessment Test - II

Sub:	Electric Circuit Analysis						Code:	18EE32	
Date:	17/02/2021	Duration:	90 mins	Max Marks:	50	Sem:	3 rd	Branch:	EEE
Answer Any FIVE FULL Questions									

Marks/CO/RBT

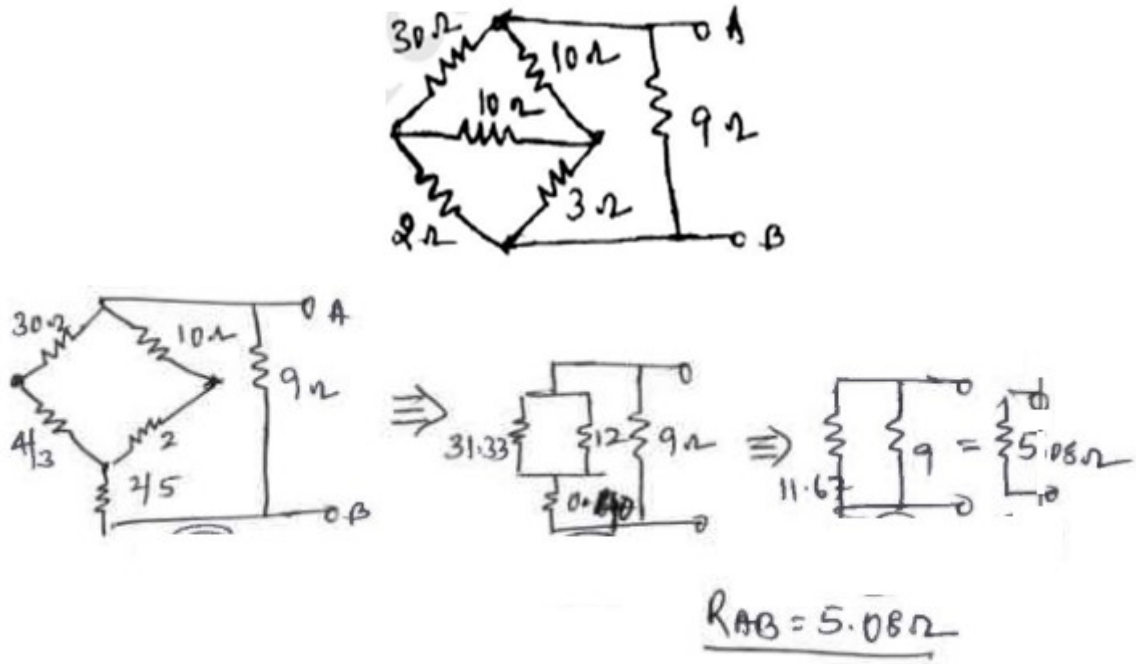
1. (Determine voltage V_3 for the circuit shown in Fig.Q1(a), using Mesh analysis method.



(5)(CO1)(L3)

- (b) Find the equivalent resistance R_{AB} using Delta-Star Transformation.

(5)(CO2)(L3)



2. (a) Use node equations to determine what value of 'E' will cause V_x to be zero for the network shown in fig. (5)(CO2)(L3)

