



**Missing Values: [ 2 Marks]** **Reasons for missing values**

- Information is not collected (e.g., people decline to give their age and weight)
- Attributes may not be applicable to all cases (e.g., annual income is not applicable to children)

 **Handling missing values**

- Eliminate Data Objects
- Estimate Missing Values
- Ignore the Missing Value During Analysis
- Replace with all possible values (weighted by their probabilities)

**Duplicate Data: [ 1 Mark]**

- Data set may include data objects that are duplicates, or almost duplicates of one another
- Major issue when merging data from heterogeneous sources
- Examples:  
Same person with multiple email addresses
- Data cleaning**  
Process of dealing with duplicate data issues

2a) Why data preprocessing is significant step data mining? Explain Discretization and Binarization techniques with example.

Data preprocessing makes the data suitable for data mining

It reduces noise, duplicates, processing time and memory requirements and removes unwanted data. [ 2 Marks]

**Binarization: [ 2 Marks]**

- **Binarization** maps a continuous or categorical attribute into one or more binary variables. Typically used for association analysis
- **Often convert a continuous attribute to a categorical attribute and then convert a categorical attribute to a set of binary attributes**
- Association analysis needs asymmetric binary attributes

**Table 2.5.** Conversion of a categorical attribute to three binary attributes.

| Categorical Value | Integer Value | $x_1$ | $x_2$ | $x_3$ |
|-------------------|---------------|-------|-------|-------|
| <i>awful</i>      | 0             | 0     | 0     | 0     |
| <i>poor</i>       | 1             | 0     | 0     | 1     |
| <i>OK</i>         | 2             | 0     | 1     | 0     |
| <i>good</i>       | 3             | 0     | 1     | 1     |
| <i>great</i>      | 4             | 1     | 0     | 0     |

**Table 2.6.** Conversion of a categorical attribute to five asymmetric binary attributes.

| Categorical Value | Integer Value | $x_1$ | $x_2$ | $x_3$ | $x_4$ | $x_5$ |
|-------------------|---------------|-------|-------|-------|-------|-------|
| <i>awful</i>      | 0             | 1     | 0     | 0     | 0     | 0     |
| <i>poor</i>       | 1             | 0     | 1     | 0     | 0     | 0     |
| <i>OK</i>         | 2             | 0     | 0     | 1     | 0     | 0     |
| <i>good</i>       | 3             | 0     | 0     | 0     | 1     | 0     |
| <i>great</i>      | 4             | 0     | 0     | 0     | 0     | 1     |

**Discretization[ 2 Marks]**

- Discretization is the process of converting a continuous attribute into an ordinal attribute
- Discretization is typically applied to attributes that are used in **classification**

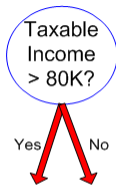
[2+4]

CO1

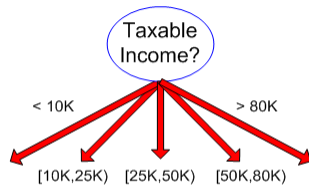
L2

**or association analysis.**

- Transformation of a continuous attribute to a categorical attribute involves two subtasks:
- deciding how many categories to have and determining how to map the values of the continuous attribute to these categories.**
- 



(i) Binary split



(ii) Multi-way split

2b) Compute the cosine similarity of the following two objects that represent two document vectors:

$$x = (2, -7, 0, 2, 0, -3), y = (-1, 1, -1, 0, 0, -1)$$

$$x \cdot y \quad - \quad [1 \text{ mark}]$$

$$|x| \quad - \quad [1 \text{ mark}]$$

$$|y| \quad - \quad [1 \text{ mark}]$$

$$\text{Cosine Similarity} = [1 \text{ mark}]$$

Compute cosine similarity:

$$x = (2, -7, 0, 2, 0, -3)$$

$$y = (-1, 1, -1, 0, 0, -1)$$

$$x \cdot y = (2 \times -1) + (-7 \times 1) + (0 \times -1) + (2 \times 0) + (0 \times 0) + (-3 \times -1) = -6.$$

