

HEAT TRANSFER (18ME73/17ME73)

IAT 2

Instructions:

Each question carries 10 Marks

Attempt all 5 questions

Use of heat transfer data hand book is permitted

Max Marks: 50

Duration: 1.5 hrs

1. A steel rod ($k=32\text{W/mK}$), 12mm in diameter and 60 mm long, with an insulated end, is to be used as a spine. It is exposed to surroundings with a temperature of 60°C and a heat transfer coefficient of $55\text{W/m}^2\text{K}$. The temperature at the base of fin is 95°C . Determine:
 - I. The Fin efficiency
 - II. The temperature at the edge of the spine
 - III. The rate of heat transfer
 - IV. Fin Effectiveness
2. A short fin with insulated tip of 0.08 m length and diameter 12 mm is exposed to air at 30°C . Thermal conductivity is 15 W/mK . The base temperature is 280°C . The heat dissipated by the fin is 7W. Determine the value of convection coefficient and also the tip temperature.
3. Saturated steam at 110°C flows inside a copper pipe ($k= 450 \text{ W/mK}$) having an internal diameter of 10 cm and external diameter of 12 cm. Convective heat transfer coefficient for steam side is $1200 \text{ W/m}^2\text{K}$ and for outside surface of pipe is $18 \text{ W/m}^2\text{K}$. Determine the rate of heat loss in the pipe if it is located in space at 25°C . Determine the % increase/decrease in rate of heat loss if the pipe is lagged with 5cm thick insulation ($k= 0.22 \text{ W/mK}$).
4. A steel slab 16 cm thickness, has thermal conductivity $k = 51 (1 - 8.6 \times 10^{-4} T)$ k is the thermal conductivity at $T^\circ\text{C}$ in W/mK . The slab surfaces are maintained at 400°C and 180°C . Determine the heat flow rate, the temperature and temperature gradient at 4cm from the end at 400°C .
5. A wire of 8mm diameter at a temperature of 60°C is to be insulated by a material having $k = 0.174 \text{ W/mK}$. Heat transfer coefficient between surface and atmosphere is $8\text{W/m}^2\text{K}$ and ambient temperature is 25°C . For maximum heat loss find the minimum thickness of insulation. Find % increase in heat dissipation due to insulation.

HT IAT-II

- ① Given, $k = 32 \text{ W/mK}$ $L = 60 \times 10^{-3} \text{ m}$
 $d = 12 \times 10^{-3} \text{ m}$ $T_{\infty} = 60^{\circ}$
 $T_b = 95^{\circ}$ $h = 55 \text{ W/m}^2\text{K}$

$$m = \sqrt{\frac{h_p}{k A_2}} = \sqrt{\frac{4h}{kd}} = \sqrt{\frac{4 \times 55}{32 \times 12 \times 10^{-2}}} \\ = 23.935$$

i) $\eta = \frac{Q_{fin}}{Q_{max}}$

ii) At the edge of the spine temp \rightarrow
 $x = L$ at the edge of spine

$$\frac{T_L - T_{\infty}}{T_b - T_{\infty}} = \frac{\cosh h[m(L-L)]}{\cosh h(mL)}$$

$$\frac{T_L - 60}{95 - 60} = \frac{\cosh h(0)}{\cosh h(23.935 \times 60 \times 10^{-3})}$$

$T_L = 75.75^{\circ}$

iii) Rate of heat transfer

$$Q_{\text{fin}} = \sqrt{h_p k A_c \frac{\theta_b}{\theta_b + \tanh(mL)}}$$

$$= \sqrt{55 \times \pi \times 12 \times 10^{-3} \times 32 \times \pi \times (6 \times 10^{-3})^2}$$
$$\times (95 - 60) \times$$
$$\tanh(23.935 \times 60 \times 10^{-3})$$

$$Q_{\text{fin}} = 2.7 \text{ watt}$$

∴ Efficiency

$$\eta = \frac{Q_{\text{fin}}}{Q_{\text{max}}} = \frac{\sqrt{h_p k A_c \frac{\theta_b}{\theta_b + \tanh(mL)}}}{h_p \rho L \theta_b}$$

~~$$\eta = \frac{\sqrt{h_p k A_c \frac{\theta_b}{\theta_b + \tanh(mL)}}}{h_p \rho L \theta_b}$$~~
$$= \frac{\sqrt{h_p k A_c} \times \frac{1}{L} \times \tanh(mL)}{h_p \rho L \theta_b}$$

$$\frac{\tanh(mL)}{m} = \frac{\tanh(23.935 \times 60 \times 10^{-3})}{23.935 \times 60 \times 10^{-3}}$$

$$\Rightarrow 0.6217 = \underline{62.17\%}$$

iv)