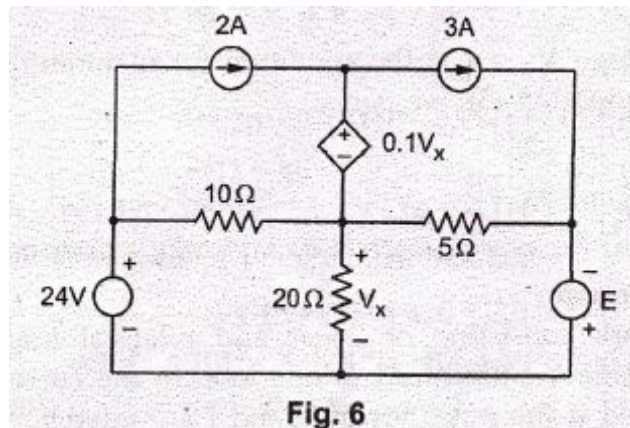
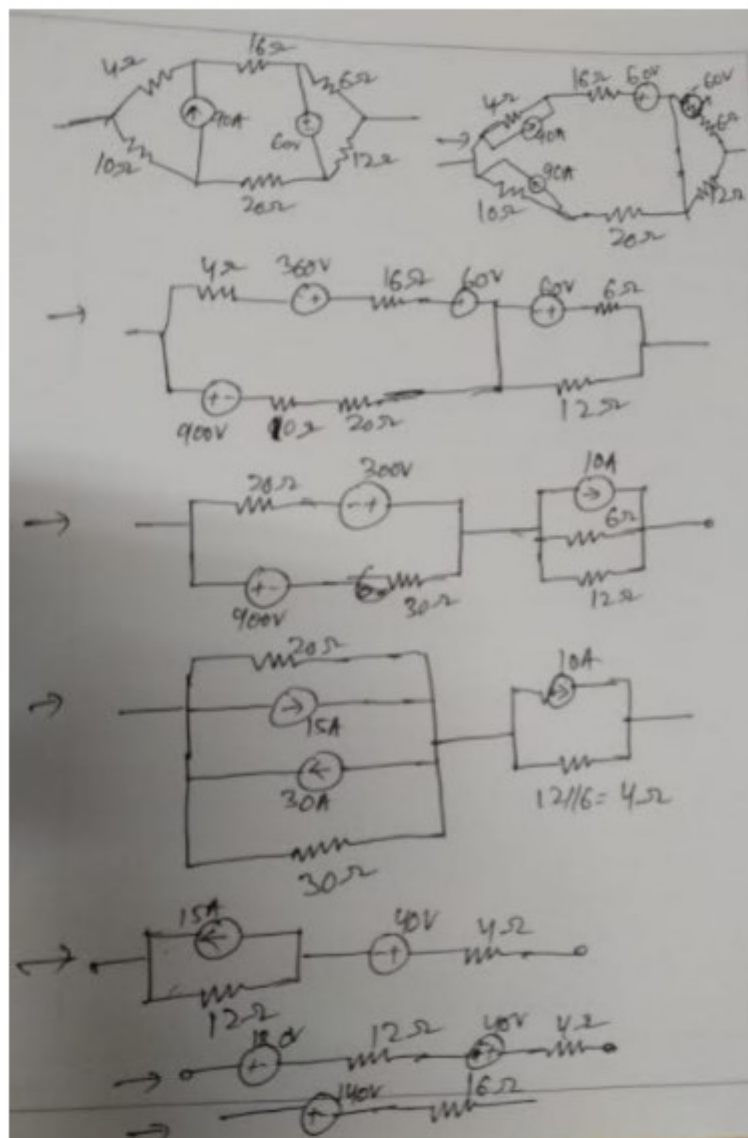
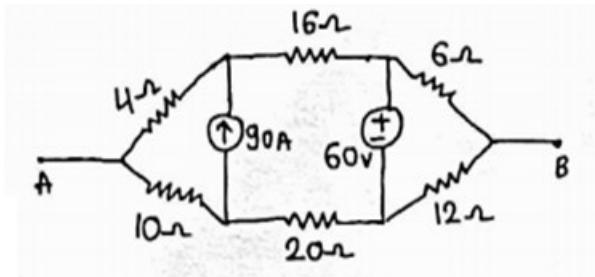


Fig. 6

(b) Convert the given circuit into a single voltage source in series with a single resistance using source transformation & shifting. (5)(CO2)(L3)



3. a) For the network shown in Fig. 2 determine the node voltages V_1 , V_2 , V_3 and V_4 using nodal analysis. (5)(CO2)(L3)

