

Re-modified  
13/11/2020

# CBCS SCHEME

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18EE32

## Third Semester B.E. Degree Examination, Dec.2019/Jan.2020 Electric Circuit Analysis

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

### Module-1

- 1 a. Setup nodal equations for the circuit of Fig.Q1(a) and then find the power supplied by 5 – V source.

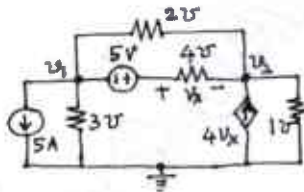


Fig.Q1(a)

(08 Marks)

- b. Making use of source shifting procedure, simplify the circuit of Fig.Q1(b) in such a way that the voltage  $V_X$  is determined.

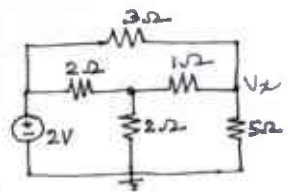


Fig.Q1(b)

(06 Marks)

- c. Use mesh analysis to determine the branch currents in the network indicated in Fig.Q1(c).

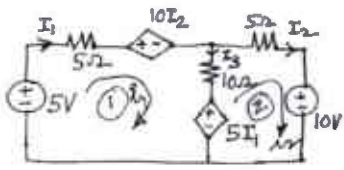


Fig.Q1(c)

(06 Marks)

### OR

- 2 a. Find 'Req' for the network shown in Fig.Q2(a) across A and B.

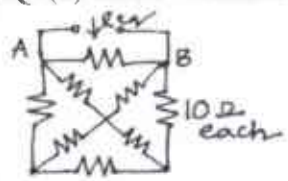


Fig.Q2(a)

(06 Marks)

- b. Draw the exact dual of the network shown in Fig.Q2(b) by writing Kirchhoff's law equations.

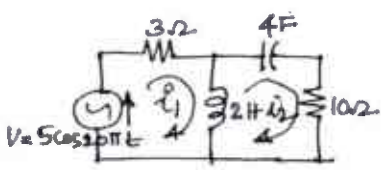


Fig.Q2(b)

(08 Marks)

- c. Reduce the network of Fig.Q2(c) to a form with only one current source across terminals using source transformation (terminals A and B).

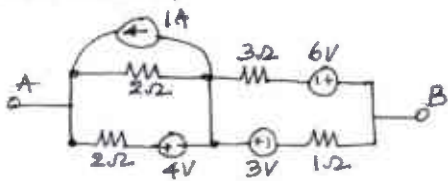


Fig.Q2(c)

(06 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any revealing of identification, appeal to evaluator and /or equations written eg. 42+8 = 50, will be treated as malpractice.

**Module-2**

- 3 a. Find the Thevenin's equivalent circuit at the terminals A and B of the circuit in Fig.Q3(a).

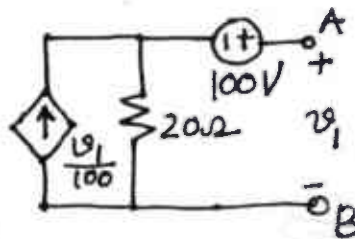


Fig.Q3(a)

(08 Marks)

- b. Find the value of  $R_L$  in the network shown in Fig.Q3(b) that will absorb a maximum power and specify the value of that power.

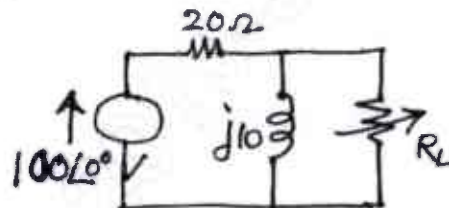


Fig.Q3(b)

(06 Marks)

- c. In the network shown in Fig.Q3(c) the voltage source of 5V causes a current I in the 2Ω resistor. Find 'I'. Verify the reciprocity theorem.

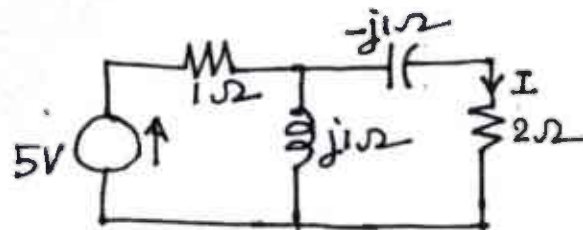


Fig.Q3(c)

(06 Marks)

OR

- 4 a. In the network shown in Fig.Q4(a) determine the nodal voltage  $V_2$  using superposition theorem.

