

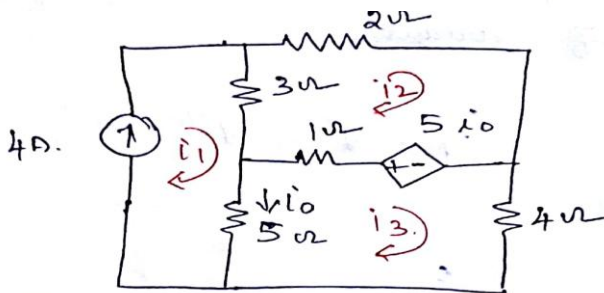
Sub:	Electric Circuit Analysis	Code:	18EE32
Date:	12/10/2019	Duration:	90 mins
		Max Marks:	50
		Sem:	3
		Branch:	EEE
Solutions			

Marks	OBE	
	CO	RBT

1 [10] CO3 L4

Use superposition theorem to find I_x of the network shown in fig1.

(i) Consider 4A, short circuit 20V.



$$I_1 = 4 \text{ A.}$$

KVL for Loop 2

$$2i_2 + 3(i_2 - i_1) + 1(i_2 - i_3) = 5i_0$$

$$i_1 - i_3 = i_0$$

$$-3i_1 + 6i_2 - i_3 = 5i_0 \quad \text{--- (1)}$$

$$i_1 - i_3 = i_0$$

$$4 - i_3 = i_0$$

$$i_3 = 4 - i_0 \quad ; \quad i_1 = 4 \text{ A}$$

Sub in (1).

$$-3 \times 4 + 6i_2 - (4 - i_0) = 5i_0$$

$$-12 + 6i_2 - 4 + i_0 = 5i_0$$

$$6i_2 - 16 = 4i_0$$

$$3i_2 - 2i_0 = 8 \quad \text{--- (2)}$$

KVL for Loop 3.

$$5(i_3 - i_1) + 1(i_3 - i_2) + 4i_3 = -5i_0 \quad \text{--- (3)}$$

$$i_1 = 4A; \quad i_3 = 4 - i_0.$$

$$5(i_3 - 4) + 1(i_3 - i_2) + 4i_3 = -5i_0.$$

$$10i_3 - 20 + i_2 = -5i_0.$$

$$i_3 = 4 - i_0$$

$$10(4 - i_0) - 20 + i_2 = -5i_0$$

$$40 - 10i_0 - 20 + i_2 = -5i_0$$

$$-i_2 - 5i_0 = -20 \quad \text{--- (4)} \quad \boxed{i_2 + 5i_0 = 20} \quad \text{--- (4)}$$

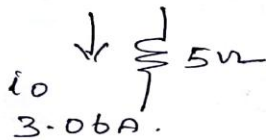
Solve (3) & (4)

$$(2) \Rightarrow 3i_2 - 2i_0 = 16$$

$$(4) \times 3 \Rightarrow 3i_2 + 15i_0 = 60$$

$$\underline{-17i_0 = -44}$$

$$\boxed{i_0 = 3.06A}$$

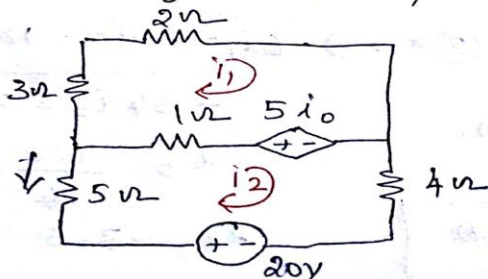


$$\boxed{i_0' = 3.06A}$$

$$i_0 = 3.384A$$

$$i_0 = \frac{52}{17}$$

(ii) Using 20V, Replace 4A.



