

USN 

Internal Assessment Test III – DEC. 2020

Sub:	DESIGN OF RC STRUCTURAL ELEMENTS				Sub code:	17CV51	Branch:	CIVIL	
Date:	10/12/2020	Duration:	90 min's	Max marks:	50	Sem/sec:	5 TH SEM / A & B	OBE	
Note	Use of IS 456:2000 is permitted Assume any missing data suitably								
<u>Answer all the three full questions</u>							MARKS	CO	RBT
1 (a)	Design the longitudinal reinforcement for the beam of clear span 6m to support a design working live load of 12kN/m. Adopt M25 grade concrete and Fe 415 HYSD bars. Also Show the detailing of reinforcements.						[15]	CO 3	L3
2 (a)	Design a RC slab simply supported of 7m X 3m. Live load acting is 2kN/m ² and the floor finish is 0.6 kN/m ² . Use M20 grade concrete and Fe 415 grade steel.						[15]	CO 4	L3
3 (a)	Design a slab for a room of size 4m by 6m with discontinuous on all four sides and simply supported edges all the sides with corners prevented from lifting and supporting a service load of 4kN/m ² . Adopt M-20 grade and Fe-415 HYSD bars						[20]	CO 4	L3

① A Reinforced Concrete Beam 400mm x 700mm is simply supported over a clear span of 8m. It carries a UDL of 48 kN/m including its self weight. The section is reinforced with 6 bars of 20mm ϕ take effective cover of 40mm & use M20 concrete & Mild steel. Calculate the shear reinforcement required if

- Ⓐ only vertical stirrups are used
- Ⓑ Two bars are bent up @ 45 near each support.

Given data

- b = 400mm
- d = 700mm
- L = 8m
- ϕ = 20mm

$$A_s = 6 \times \frac{\pi}{4} \times 20^2 = \cancel{2613.57 \text{ mm}^2} \quad \underline{1884.955 \text{ mm}^2}$$

→ factored shear force

$$\begin{aligned} &= \text{UDL} \times 1.5 \\ &= 48 \times 1.5 \\ &= 72 \text{ kN/m} = 72 \times 10^3 \text{ N/m} \end{aligned}$$

$$\begin{aligned} \text{factored shear force} &= \cancel{V_d} \frac{K_l V_u l}{2} = \frac{72 \times 10^3 \times 8}{2} \\ &= \underline{288000 \text{ N}} \end{aligned}$$

→ Nominal shear force V_u

$$V_u = \frac{V_d}{bd} = \frac{45000}{400 \times 700}$$

$$V_u = \underline{0.16}$$

Ⓐ Calculation for area of steel:-

$$M_u = 0.87 \times f_y \times A_{st} \times d \left(1 - \frac{A_{st} \times f_y}{b \times d \times f_{ck}} \right)$$

$$109.89 \times 10^6 = 0.87 \times 415 \times A_{st} \times 450 \left(1 - \frac{A_{st} \times 415}{250 \times 450 \times 25} \right)$$

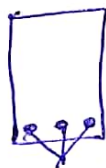
$$A_{st} = 762.05 \text{ mm}^2$$

The bar will be in the dia of 18, 20, 22mm

$$\text{No of bars} = \frac{A_{st}}{\frac{\pi d^2}{4}} = \frac{762.05}{\frac{\pi (20)^2}{4}} = 3 \text{ nos}$$

Provide 3 nos of 20mm dia bars.

$$\text{actual } A_{st} = \frac{3}{4} \times \pi d^2 = \frac{3}{4} \times \pi (20)^2 = 942.47 \text{ mm}^2$$



3 nos of 20mm ϕ .

$$\tau_v = \frac{V_u}{bd} = \frac{70.61}{250 \times 450} = 0.63 \text{ N/mm}^2$$

$$\tau_c = \frac{100 A_{st}}{b \cdot d} = \frac{100 (942.47)}{250 \times 450}, \tau_c = 0.837 \text{ N/mm}^2$$

$$\begin{array}{l} 0.75 \rightarrow 0.57 \\ 0.83 \rightarrow ? \\ 1 \rightarrow 0.64 \end{array} \quad \frac{0.57 \times 0.64}{0.57 \times x} = \frac{0.75 \times 1}{0.75 \times 0.33}$$

$$x = 0.53 = \tau_c$$

for stirrups provide 2-legged 8mm ϕ bars.