$$|x| = \sqrt{(2 \times 2) + (-7 \times -7) + (0 \times 0) + (2 \times 2) + (0 \times 0) + (-3 \times -3)}$$

$$= \sqrt{4 + 49 + 4 + 9} = \sqrt{66} = 8.12$$

$$= 8.12$$

$$|y| = \sqrt{(-1 \times -1) + (1 \times 1) + (-1 \times -1) + 0 + 0 + (-1 \times -1)}$$

$$= \sqrt{1 + 1 + 1 + 1} = \sqrt{4} = 2.$$

$$|y| = 2.$$

$$\text{Cos}(x, y) = -6 / (8.12 \times 2) = -0.36 \text{ Ans.}$$

[4] CO1 L3

3 Write and Explain Apriori Algorithm for frequent itemset generation with example.  
**Algorithm with Explanation -[ 5 marks]**

- The algorithm initially makes a single pass over the data set to determine the support of each item. Upon completion of this step, the set of all frequent 1-itemsets,  $F_1$ , will be known (steps 1 and 2).
- Next, the algorithm will iteratively generate new candidate  $k$ -itemsets using the frequent  $(k - 1)$ -itemsets found in the previous iteration (step 5). Candidate generation is implemented using a function called apriori-gen, which is described in Section 6.2.3.

[5+5] CO3 L2

- To count the support of the candidates, the algorithm needs to make an additional pass over the data set (steps 6–10). The subset function is used to determine all the candidate itemsets in  $C_k$  that are contained in each transaction  $t$ . The implementation of this function is described in Section 6.2.4.
- After counting their supports, the algorithm eliminates all candidate itemsets whose support counts are less than  $minsup$  (step 12).
- The algorithm terminates when there are no new frequent itemsets generated, i.e.,  $F_k = \emptyset$  (step 13).

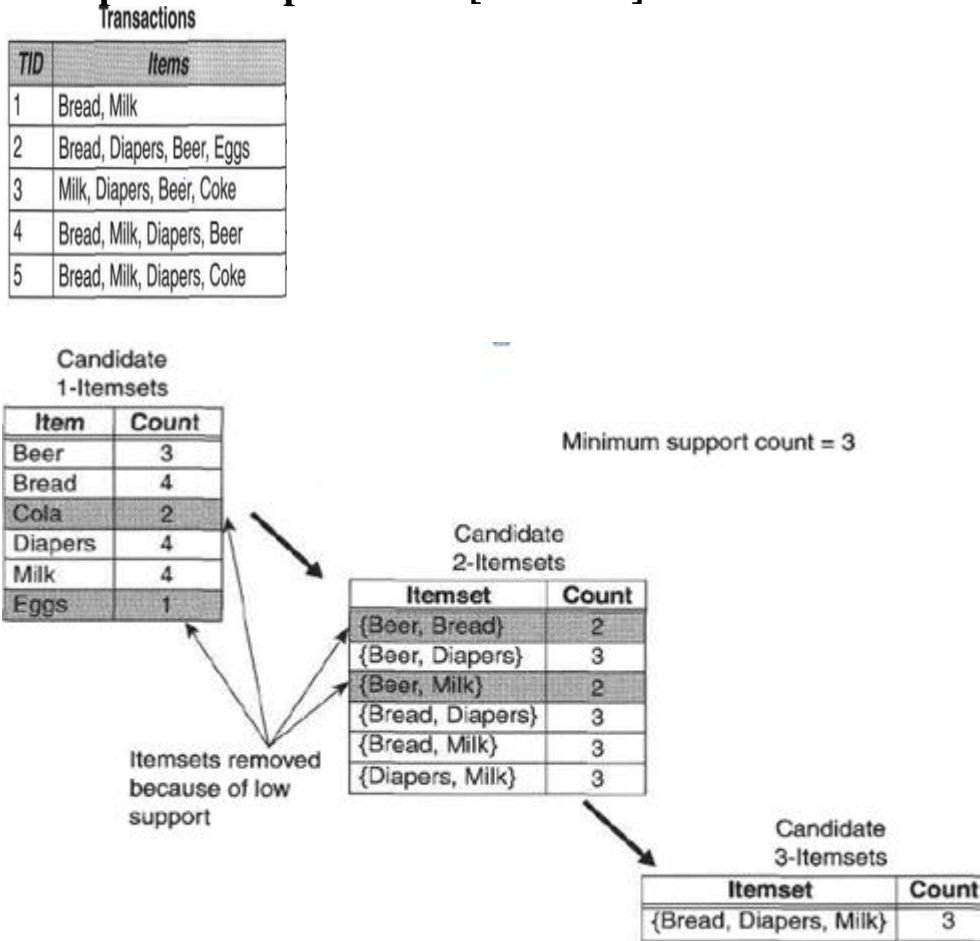
**Algorithm 6.1** Frequent itemset generation of the *Apriori* algorithm.

```

1:  $k = 1$ .
2:  $F_k = \{ i \mid i \in I \wedge \sigma(\{i\}) \geq N \times minsup \}$ . {Find all frequent 1-itemsets}
3: repeat
4:    $k = k + 1$ .
5:    $C_k = \text{apriori-gen}(F_{k-1})$ . {Generate candidate itemsets}
6:   for each transaction  $t \in T$  do
7:      $C_t = \text{subset}(C_k, t)$ . {Identify all candidates that belong to  $t$ }
8:     for each candidate itemset  $c \in C_t$  do
9:        $\sigma(c) = \sigma(c) + 1$ . {Increment support count}
10:    end for
11:  end for
12:   $F_k = \{ c \mid c \in C_k \wedge \sigma(c) \geq N \times minsup \}$ . {Extract the frequent  $k$ -itemsets}
13: until  $F_k = \emptyset$ 
14: Result =  $\bigcup F_k$ .