$$i_0 = -i_2.$$

KVL for Loop 1

$$2i_1 + 3i_1 + 1(i_1 - i_2) = 5i_0.$$

$$6i_1 - i_2 = 5i_0$$

$$6i_1 + i_0 = 5i_0$$

$$6i_1 - 4i_0 = 0 \quad \text{--- (1)}$$

KVL for Loop 2

$$1(i_2 - i_1) + 5i_2 + 4i_2 = 20 - 5i_0.$$

$$10i_2 - i_1 = 20 - 5i_0.$$

$$i_2 = -i_0$$

$$-10i_0 - i_1 = 20 - 5i_0$$

$$-i_1 + 5i_0 = 20 \quad \text{--- (2)}$$

$$\boxed{i_0 = -3.53 \text{ A}}$$

$$\text{(1)} \Rightarrow 6i_1 - 4i_0 = 0.$$

$$\text{(2)} \times 6 \Rightarrow -6i_1 - 30i_0 = 120$$

$$-34i_0 = 120$$

$$i_0 = \frac{120}{-34}$$

$$i_0 = -3.53 \text{ A}$$



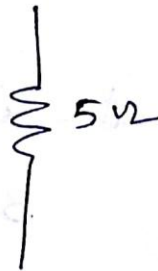
$$\boxed{i_0'' = -3.53 \text{ A}}$$

(ii) Algebraic sum.

Using 4A.

$$\downarrow i_0'$$

$$3.06 \text{ A}$$



Using 20V

$$\downarrow i_0''$$

$$-3.53 \text{ A}$$

$$i_0 = i_0' + i_0''$$

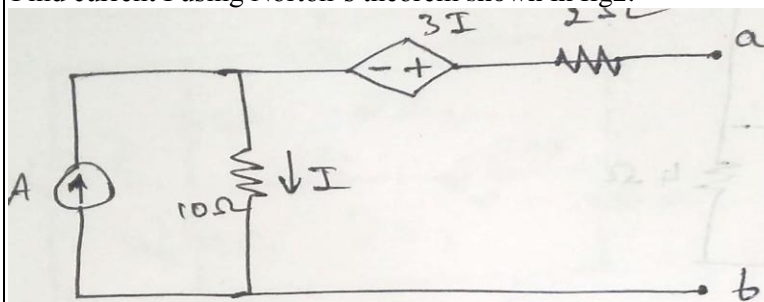
$$= 3.06 - 3.53$$

$$\boxed{i_0 = -0.47 \text{ A}}$$

2

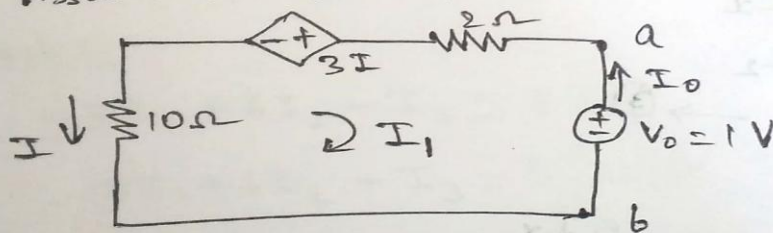
Find current I using Norton's theorem shown in fig2.