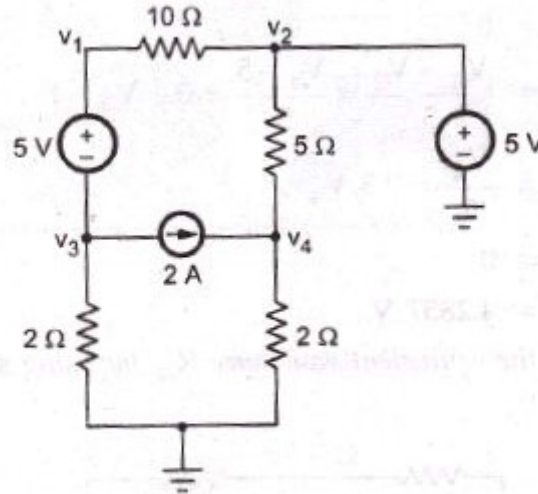
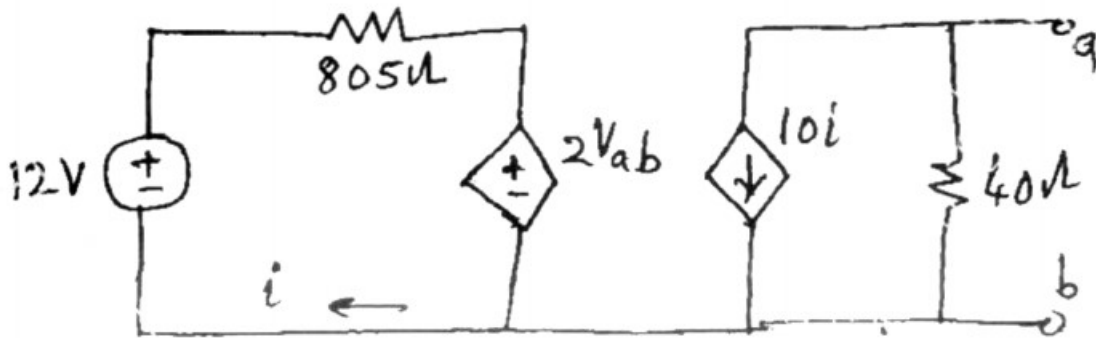


Fig. 2

- (b) Find Thevenin's & Norton's equivalent circuit for the given network. (5)(CO2)(L3)



Apply KVL to loop 1

$$12 - 805i - 2V_{ab} = 0$$

$$805i + 2V_{ab} = 12 \quad \text{--- (1)}$$

Apply KVL to loop 2

$$V_{ab} = 40(-10i)$$

$$i = \frac{-V_{ab}}{400} \quad \text{--- (2)}$$

Sub (2) in (1)

$$805 \left(\frac{-V_{ab}}{400} \right) + 2V_{ab} = 12$$

$$-2.0125 V_{ab} + 2V_{ab} = 12$$

$$-0.0125 V_{ab} = 12$$

$$V_{oc} = V_{ab} = -960V$$

$\therefore i = \frac{-V_{ab}}{400}$

$$= \frac{-(-960)}{400} = 2.4A$$

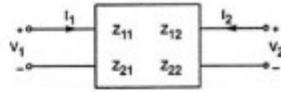
$i_{40} = 10i = 10 \times 2.4 = 24A \text{ (A to b)}$

4. Describe about Z-parameter & draw its equivalent circuit. Derive the relationship between Z & ABCD parameters. (10)(CO3)(L3)

Two port network parameters:

Z parameters.

It is also called as impedance parameters or open circuit parameters.



The Z parameters equations are obtained by considering I_1 and I_2 of the network as independent variables and V_1 and V_2 are the dependent variables. The impedance parameters are obtained by expressing voltages at two ports in terms of currents at two ports.

$$V_1 = f_1(I_1, I_2)$$

$$V_2 = f_2(I_1, I_2)$$

In equation form

$$V_1 = Z_{11} I_1 + Z_{12} I_2$$

$$V_2 = Z_{21} I_1 + Z_{22} I_2$$

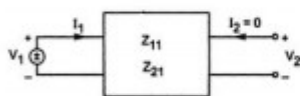
In matrix form

$$[V] = [Z] [I]$$

$$\begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

Individual Z parameters

Sub $I_2=0$ (Output port is open circuited)



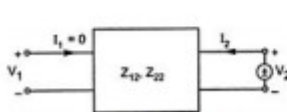
$$V_1 = Z_{11} I_1$$

$$V_2 = Z_{21} I_1$$

$$Z_{11} = \frac{V_1}{I_1}$$

$$Z_{21} = \frac{V_2}{I_1}$$

Sub $I_1=0$ (Input port is open circuited)



$$V_1 = Z_{12} I_2$$

$$V_2 = Z_{22} I_2$$

$$Z_{12} = \frac{V_1}{I_2}$$

$$Z_{22} = \frac{V_2}{I_2}$$

Z_{11} = Open circuit input driving point impedance

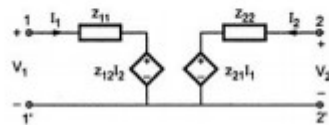
Z_{22} = Open circuit output driving point impedance