$$A_{sv} = 2 \times \frac{\pi}{4} \times d^2 = 2 \times \frac{\pi}{4} \times 8^2 = 100.53 \text{ mm}^2$$

$$V_u = (V_u - \tau_c b d) = \frac{0.87 \times f_y \times A_{sv} \times d}{s_v}$$

$$s_v = \frac{0.87 \times 415 \times 100.53 \times 450}{70.61 - 0.53 (250 \times 450)}$$

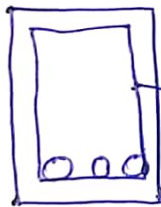
$$S_v = 1486.88 \text{ mm.}$$

$$S_v = 0.75 \times d.$$

$$= 0.75 \times 450.$$

$$S_v = 337.5 \text{ mm} \underline{\underline{=}}$$

hence provide 2-legged 8mm ϕ bars at 300 mm c/c.



→ 2-legged 8mm ϕ at 300 mm c/c

②

* Check for one way or two way slab:-

$$\frac{l_y}{l_x} = \frac{7}{3} = 2.33 > 2 \quad \therefore \text{one way slab.}$$

* Effective depth :-

$$20 = \frac{L}{d}, \quad d = \frac{3000}{20} = 150 \text{ mm.}$$

Assuming overall as = 145 mm

\therefore Assume effective cover as 25 mm.

$$d = 145 - 25 = 120 \text{ mm.}$$

* Design load (W_u):-

$$b = 1 \text{ m} = 1000 \text{ mm.}$$

$$\text{D.L} = 0.145 \times 1 \times 25 = 3.625 \text{ kN/m}$$

$$\text{LL} = 1 \times 2 = 2 \text{ kN/m.}$$

$$\text{F.F} = 1 \times 0.6 = 0.6 \text{ kN/m}$$

$$\text{Total load} = 6.225 \text{ kN/m.}$$

$$W_u = 6.225 \times 1.5 = 9.33 \text{ kN/m.}$$

* Effective Span:

$$\text{c/c distance} = \frac{0.23}{2} + 3 + \frac{0.23}{2} = 3.23 \text{ m.}$$

$$\text{clear span} + \text{Eff depth} = 3 + 0.12 = 3.12 \text{ m.}$$

$$\text{take least} = l = 3.12 \text{ m}$$

⊛ moments & shear :-

$$\text{factored moment} = \frac{wul^2}{8} = \frac{9.33 \times 3.12^2}{8} = 11.35 \text{ kNm}$$

$$\text{Shear force} = V_u = \frac{wl}{2} = \frac{9.33 \times 3.12}{2} = 14.55 \text{ kNm}$$

⊛ check for depth :-

$$d_{req} = \sqrt{\frac{M_u}{R_u \times b}} \quad \therefore R_u = 2.75$$

$$= \sqrt{\frac{11.35}{2.75 \times 1000}}$$

$$d_{req} = 64.24 \text{ mm} < \text{assuming under reinforced.}$$

\therefore hence OK.

⊛ Area of tension steel :-

$$M_u = 0.87 f_y A_{st} \left(1 - \frac{A_{st} \cdot f_y}{f_k \cdot b \cdot d}\right)$$

$$11.35 \times 10^6 = 0.87 \times 415 \times A_{st} \left[1 - \frac{A_{st} \times 415}{20 \times 1000 \times 120}\right]$$

$$11.35 \times 10^6 = 43326 A_{st} - 7.491 A_{st}^2, \quad \boxed{A_{st} = 275.04 \text{ mm}^2}$$

$$\text{Spacing at } \#10 \text{ mm} = \frac{\frac{\pi}{4} \times 10^2}{A_{st}} \times b = \frac{\frac{\pi}{4} \times 10^2}{275.04} \times 1000 = 285.55 \text{ mm}$$

\therefore provide 10ϕ @ 285.55 mm c/c.

⊛ Area of distribution bars :-

$$\text{Area} = 0.15\% \text{ BD} = \frac{0.15}{100} \times 1000 \times 145 = 217.5 \text{ mm}^2$$

$$\text{Spacing at } 8 \text{ mm } \phi = \frac{\frac{\pi}{4} \times 8^2}{217.5} \times 1000 = 231.1 \text{ mm}$$

\therefore provide 8ϕ @ 231.1 mm c/c.