[10] CO3 L4



To find R_{th}

Replace current source with open circuit
Assume voltage $V_0 = 1V$



$$I = -I_1$$

$$I_0 = -I_1$$

$$0 I_1 + 2 I_1 = 3 I - 1$$

$$12 I_1 = -3 I - 1$$

$$15 I_1 = -1$$

$$I_1 = -1/15 \text{ A}$$

$$I_0 = -I_1$$

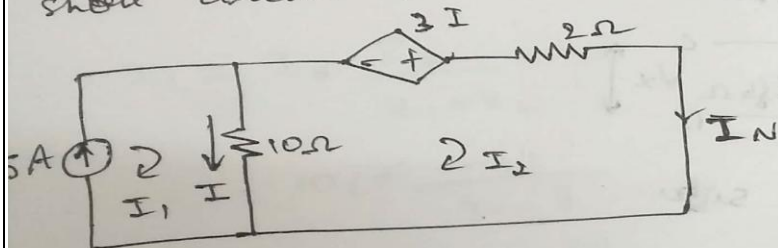
$$= \frac{1}{15} \text{ A}$$

$$R_{th} = \frac{V_0}{I_0} = \frac{1}{1/15} = 15 \Omega$$

$$R_{th} = 15 \Omega$$

To find I_N

short circuit the load resistor



$$I = I_1 - I_2$$

Mesh 1

$$I_1 = 5 \text{ A}$$

Mesh 2

$$-10I_1 + 12I_2 = 3I$$

$$-10I_1 + 12I_2 = 3(I_1 - I_2)$$

$$15I_2 = 13I_1$$

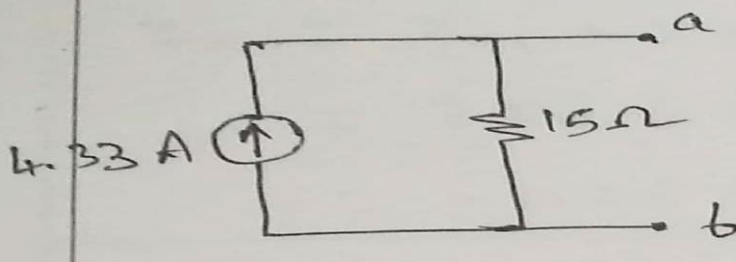
$$I_2 = \frac{65}{15}$$

$$I_N = I_2 = 4.333 \text{ A}$$

$$I = I_1 - I_2 = 5 - 4.333$$