```

**Example with explanation- [ 5 marks]**



**Figure 6.5.** Illustration of frequent itemset generation using the *Apriori* algorithm.

4a) A database has five transactions. Let  $min\ sup=60\%$  and  $min\ conf =80\%$ .

|     |              |
|-----|--------------|
| TID | items bought |
|-----|--------------|

[8]

CO3

L3

|      |                    |
|------|--------------------|
| T100 | {M, O, N, K, E, Y} |
| T200 | {D, O, N, K, E, Y} |
| T300 | {M, A, K, E}       |
| T400 | {M, U, C, K, Y}    |
| T500 | {C, O, O, K, I, E} |

Find all frequent item sets using Apriori algorithm.

**Computation of C1 = 2 marks**

**Computation of F1 = 1 marks**

**Computation of C2 = 1 marks**

**Computation of F2 = 1 marks**

**Computation of C3 = 1 marks**

**Computation of F3 = 2 marks**

Given:

min.Supp = 60% Conf = 80%

Support =  $\frac{60}{100} \times 6 = 3$

Conf = 80%

Step 1: C1

| Item | Count |    |
|------|-------|----|
| A    | 1     | <3 |
| C    | 2     | <3 |
| D    | 1     | <3 |
| E    | 4     |    |
| I    | 1     | <3 |
| K    | 5     |    |
| M    | 3     | ✓  |
| N    | 2     | <3 |
| O    | 3     |    |
| U    | 1     | <3 |
| Y    | 3     |    |

| Item | Count |
|------|-------|
| E    | 4     |
| K    | 5     |
| M    | 3     |
| O    | 3     |
| Y    | 3     |

| Item | Count |    |
|------|-------|----|
| EI   | 4     |    |
| EM   | 2     | <3 |
| EO   | 3     |    |
| EY   | 2     | <3 |
| KM   | 3     |    |
| KO   | 3     |    |
| KY   | 3     |    |
| MO   | 1     | <3 |
| MY   | 2     | <3 |
| OY   | 2     | <3 |

| Item | Count |
|------|-------|
| EK   | 4     |
| EO   | 3     |
| KM   | 3     |
| KO   | 3     |
| KY   | 3     |

| Item | Count |    |
|------|-------|----|
| ERO  | 3     | ✓  |
| EKM  | 2     | <3 |
| EKY  | 2     | <3 |
| KMO  | 1     | <3 |
| KMY  | 2     | <3 |
| KOY  | 2     | <3 |

