

IAT: 01

Hydrology & Irrigation Engineering

Q3 A catchment has six rain gauge stations. in a year. the annual rainfall recorded by the gauges are

Stations	A	B	C	D	E	F
Rainfall (cm)	92.8	112.6	190.8	110.3	99.8	146.7

For a 10% Error in the estimation of the mean rainfall in the existing set of rain gauges optimum number of stations in the catchment

for Given data

Number of rain gauges $m=6$

Mean annual rainfall $\bar{P} = 125.5$

$$\bar{P} = \frac{1}{m} \left[\sum_{i=1}^m P_i \right]$$

$$= \frac{1}{6} \{ 92.8 + 112.6 + 190.8 + 110.3 + 99.8 + 146.7 \}$$

$$\bar{P} = 125.5$$

Standard deviation $\sigma_{m-1} =$

$$9994.92 + 1109.93$$

$$\sigma_{m-1} = \sqrt{\frac{\sum_{i=1}^m (P_i - \bar{P})^2}{m-1}}$$

$$= \sqrt{\frac{(92.8-125.5)^2 + (112.6-125.5)^2 + (190.8-125.5)^2 + (110.3-125.5)^2 + (99.8-125.5)^2 + (146.7-125.5)^2}{6-1}}$$

$\sigma_{m-1} = 47.12$ Standard deviation

$$\text{Co-efficient of Variation } C_v = \frac{100 \times \sigma_{m-1}}{\bar{P}} = \frac{100 \times 47.12}{125.5} = 37.54$$

(a) Standard Error in the estimation of the mean

$$= E_{ex} = \frac{C_v}{\sqrt{m}} = \frac{37.54}{\sqrt{6}} = 15.32\%$$

When the Error is limited to 10%. $\epsilon = 10$ and the optimum number of rain gauges in the catchment

$$\text{is Given by } N = \left(\frac{C_v}{\epsilon}\right)^2 = \left(\frac{37.54}{10}\right)^2 = 8.72$$

Hence optimum number of rain gauges is 9 rain gauges
Thus the number of additional rain gauges required = $(9 - 6) = 3$

Q5) Explain with formulae to find the optimum no of rain gauge Station.

If there are already some rain gauge Stations in a catchment the optimal number of Stations that should exist to have an assigned percentage of Error in the Estimation of mean rainfall is obtained by Statistical mean rainfall is obtain by Statistical analysis as

$$N = \left(\frac{C_v}{\epsilon}\right)^2$$

Where N = optimal number of Stations

ϵ = allowable degree of Error in the Estimate of the mean rainfall & co-efficient of variation of the rainfall and

C_v = co-efficient of variation of the rainfall values at m Station in the catchment Each recording rainfall values = $P_1, P_2, P_3, \dots, P_m$ in a know time the co-efficient of variation of C_v is calculation

$$C_v = \frac{100 \times \sigma_{m-1}}{\bar{p}}$$

Where $\sigma_{m-1} = \sqrt{\frac{\sum_{i=1}^m (P_i - \bar{p})^2}{m-1}}$ Standard deviation

P_i - Precipitation magnitude in the i th Station

$$\bar{p} = \frac{1}{m} \left[\sum_{i=1}^m (P_i) \right] \text{ mean precipitation}$$

Consider the existing m rain gauges they have a mean rainfall of \bar{p} and a coefficient of variation of C_v . To know the percentage of error (E_{cx}) of the estimation of mean in the existing system of m rain gauge Eq can be rearranged changing N by m as

$$m = \left(\frac{C_v}{E_{cx}} \right)^2 = E_{cx} = \frac{C_v}{\sqrt{3}}$$

In the above Eqⁿ the term E_{cx} represents the Expected Error (in percentage) in the estimation of a mean \bar{p} . It is a measure of the accuracy of estimation of mean precipitation in the existing system and is called Standard Error in the estimation of the mean. In calculating the number of rain gauges N for a given level of error by using Eqⁿ it is usual to take E_{cx} as 10%. It is seen that if the value of E_{cx} is small no. of rain gauge required be more.