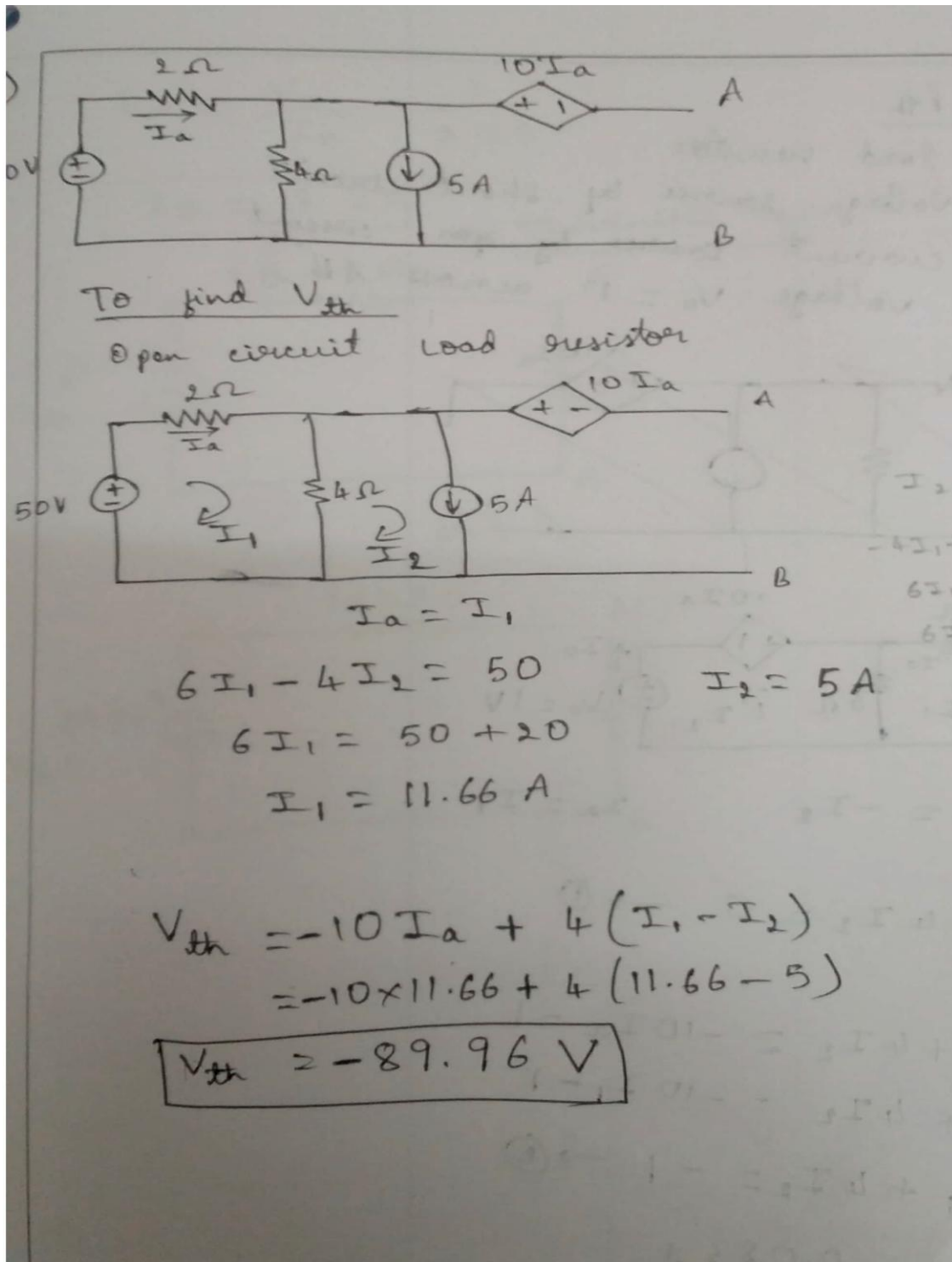
$$I = 0.666 \text{ A}$$

Norton's Eq. circuit



3 Find Thevenin's equivalent circuit across the terminal A-B of the network shown in fig3.

[10] CO3 L4



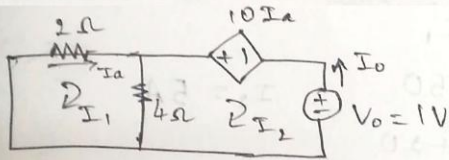
To find R_{th}

Remove load resistor

Replace voltage source by short circuit

current source by open circuit

Assume voltage $V_o = 1$ across AB



$$I_o = -I_2$$

$$I_a = I_1$$

esh 1

$$6I_1 - 4I_2 = 0 \rightarrow \textcircled{1}$$

esh 2

$$-4I_1 + 4I_2 = -10I_a - 1$$

$$-4I_1 + 4I_2 = -10I_1 - 1$$

$$6I_1 + 4I_2 = -1 \rightarrow \textcircled{2}$$

$$I_1 = -0.083 \text{ A}$$

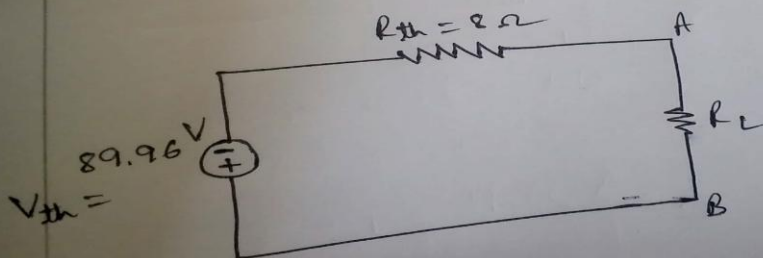
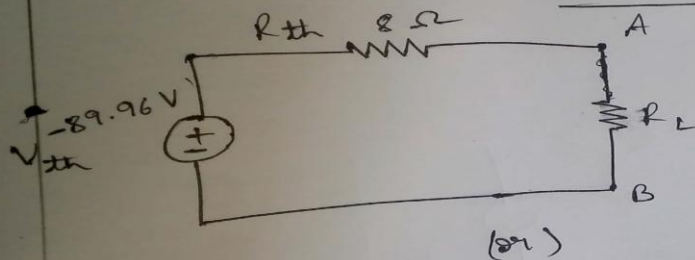
$$I_2 = -0.125 \text{ A}$$