Z_{12} = Open circuit forward transfer impedance

Z_{21} = Open circuit reverse transfer impedance

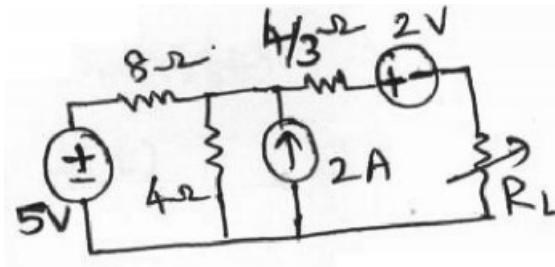
Where Z_{11} , Z_{12} , Z_{21} and Z_{22} are called as impedance parameters. These parameters are defined only when the current in any one of the port is zero.

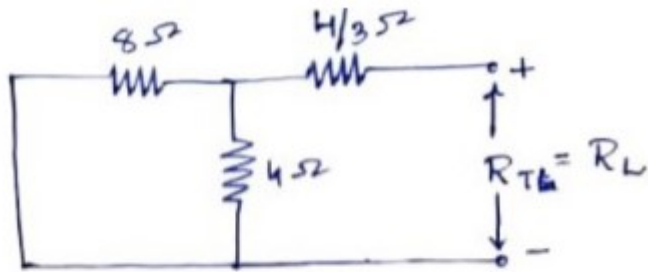
Equivalent Circuit



5. (a) Find the value of R_L for which maximum power is delivered to it.

(6)(CO3)(L3)





$$R_T = R_L = 8 \parallel 4 + \frac{4}{3} = \frac{8(4)}{8+4} + \frac{4}{3} = \frac{32}{12} + \frac{4}{3}$$

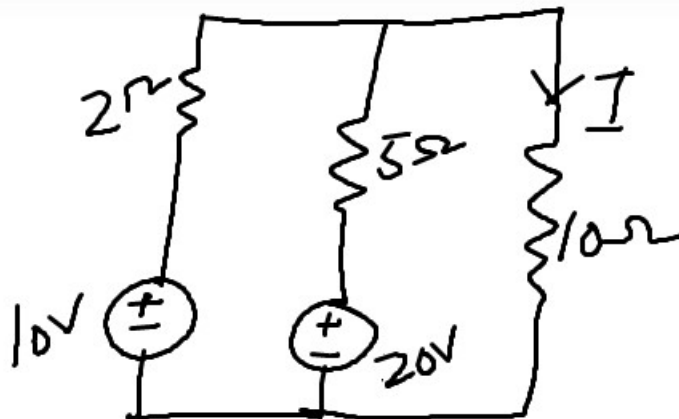
$$= \frac{32 + 16}{12}$$

$$= \frac{48}{12}$$

$$R_T = R_L = 4 \Omega$$

(b) Find current I using Millman's Theorem.

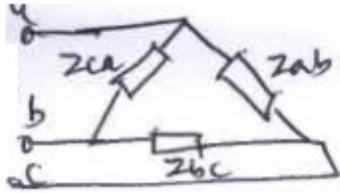
(4)(CO3)(L3)



6. a)

Determine the line currents and total power supplied to a delta connected load of $Z_{ab} = 10 \angle 60^\circ \Omega$, $Z_{bc} = 20 \angle 90^\circ \Omega$ and $Z_{ca} = 25 \angle 30^\circ \Omega$. Assume a 3 phase, 400 V, ABC system.