F3: {E, K, O} Ans

4b) What is anti-monotone property with respect to support of an itemset? Explain with example

[2]

CO3

L2

**Property: 1 mark**

**Example: 1 mark**

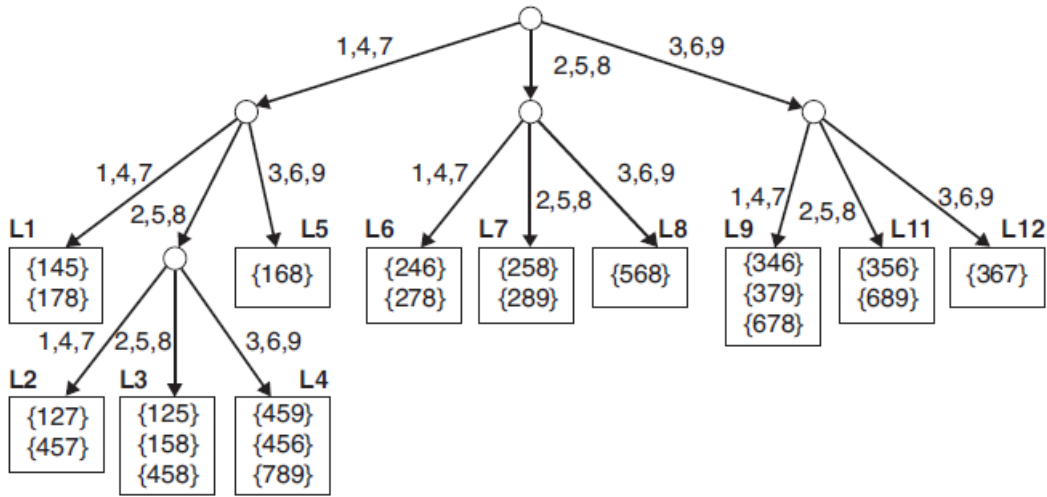
Apriori principle holds due to the following property of the support measure:

$$\forall X, Y : (X \subseteq Y) \Rightarrow s(X) \geq s(Y)$$

- Support of an itemset never exceeds the support of its subsets
- This is known as the **anti-monotone** property of support

Example:

Consider {a,b,c} itemset. Assume Support count (a,b,c)=5    support count(a,b)  $\geq$  Support count(a,b,c) Number of times a,b,c occurring in Transactions never exceeds Support count(a,b)

|   |   |      |     |    |
|---|---|------|-----|----|
| 5 | <p>Construct the Hash tree structure for the given set of candidate item sets. Given transaction {1, 3, 4, 5, 8}, which of the hash tree leaf nodes will be visited when finding the candidates of the transaction?</p> <p>{145}{178}{127}{457}{125}{158}{458}{459}{456}{789}{168}{246}{278}{258}{289}{568}{346}{379}{678}{356}{689}{367}</p> <p><b>Construction of Hash Tree: 5 marks</b></p>  <p>Given a transaction that contains items {1, 3, 4, 5, 8}, The leaf nodes visited are L1, L3, L5, L9, and L11 will be visited when finding the candidates of the transaction. <b>5 marks</b></p> | [10] | CO3 | L3 |
|---|---|------|-----|----|