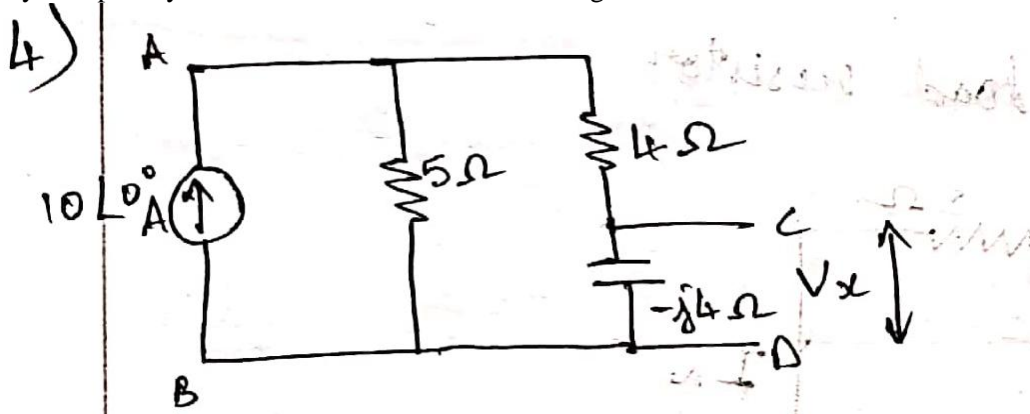
$$I_o = -I_2 = 0.125 \text{ A}$$

$$R_{th} = \frac{V_o}{I_o} = \frac{1}{0.125}$$

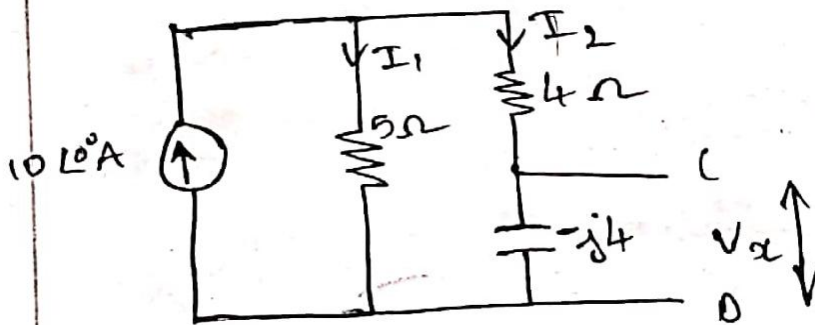
$$R_{th} = 8 \Omega$$

Thevenin's equivalent circuit





case i) considering AB side



$$I_2 = 10 \angle 0^\circ \frac{5}{9 - j4}$$

$$= 10 \angle 0^\circ \frac{5 \angle 0^\circ}{9.84 \angle -23.96}$$

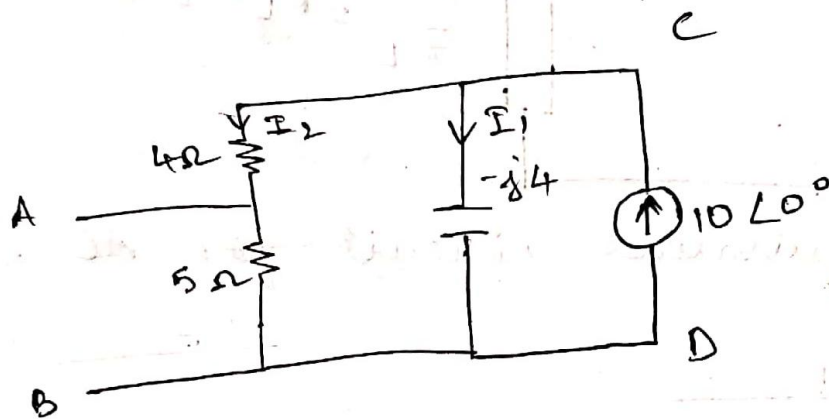
$$= 5.08 \angle 23.96 \text{ A}$$

$$V_x = -j4 (5.08 \angle 23.96)$$

$$= 4 \angle -90 \cdot (5.08 \angle 23.96)$$

$$V_{CD} = V_x = 20.32 \angle -66.04 \text{ V}$$

case ii) considering CD source



$$I_2 = I \cdot \frac{Z_1}{Z_1 + Z_2}$$

$$= 10 \angle 0^\circ \frac{-j4}{9 - j4}$$

$$= 10 \angle 0^\circ \left(\frac{4 \angle -90}{9.84 \angle -23.96} \right)$$

$$I_2 = 4.065 \angle -66.04 \text{ A}$$

$$V_{AB} = V_x = 5 (4.065 \angle -66.04)$$

$$V_{AB} = 20.32 \angle -66.04 \text{ V}$$

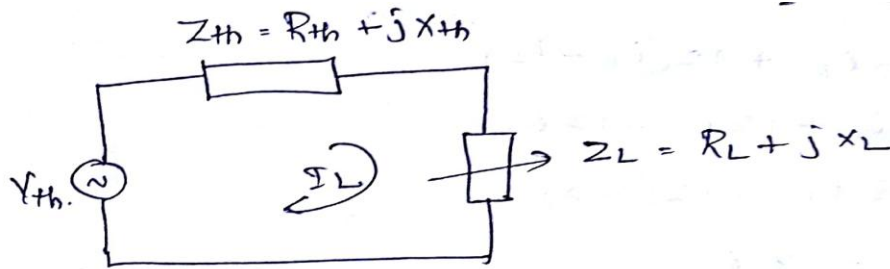
From case (i) & (ii)