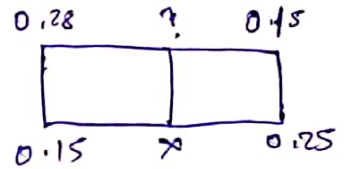
* check for shear :-

$$\tau_v = \frac{V_u}{bd} = \frac{14.55 \times 10^3}{1000 \times 120} = 0.121 \text{ KN/mm}^2$$

$$P_t = 100 \cdot \frac{A_{st}}{b \cdot d} = \frac{100 \times 275.04}{1000 \times 120} = 0.22$$

$\therefore \tau_c = 0.336$. from table 19. SP.16

\therefore The shear design is OK.



$$\frac{0.25 - 0.15}{0.36 - 0.28} = \frac{0.25 - 0.22}{0.36 - x}$$

$$0.036 - 0.1x = 0.0026$$

$$x = 0.336$$

③

Sol :- Given $LL = 4 \text{ KN/m}^2$

$f_{ck} = 20 \text{ N/mm}^2$, $f_y = 415 \text{ N/mm}^2$, assuming $FF = 1 \cdot \text{KN/m}$.

① $\frac{l_y}{l_x} = \frac{6}{4} = 1.5 < 2$ \therefore Two way slab.

② Assumption of $D = 160 + 15 + \frac{10}{2} = 150 \text{ mm}$.

eff depth along long span

$$d_y = d_x - \phi = 160 - 10 = 150 \text{ mm}$$

Effective span $l_x =$ least of following \therefore assuming bearing = 230

(i) $l_{x1} = \text{clear span} + \text{bearing} = 4 + 0.23 = 4.23 \text{ m}$

(ii) $l_{x2} = \text{clear span} + \text{eff depth} = 4 + 0.200 = 4.2 \text{ m}$

$l_x = 4.2 \text{ m} = x\text{-direction}$

$l_y = 6.2 \text{ m} = y\text{-direction}$

$$20.01 \times 10^6 = 5776 A_{st} - 7.481 \times A_{st}^2 = A_{st} = 363.52 \text{ mm}^2$$

$$\text{Spacing at } 8 \text{ mm } \phi = \frac{\pi/4 \times 8^2}{363.52} \times 1000 = 138.27 \text{ mm}$$

∴ provide #8 mm ϕ for 138 mm c/c

Check for A_{st} , $A_{st \text{ min}} = \frac{0.12}{100} \times b d = 192 \text{ mm}$.

∴ provide 8mm is at 138mm c/c

* Y-direction:- width of middle strip = $\frac{3}{4} \cdot l_x = 3.15 \text{ m}$

$$M_{wy} = 0.87 \times f_y \times A_{st} \times d \times \left(1 - \frac{A_{st} \times f_y}{f_k \times b d}\right)$$

$$12.59 \times 10^6 = 57768 A_{st} - 7.491 A_{st}^2$$

$$A_{st} = 224.47 \text{ mm}^2$$

$$\text{Spacing @ } 8 \text{ mm } \phi = \frac{1000 \times 503}{138} = 364.49 \text{ mm}$$

* Check for spacing shear:-

$$\tau_v = \frac{V_u}{b \cdot d} = \frac{26.77 \times 10^3}{1000 \times 180} = 0.167 \text{ N/mm}^2$$

$$p_t = \frac{100 A_{st}}{b \cdot d} = 0.22 \text{ } \therefore \tau_c = 0.33 \text{ N/mm}^2$$

from clause 40.2.1.1, $\tau_c = 0.33 \times K_t$, $K_t = 1.24$.

$$\therefore \tau_c = 0.33 \times 1.24 = \tau_c = 0.41 \text{ N/mm}^2$$

* Torsional reinforcement at corner:-

$$\text{mesh size} = \frac{l_x}{5} = \frac{4.02}{5} = 0.84 = 840 \text{ mm}$$

$$\text{Area of torsional reinforcement} = \frac{3}{4} \times 364 = 273 \text{ mm}^2$$

$$\text{using } 8 \text{ mm } \phi \text{ bars} = \frac{\pi}{4} \times 8^2 = 503 \text{ mm}^2$$

$$\text{Spacing} = 1000 \times \frac{503}{273} = 184.24 \text{ mm}$$

∴ provide 8mm mesh @ 184 mm c/c.