(5)(CO5)(L3)



$$V_L = V_{ph} = 400V$$

$$V_{ab} = 400\angle 0^\circ, V_{bc} = 400\angle -120^\circ, V_{ca} = 400\angle 120^\circ$$

Phase currents

$$I_{ab} = \frac{V_{ab}}{Z_{ab}} = \frac{400\angle 0^\circ}{10\angle 60^\circ} = 40\angle -60^\circ A$$

$$I_{bc} = \frac{V_{bc}}{Z_{bc}} = \frac{400\angle -120^\circ}{20\angle 90^\circ} = 20\angle -210^\circ A$$

$$I_{ca} = \frac{V_{ca}}{Z_{ca}} = \frac{400\angle 120^\circ}{25\angle 30^\circ} = 16\angle 90^\circ A$$

$$I_a = 54.45\angle -68.45^\circ, I_b = 58.173\angle 129.88^\circ, I_c = 18.316\angle 119.1^\circ$$

$$P = P_{ab} + P_{bc} + P_{ca} = 13.542 \text{ kW}$$

b)

Determine the line currents in an unbalanced star connected load supplied from a symmetrical 3 phase, 440 V system. The branch impedances are $Z_R = 4\angle 30^\circ \Omega$, $Z_Y = 10\angle 45^\circ \Omega$ and $Z_B = 10\angle 60^\circ \Omega$. The phase sequence is RYB.

(5)(CO5)(L3)

1st loop:-

$$-(4\angle 30^\circ)j_1 - (10\angle 45^\circ)j_1 + V_{RY} + (10\angle 45^\circ)j_2 = 0$$

$$V_{RY} = (4\angle 30^\circ)j_1 + (10\angle 45^\circ)j_1 - (10\angle 45^\circ)j_2$$

$$440\angle 0^\circ = (13.9\angle 40.73^\circ)j_1 - (10\angle 45^\circ)j_2 \rightarrow (1)$$

2nd loop:-

$$V_{YB} = -(10\angle 45^\circ)j_1 + (19.82\angle 52.7^\circ)j_2 \rightarrow (2)$$

$$\begin{bmatrix} (13.9\angle 40.73^\circ) & -(10\angle 45^\circ) \\ -(10\angle 45^\circ) & (19.82\angle 52.7^\circ) \end{bmatrix} \begin{bmatrix} j_1 \\ j_2 \end{bmatrix} = \begin{bmatrix} 440\angle 0^\circ \\ 440\angle 120^\circ \end{bmatrix}$$

By Cramer's rule:-

$$j_1 = 39.7\angle -72.52^\circ$$

$$j_2 = 29.26\angle -129.28^\circ$$

Line currents

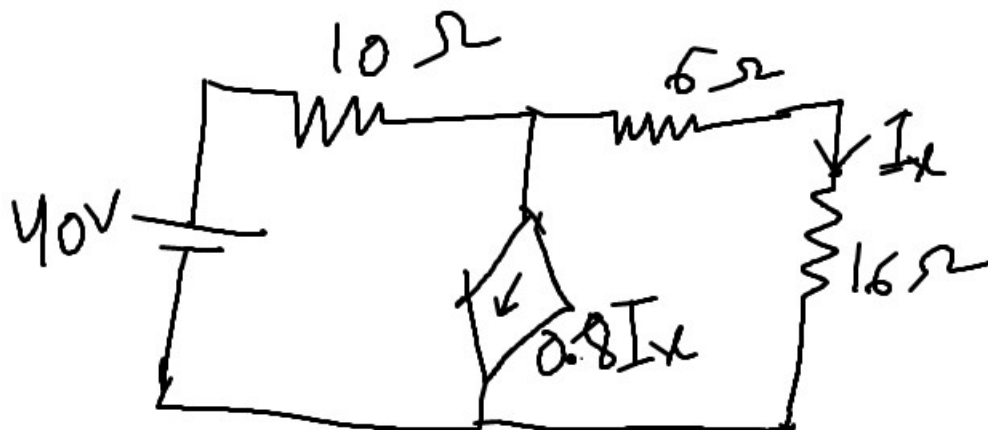
$$I_a = j_1 = 39.7\angle -72.52^\circ A$$

$$I_b = j_2 - j_1 = 34\angle 153.44^\circ A$$

$$I_c = -j_2 = 29.26\angle 50.72^\circ A$$

7. (a) Find current through 16Ω resistor using Norton's Theorem.