$$V_{AB} = V_{CD} = 20.32 \angle -66.04 \text{ V}$$

5a

Obtain the condition for an alternating voltage source to transfer maximum power to the load when the load impedance is the complex conjugate of the source impedance.

[5] CO3L3



$$I_L = \frac{V_{th}}{Z_{th} + Z_L} = \frac{V_{th}}{(R_{th} + jX_{th}) + (R_L + jX_L)}$$

$$I_L = \frac{V_{th}}{(R_{th} + R_L) + j(X_{th} + X_L)}$$

$$\frac{dP_L}{dX_L} = 0 \quad (V) - 2((R_{th} + R_L) + 2j(X_{th} + X_L)) \frac{V_{th}^2 R_L}{R_{th} + R_L} = 0$$

$$2j(X_{th} + X_L) = 0$$

$$-X_{th} = X_L$$

$$X_L = -X_{th}$$

$$Z_L = R_L + jX_L$$

$$Z_L = R_{th} - jX_{th} = Z_{th}^*$$

$$\frac{dP_L}{dR_L} = 0 ; X_L = -X_{th}$$

$$\frac{d}{dR_L} P_L = \frac{V_{th}^2 (R_{th} + R_L)^2}{2(R_{th} + R_L) R_L} = 0$$

$$R_L = R_{th} \quad (R_{th} + R_L)^2 = 2(R_{th} + R_L) R_L$$

$$R_{th} + R_L = 2R_L$$

$$R_{th} = R_L$$

Maximum Power will be transferred from source to load in AC circuits, when load impedance is complex conjugate of Thevenin's impedance.