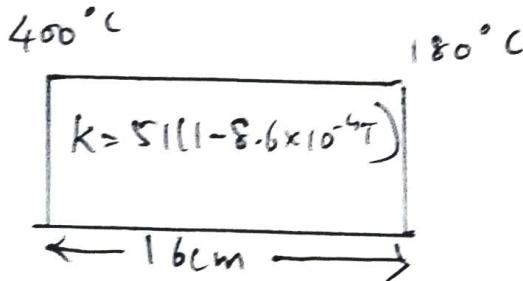
$$\text{Fin effectiveness} = \frac{Q_{\text{with fin}}}{Q_{\text{without fin}}}$$

$$Q_{\text{without fin}} = h A_c \theta_b$$

$$\begin{aligned} \text{Fin effectiveness} &= \frac{2.7}{\frac{35 \times \pi \times (12 \times 10^{-3})^2}{4} (95 - 60)} \\ &= 12.40 \end{aligned}$$

$$\text{Fin effectiveness} = 12.40$$

(4)



$$\text{Here } k = 51 (1 - 8.6 \times 10^{-4} T)$$

$$\text{Wkt } Q = -kA \frac{dT}{dx}$$

$$Q dx = -51 (1 - 8.6 \times 10^{-4} T) A dT$$

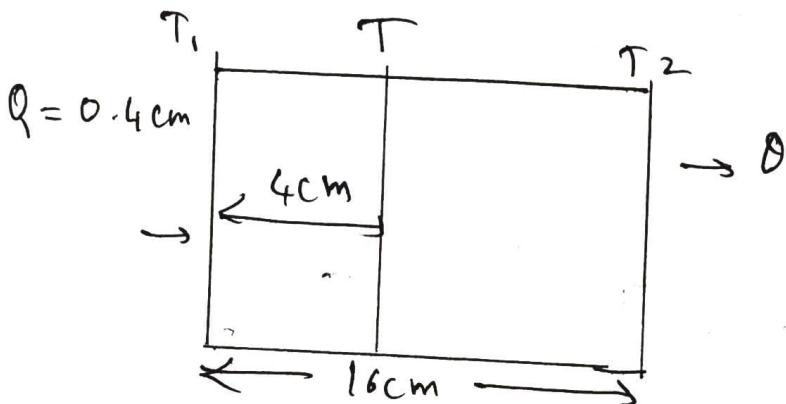
$$Q \int_{0.16}^{0.16} dx = \int_{400}^{180} 51 (1 - 8.6 \times 10^{-4} T) A dT$$

$$Q \int_0^{0.16} dx = -51 A \int_{400}^{180} (1 - 8.6 \times 10^{-4} T) dT$$

$$Q \times [0.16 - 0] = -51A \left[(480 - 400) - 8.6 \times 10^{-4} \frac{(180^2 - 400^2)}{2} \right]$$

$$\frac{Q}{A} = \frac{51}{0.16} \left[(400 - 180) - \frac{8.6 \times 10^{-4} (400^2 - 180^2)}{2} \right]$$

$$\boxed{\frac{Q}{A} = 52635.825 \text{ W/m}^2}$$



$$Q = -kA \frac{dT}{dx}$$

$$\frac{Q}{A} dx = -51 (1 - 8.6 \times 10^{-4} T) dT$$

$$52635.825 \int_0^{0.04} dx = -51 \int_{400}^T (1 - 8.6 \times 10^{-4} T) dT$$

$$52635.825 [0.04 - 0] = -51 \left[(T - 400) - 8.6 \times 10^{-4} \frac{(T^2 - 400^2)}{2} \right]$$

$$52635.825 \times 0.04 = 51 \left[400 - T - \frac{8.6 \times 10^{-4} \times (400^2 - T^2)}{2} \right]$$

$$\frac{51 \times 8.6 \times T^2}{2} - 51T + \frac{51 \times 400 - 8.6 \times 10^{-4} \times 400^2}{2}$$

$$- 52635.825 \times 0.04 \\ = 0$$

$$T = 339.47^\circ C$$

$$\downarrow \\ 1986.1$$

So, $\boxed{T = 339.47^\circ C}$

$$\therefore \frac{Q}{A} = 52635.825 \text{ W/m}^2$$

$$T_{4\text{cm}} = 339.5^\circ C$$

$$Q = -kA \underbrace{\frac{dT}{dx}}$$

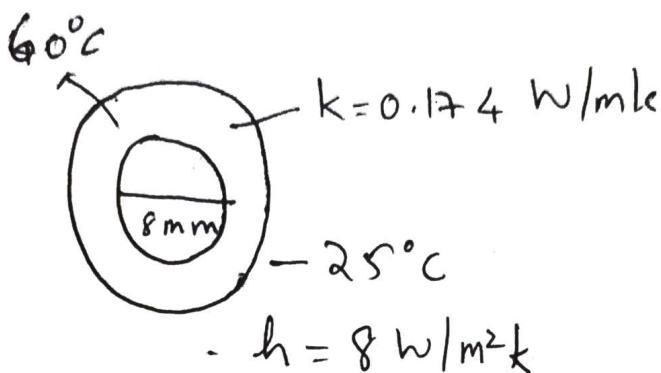
$$\frac{dT}{dx} = -\frac{Q}{kA} = \frac{-52635.825}{51(1 - 8.6 \times 10^{-4}T)}$$