(5)(CO3)(L3)



To find V_{th} :-

$I_x = 0 \rightarrow 0.8V_x = 0$

$V_{th} = 40V$

To find J_{sc} :-

$J_{sc} = I_x$

KCL at node :-

$$0.8J_{sc} + \frac{V_x - 40}{10} + \frac{V_x}{6} = 0$$

$$0.8J_{sc} + \frac{V_x - 40}{10} + J_{sc} = 0$$

$$1.8J_{sc} + 0.1V_x = 4$$

$$1.8J_{sc} + 0.1(6J_{sc}) = 4 \Rightarrow J_{sc} = 1.666A$$

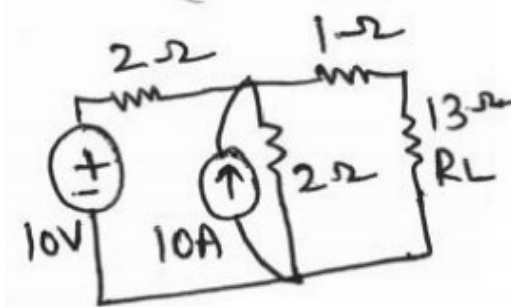
$R_{th} = \frac{V_{th}}{J_{sc}} = \frac{40}{1.666} = 24\Omega$ - 1M

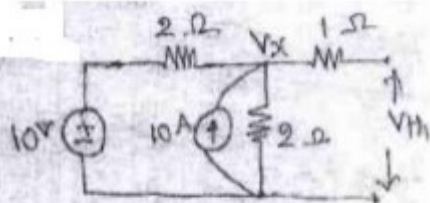
$I_{16\Omega} = \frac{1.666 \times 24}{24 + 16} \approx 1A$ - 2M

-3-

(b) Find current through R_L using Thevenin's Theorem

(5)(CO3)(L3)



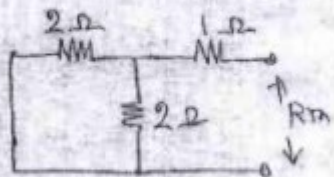


$$V_{th} = V_x$$

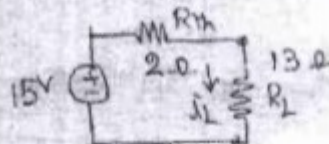
KCL @ node :-

$$10 = \frac{V_x}{2} + \frac{V_x - 10}{2}$$

$$\therefore V_x = V_{th} = 15V$$



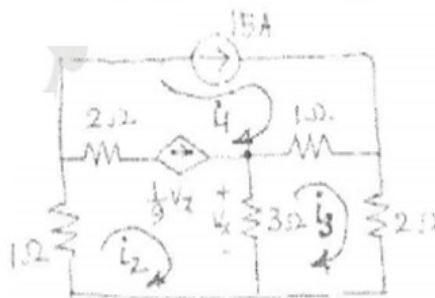
$$R_{th} = \frac{2 \times 2}{2 + 2} + 1 = 2\Omega$$



$$i_L = \frac{V_{th}}{R_{th} + R_L} = 1A$$

8. a)

Find the loop currents i_1 , i_2 and i_3 using Mesh analysis for the network shown



(5)(CO1)(L3)

Loop equations: Supermesh (comprising of ① & ②) loops gets open circuited

$$i_1 = 15 \text{ A}; \quad \text{--- (1)}$$

$$-i_1 - 3i_2 + 6i_3 = 0 \quad \text{for Mesh (3)} \quad \text{--- (2)}$$

$$i_2 - i_1 = \frac{1}{9} V_x = \frac{1}{9} [3(i_2 - i_3)] \quad \text{or} \quad \text{where } V_x = V_{3\Omega} \text{ across } 3\Omega$$

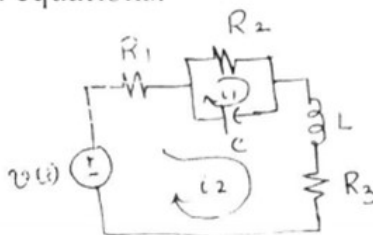
$$-i_1 + \frac{2}{3}i_2 + \frac{1}{3}i_3 = 0 \quad \text{--- (3)}$$

on Solving ①, ② and ③

$$i_1 = 15 \text{ A}, \quad i_2 = 17 \text{ A} \quad \text{and} \quad i_3 = 11 \text{ A}$$

b)

Write the equilibrium equations using KVL for the network shown in Fig.Q.2(b). Draw its dual and also write equilibrium equations.



(5)(CO2)(L3)