write the relation matrix and digraph of R.

(06 Marks)

(07 Marks)

(07 Marks)

Draw the Hasse diagram for the subset relation on the power set of $A = \{a, b, c\}$.

- For any sets A, B, C \subseteq U, prove that $A \times (B C) = (A \times B) (A \times C)$. (06 Marks)
 - Show that if any (n + 1) numbers from $\{1, 2, 3, \dots, 2n\}$ are chosen, then two of them will have their sum equal to (2n + 1). (07 Marks)
 - Let $A = \{1, 2, 3, 4, 5\}$ and R be a relation on $A \times A$ defined by (a, b) R (c, d) if and only if a + d = b + c. Show that R is equivalence relation. Determine the partition induced by R and the equivalence class [(2, 5)]. (07 Marks)

Module

- Determine the number of positive integers n where $1 \le n \le 100$, and n is not divisible by 2, 3
 - An apple, a banana, a mango and an orange are to be distributed for four boys A, B, C, D. The boys A and B do not wish to have apple. C does not want banana or mango and D refuses orange. In how many ways the distribution can be made so that no boy is displeased? (07 Marks)
 - Solve $2a_n = 7a_{n-1} 3a_{n-2}$ for $n \ge 2$ and $a_0 = 2$, $a_1 = 5$.

(07 Marks)

- Define the principle of inclusion and exclusion and generalization of the principle. (06 Marks) (07 Marks)
 - Find the rook polynomial of the chess board. (Refer Fig. Q8 (b)). b.



 $-2a_{n-2}$ for $n \ge 2$ and $a_0 = 1$, $a_1 =$

07 Marks

Discuss the Konigsberg-bridge problem and solution.

Define Isomorphic graphs. Show that the following two graphs are isomorphic. (Refer Fig. Q9 (b)) (07 Marks)

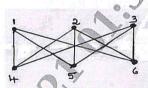


Fig. 09 (b)

Construct an optimal prefix code for the symbols a, b, c, d, e, f, that occur with respective frequencies 20, 28, 4, 17, 12, 7. (07 Marks)

- Find the number of spanning sub graphs of the graph given below. How many of them are 10 connected. How many are spanning trees? (06 Marks)
 - Prove that for every tree $T \equiv (V, E)$, if $|V| \ge 2$ then T has at least two pendent vertices.

(07 Marks)

Define directed tree, rooted tree, binary rooted tree, complete binary tree, m-ary tree complete m-ary tree, leaf. (07 Marks)

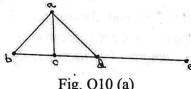


Fig. Q10 (a)