|   |  |      |     |    |
|---|--|------|-----|----|
| 6 | <p>Explain the Apriori rule Generation algorithm with example</p> <p><b>Algorithm: 5 marks</b></p> <p><b>Example: 5 marks</b></p> <hr/> <p><b>Algorithm 6.2</b> Rule generation of the <i>Apriori</i> algorithm.</p> <ol style="list-style-type: none"> <li>1: for each frequent <math>k</math>-itemset <math>f_k, k \geq 2</math> do</li> <li>2: <math>H_1 = \{i \mid i \in f_k\}</math> {1-item consequents of the rule.}</li> <li>3: call ap-genrules(<math>f_k, H_1</math>.)</li> <li>4: end for</li> </ol> <hr/> <p><b>Algorithm 6.3</b> Procedure ap-genrules(<math>f_k, H_m</math>).</p> <ol style="list-style-type: none"> <li>1: <math>k =  f_k </math> {size of frequent itemset.}</li> <li>2: <math>m =  H_m </math> {size of rule consequent.}</li> <li>3: <b>if</b> <math>k &gt; m + 1</math> <b>then</b></li> <li>4: <math>H_{m+1} = \text{apriori-gen}(H_m)</math>.</li> <li>5: <b>for each</b> <math>h_{m+1} \in H_{m+1}</math> <b>do</b></li> <li>6: <math>\text{conf} = \sigma(f_k) / \sigma(f_k - h_{m+1})</math>.</li> <li>7: <b>if</b> <math>\text{conf} \geq \text{minconf}</math> <b>then</b></li> <li>8: <b>output</b> the rule <math>(f_k - h_{m+1}) \longrightarrow h_{m+1}</math>.</li> <li>9: <b>else</b></li> <li>10: <b>delete</b> <math>h_{m+1}</math> from <math>H_{m+1}</math>.</li> <li>11: <b>end if</b></li> <li>12: <b>end for</b></li> <li>13: <b>call</b> ap-genrules(<math>f_k, H_{m+1}</math>.)</li> <li>14: <b>end if</b></li> </ol> <hr/> | [10] | CO2 | L2 |
|---|--|------|-----|----|

Rule generation: Min conf = 50%

Assume  $k = 3$ .

$f_3 = \{B, C, E\}$  frequent item set.

Alg 6.2 produces

$H_1 = \{B\} \{C\} \{E\}$

Alg 6.3 ap-genrules

①  $k = |f_k| = 3$  ②  $m = |H_m| = 1$   
 $k = 3$ .

$\sigma(B, C, E) = 3$   
 $\sigma(E) = 5$   
 $\sigma(C) = 4$   
 $\sigma(B) = 5$ .

③  $3 > 2$

for  $H_{m+1} = H_2 = \text{ap-gen}(H_1)$

$H_2 = \{B, C\} \{B, E\} \{C, E\}$

④  $\text{Conf} = \frac{\sigma(BCE)}{\sigma(BCE - BC)} = \frac{3}{\sigma(E)} = \frac{3}{5} = 60\% > \text{min conf}$  (50%)  
 $\therefore E \rightarrow BC$  is valid rule. — ①

for  $(B, E)$   $\text{Conf} = \frac{\sigma(BCE)}{\sigma(BCE - BE)} = \frac{\sigma(BCE)}{\sigma(C)} = \frac{3}{4} = 75\% > \text{min conf}$  (50%)  
 $C \rightarrow BE$  is valid rule. — ②

for  $(CE)$   $\text{Conf} = \frac{\sigma(BCE)}{\sigma(BCE - CE)} = \frac{\sigma(BCE)}{\sigma(B)} = \frac{3}{5} = 60\% > \text{min conf}$  (50%)  
 $\therefore B \rightarrow CE$  is valid rule. — ③

Recursive call.  $f_k, H_{m+1}$   
 ap-genrules ( $\{B, C, E\}, \{\{BC\}, \{B, E\}, \{CE\}\}$ )

nd  
 2 call

$k = |f_k| = 3$   
 $m = |H_m| = 2$  (size of the rule consequent)

$3 > 3$   
 $k > 2 + 1$

false  
 End if.