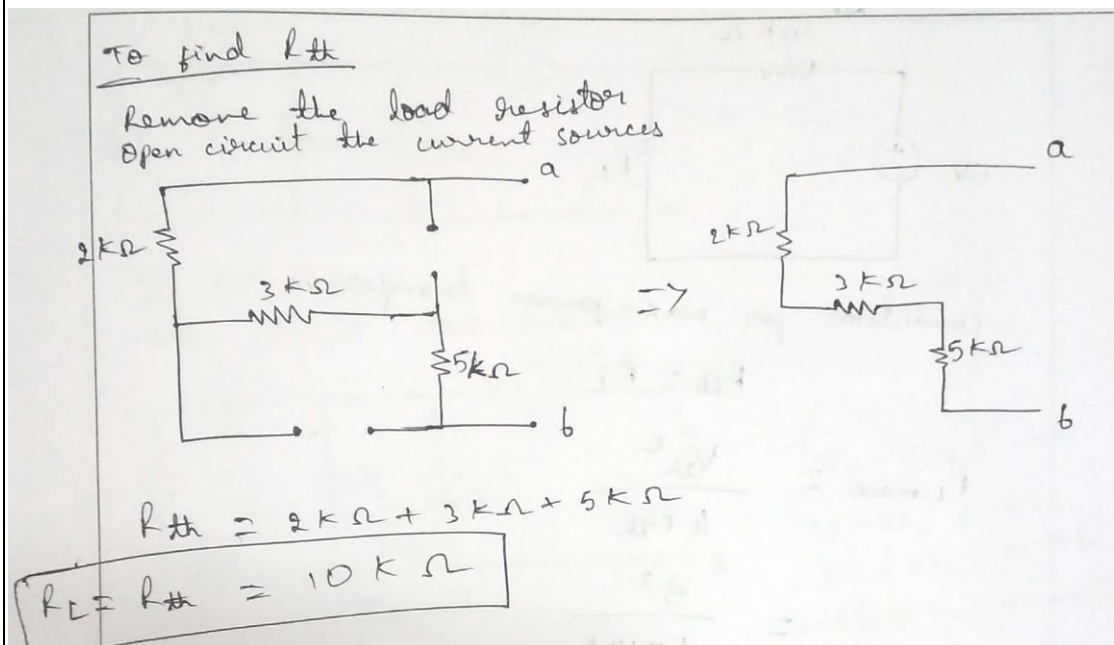
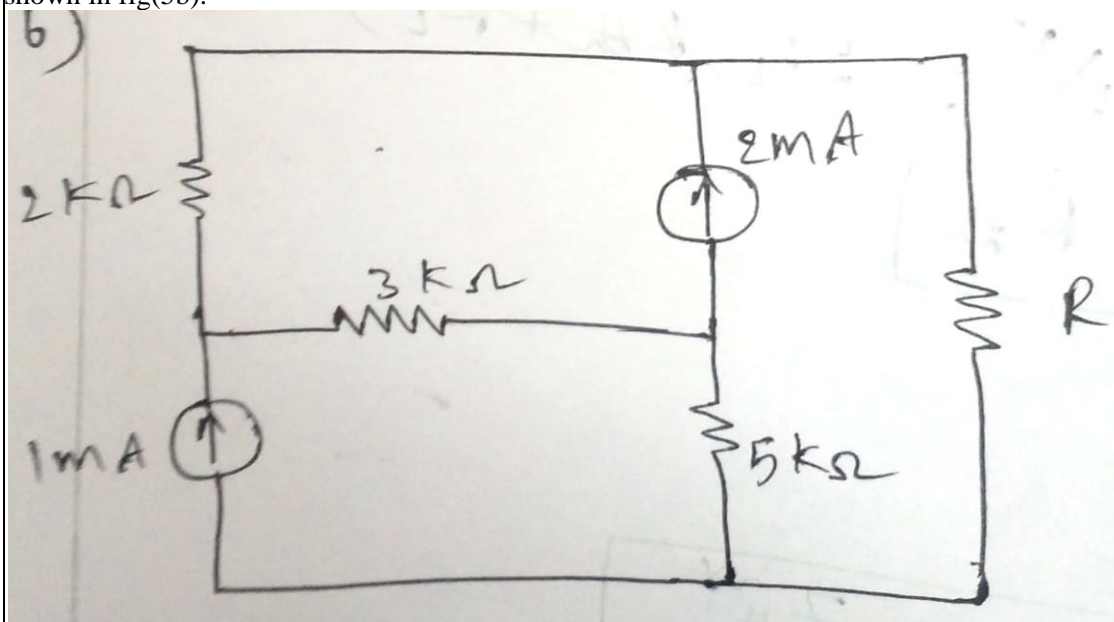
$$Z_L = Z_{th}^*$$

5b

Find the value of load resistance R when maximum power is transfer across it in the network shown in fig(5b).