Q28 The details of Thiessen polygons surrounding each rain gauge and the recordings of the rain gauges in the month of August 2011 are given below

Stations	A	B	C	D	E	F
Rainfall	121	134	145	126	99.8	115
Thiessen polygon area (km ²)	720	380	440	1040	800	220

determine the average depth of rainfall on the basin in August 2011 by
 i) Thiessen polygon method and ii) arithmetic mean method

Solution (ii) Arithmetic Mean: only rain gauge station.

1, 2 and 4 are within the basin

Hence the arithmetic mean is obtained

by considering the readings of these station only

$$\bar{p} = \frac{P_1 + P_2 + \dots + P_i + \dots + P_n}{N} = \frac{1}{N} \sum_{i=1}^n P_i$$

$$= \frac{121 + 134 + 126}{3} = 127 \text{ mm}$$

(i) Thiessen Mean:- the calculation are performed in the tabular form

Total area of basin = Total of col 2 = 3600 km²

Rain gauge Station	Thiessen polygon area = (km ²)	Thiessen Weightage Factor (= Fraction of total area (col 2 / 3600))	Station reading (= Monthly Rainfall in mm)	Weighted Station rainfall (mm) = (col 3 x col 4)
1	720	0.200	121	24.2
2	380	0.106	134	14.1
3	440	0.122	145	17.7
4	1040	0.289	126	36.4
5	800	0.222	99.8	22.155
6	220	0.061	115	7.0
Total catchment area = 3600		1.000		121.655

Thiessen mean of the station readings for the month of Aug. 2011 Total of col 5 = 121.655 mm