$$\frac{dT}{dx} \Big|_{4\text{cm}^2} = \frac{-52635.825}{51(1 - 8.6 \times 10^{-4} \times 339.5)}$$

$$\frac{dT}{dx} = -1457.17 \text{ K/m or } ^\circ\text{C/m}$$

\approx

(5)



$$k = 0.174 \text{ W/mK}$$

$$h = 8 \text{ W/m}^2\text{K}$$

$$\tau_c = \frac{k}{h} = \frac{0.174}{8} = 0.0218 \text{ m}$$

$$t_c = \tau_c - \tau_i = 0.0218 - 4 \times 10^{-3} = 0.0178 \text{ m}$$

$$t_c = 17.8 \text{ mm}$$

$$Q_w = \frac{T_1 - T_2}{\frac{1}{2\pi k_e} \ln \left(\frac{\lambda_c}{\tau_i} \right) + \frac{1}{2\pi \tau_c h}} \rightarrow \text{Case in } \underline{\text{with insulation}}$$

$$\frac{1}{2\pi k_e} \ln \left(\frac{\lambda_c}{\tau_i} \right) + \frac{1}{2\pi \tau_c h}$$

$$\frac{Q_H}{d} = \frac{60 - 25}{\frac{1}{2\pi \cdot 0.174} \ln \left(\frac{0.0218}{4 \times 10^{-3}} \right) + \frac{1}{2\pi (0.0218) \times 8}}$$

Case ii \rightarrow Without insulation

$$\frac{Q_{W10}}{l} = \frac{T_1 - T_2}{\frac{1}{h(2\pi\lambda)d}} = \frac{60 - 25}{\frac{1}{8(2\pi(4 \times 10^{-3})}}} = 7.037 \text{ W/m}$$

% increase in heat dissipation

$$= \frac{14.2 - 7.037}{7.037} \times 100 \\ = \boxed{101.88 \%}$$

②

$$L = 0.08 \text{ m}$$

$$d = 12 \times 10^{-3} \text{ m} \quad T_\infty = 30^\circ \text{C}$$

$$k = 15 \text{ W/mK} \quad Q = 7 \text{ W}$$

$$T_b = 280^\circ \text{C}$$

$$m = \sqrt{\frac{h_p}{kA_c}}$$

$$m = \sqrt{\frac{h \times \pi \times d}{k \times \pi \times d^2}}$$

$$m = \sqrt{\frac{b \times 4}{k \times d}}$$

$$m^2 = \frac{h \times 4}{k \times d}$$

$$h = \frac{m^2 \times k \times d}{4}$$

$$h = \frac{m^2 \times 15 \times (120 \times 10^{-3})}{4}$$

$$h = 0.045 \text{ m}^2$$

$$Q = \sqrt{h p \times A_c \cdot \theta_b \tanh(m)}$$

$$Q = \sqrt{(0.045 \text{ m}^2) \times (\pi \times 12 \times 10^{-3}) \times 15 \times \left(\frac{\pi (120 \times 10^{-3})^2}{4} \right)}$$

$$T = m (1.696 \times 10^{-3}) \times (250) \times \tanh(280-30) \times \tanh(m \times 0.08)$$

$$T = 0.4241 \text{ m} \tanh(0.08 \text{ m})$$

$$16.5044 = m \cdot \tanh(m \cdot 0.08)$$

$$m = 18.3531 \text{ m}$$

$$\text{Now, } h = (0.045) (18.353)^2$$

$$h = 18.157 \text{ W/m}^2\text{K}$$

Tip temp, At $\chi = 0.08$

$$\frac{T - T_{\infty}}{T_b - T_{\infty}} = \frac{\cosh h(m(L-x))}{\cosh hmL}$$

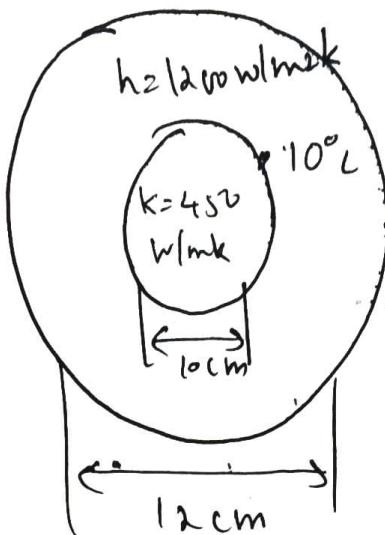
$$\frac{T - 30}{250} = \frac{\cosh h(18.353(0.08 - 0.03))}{\cosh h(18.353 \times 0.68)}$$