[5]

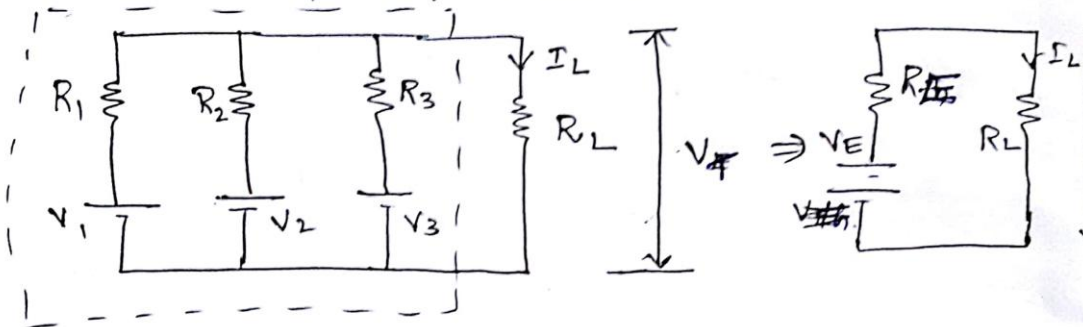
CO3L3



Millman's Theorem

- * It is otherwise called as "Parallel Generator Theorem".
- * This is combination of Norton's theorem and Thevenin's theorem.

Circuit with Voltage Sources.



- * V_1, V_2, V_3 are voltages of 1st, 2nd + 3rd branch
- * R_1, R_2, R_3 are respective resistances.
- * $I_L, R_L, V_T \rightarrow$ Load current, load resistance and Terminal voltage.
- * This can be converted into single voltage source and resistance.

where $V_{th}^E =$ Equivalent voltage \Rightarrow Thevenin's voltage

$$V_{th}^E = \frac{\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3}}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} = \frac{\sum \frac{V}{R}}{\sum \frac{1}{R}}$$

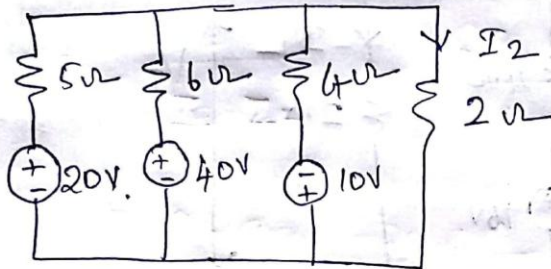
$R_{th} \Rightarrow$ Thevenin's resistance

$$R_{th} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$$

Load current $I_L = \frac{V_{th}}{R_{th} + R_L}$

Terminal Voltage $V_T = I_L R_L$

6b. Determine the current I by applying Millman's theorem shown in fig(6b).



$$R_E = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} = \frac{1}{\frac{1}{5} + \frac{1}{6} + \frac{1}{4}} = \frac{1}{0.2 + 0.167 + 0.25}$$

$$R_E = 1.62 \Omega$$

$$V_E = \frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} = \frac{20}{5} + \frac{40}{6} - \frac{10}{4}$$

$$= \frac{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}{\frac{1}{5} + \frac{1}{6} + \frac{1}{4}}$$

$$= \frac{4 + 6.67 - 2.5}{0.617}$$

$$V_E = 13.24 \text{ V}$$

$$I_2 = I_L = \frac{V_E}{R_E + R_L}$$

$$I_2 = \frac{13.24}{1.62 + 2} = 3.66 \text{ A}$$

$$I_2 = 3.66 \text{ A}$$