07 List out various types of measuring rain gauges.
Explain with a neat sketch of Syphon's rain gauge

Two types of Rain gauge

01 Non Recording rain gauge

(a) Syphon's rain gauge

(b) IMD rain gauge

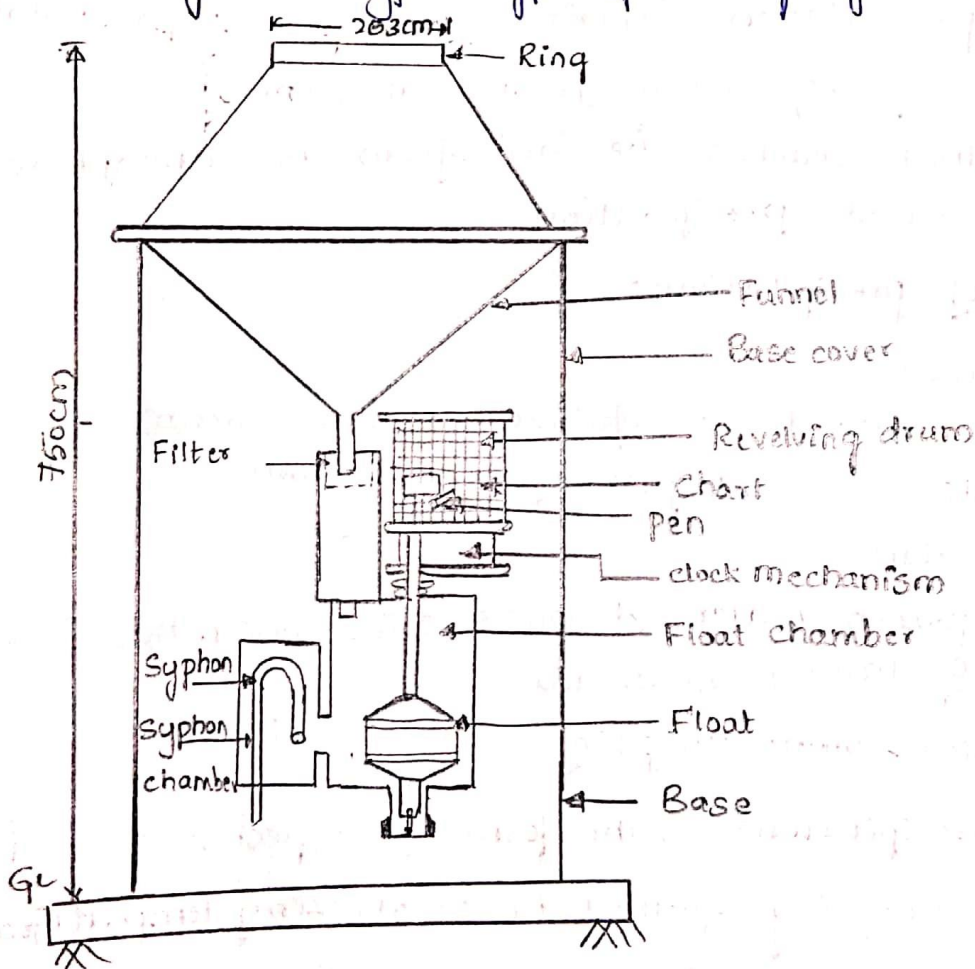
02 Recording Rain gauge

01) Tipping bucket type rain gauge

02) Weighing bucket type rain gauge

03) Flat type rain gauge / Natural Syphon type rain gauge

01) ~~Syphon's~~ Syphon type of Rain gauge



- This is also called integrating rain gauge as it depicts an integrated graph of rain fall with respect to time
- A receiver and funnel arrangement drain the rainfall into a container in which a float mechanism at the bottom is provided
- As water accumulates the float rises. A pen arm attached to the float mechanism continuously records the rainfall on a clock driven chart and also produces a mass curve of rainfall
- When the water level rises above the crest of the siphon the accumulated water in the container will be drained off the syphonic action the rain gauge is ready to receive the new rainfall

01) (a) Define precipitation. Explain different forms of precipitation

The term precipitation denotes all form of water that reaches the Earth from the atmosphere is called precipitation

formation of precipitation:

0) Rain & Drizzle:

Rain - water droplets of size = 0.5mm to 6mm

Drizzle - water droplets of size < 0.5mm

02) Sleet and Hail

Sleet: frozen water droplets or ice which has size of 1mm to 4mm dia

Hail: size > 5mm lumps of ice

03) Snow: precipitation in the form of ice flecks

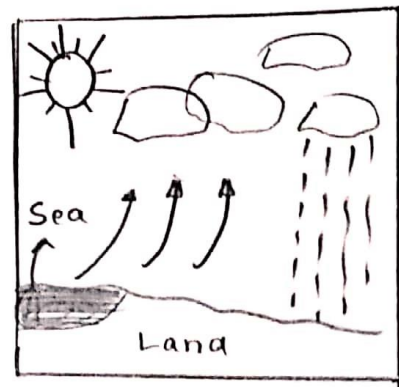
04) Glaze: ice coating formed due to freezing temp at ground

05) Dew: These water droplets formed due to condensation of atmospheric moisture during night

Types of precipitation:-

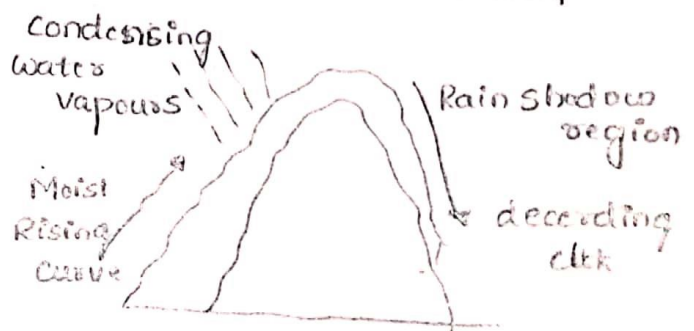
01 Convective precipitation

- This type of precipitation occurs due to even heating of air masses
- The air mass close to the Earth surface gets heated and its density decreases
- Consequently the air mass rises upward in the atmosphere and it gets cooled adiabatically to form cloud precipitation caused by such clouds is called convective precipitation
- It covers a small area (less than 50 km^2)
- The rain fall intensity may be very high. Sometimes it may even reach 100 cm/hr



02 Orographic precipitation

- The precipitation caused by lifting of air over a mountain barrier is called orographic precipitation



- Due to lifting air masses get cooled and condensation process takes place
- Heavy precipitation occurs on the windward side of the mountain whereas on the leeward direction

03 Cyclonic / frontal precipitation

- Air tends to move into the low pressure zone from surrounding areas

04 Turbulent precipitation

- This type of precipitation occurs when an air mass is forced to rise up due to friction of the Earth surface