$$\frac{T - 30}{250} = \frac{\cosh h(18.353(0.08 - 0.03))}{\cosh h(18.353 \times 0.68)}$$

$$\frac{T - 30}{250} = \frac{1}{2.2859}$$

$$T = 139.36^\circ\text{C}$$

(3)



$$h = 1200 \text{ W/m}^2\text{K}$$

$$25^\circ\text{C}$$

$$\lambda_1 = 5 \text{ cm}$$

$$= 5 \times 10^{-2} \text{ m}$$

$$\lambda_2 = 12 \text{ cm} = 12 \times 10^{-2} \text{ m}$$

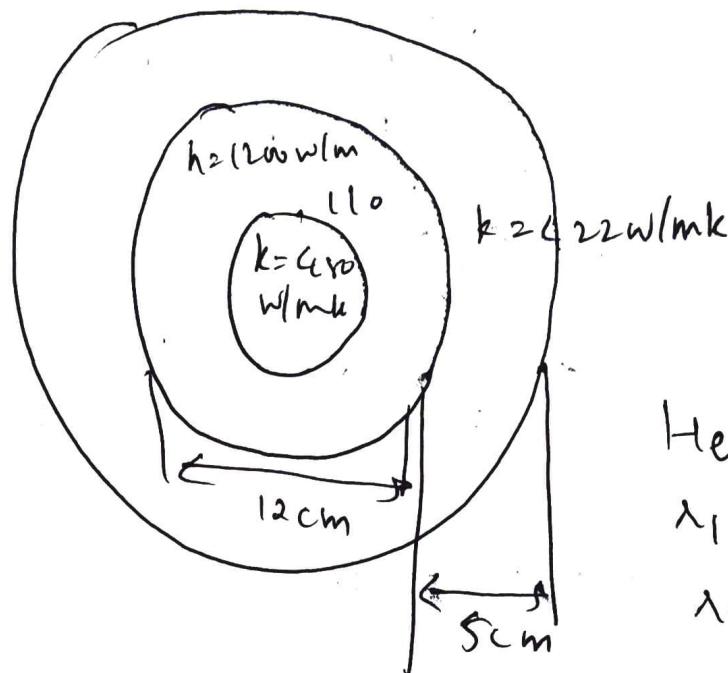
i) Q without insulation

$$\frac{Q_{\text{without}}}{l} = \frac{1}{1200 \times 2\pi(5 \times 10^{-2})} + \frac{\ln\left(\frac{6 \times 10^{-2}}{5 \times 10^{-2}}\right)}{2\pi \times 450} + \frac{1}{18 \times 2\pi \times 0.6 \times 10^{-2}}$$

$$\frac{Q_{\text{without}}}{l} = \frac{1}{1200 \times 2\pi \times 5 \times 10^{-2} \times 1200} + \frac{\ln\left(\frac{6 \times 10^{-2}}{5 \times 10^{-2}}\right)}{2\pi \times 450} + \frac{1}{18 \times 2\pi \times 0.6 \times 10^{-2}}$$

$$\frac{Q_{\text{without}}}{l} = 57.57 \text{ W/m}$$

ii) Without insulation



Here

$$\lambda_1 = 8 \text{ cm}$$

$$\lambda_2 = 6 \text{ cm}$$

$$\lambda_3 = 11 \text{ cm}$$

110

$$\frac{1}{120 \times 2 \pi \times 5 \times 10^{-2}} + \frac{\ln \left(\frac{6 \times 10^{-2}}{5 \times 10^{-2}} \right)}{2 \times \pi \times 4.5} + \frac{\ln \left(\frac{11 \times 10^{-2}}{6 \times 10^{-2}} \right)}{2 \times \pi \times 0.22} + \frac{1}{1 \times 2 \times \pi \times 10^{-2}}$$

$$\frac{Q_{\text{with}}}{l} = \frac{110 - 25}{120 \times 2 \pi \times 5 \times 10^{-2}}$$

$$\frac{1}{120 \times 2 \pi \times 5 \times 10^{-2}} + \frac{\ln \left(\frac{6 \times 10^{-2}}{5 \times 10^{-2}} \right)}{2 \times \pi \times 4.5} + \frac{\ln \left(\frac{11 \times 10^{-2}}{6 \times 10^{-2}} \right)}{2 \times \pi \times 0.22} + \frac{1}{1 \times 2 \times \pi \times 10^{-2}}$$

$$\frac{Q_{\text{with}}}{l} = 162.96 \text{ W/m}$$

∴ Increase in heat transfer

$$\frac{162.96 - 57.52}{57.52} \times 100$$

$$= 183.06\%$$