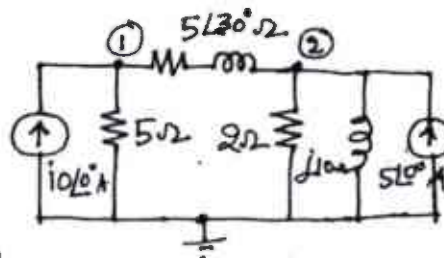


Fig.Q4(a)

(08 Marks)

- b. Use Thevenin's theorem to find current in  $R_L = 6\Omega$  in Fig.Q4(b).

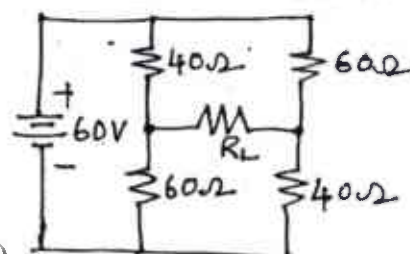


Fig.4(b)

(08 Marks)

- c. State and prove Millman's theorem.

(04 Marks)

**Module-3**

- 5 a. Derive an expression for resonant frequency ' $f_0$ ' for the general parallel resonant circuit show in Fig.Q5(a).

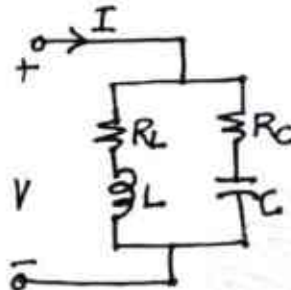


Fig.Q5(a)

(08 Marks)

- b. Fig.Q5(b) shows a network with zero capacitor voltage and zero inductor current when the switch 'K' is open. At  $t = 0$  the switch 'K' is closed. Solve for :

- i)  $V_1$  and  $V_2$  at  $t = 0^+$
- ii)  $\frac{dv_1}{dt}$  and  $\frac{dv_2}{dt}$  and  $t = 0^+$
- iii)  $V_1$  and  $V_2$  at  $t = \infty$

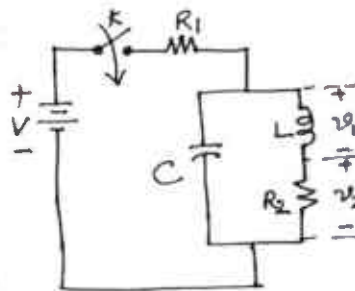


Fig. Q5(b)

(12 Marks)

**OR**

- 6 a. Fig.Q6(a) shows a RCL parallel circuit excited by a DC current source. At  $t = 0$ , the switch K is opened. Find  $v(t)$ .

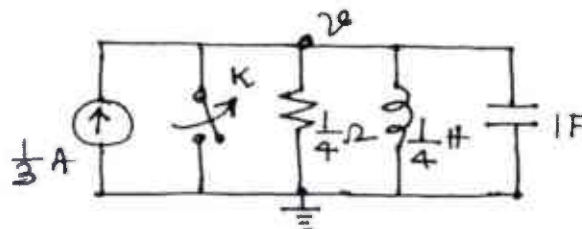


Fig.Q6(a)

(08 Marks)

- b. A 400V, 200Hz AC source is connected in series with a capacitor and a coil whose resistance and inductance are 20m $\Omega$  and 6mH respectively. If the circuit is in resonance at 200Hz, find :
- i) Value of capacitor
  - ii)  $V_g$  A/C the capacitor
  - iii) Maximum energy stored (instantaneous) in the coil
- c. iv) The half - power frequencies.

(08 Marks)

What are initial conditions in network? Write the equivalent form of the network elements interms of the initial conditions.

(04 Marks)

**Module-4**

- 7 a. Find the Laplace transform of the square wave shown in Fig.Q7(a).

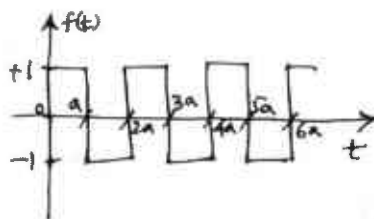


Fig.Q7(a)

(08 Marks)

- b. Fig.Q7(b) shows a series R-L-C circuit excited by a voltage  $v(t) = 12 \sin 5t$ . The initial current in the circuit is 5A and the initial voltage a/c capacitor is one volt with polarity shown. Find  $i(t)$  using Laplace transformation method.

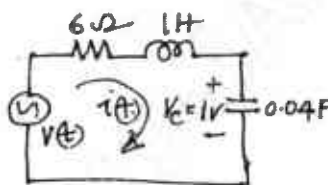


Fig.Q7(b)

(08 Marks)

- c. State and prove the initial-value theorem in the context of Laplace transformation. (04 Marks)

**OR**

- 8 a. A rectangular voltage pulse of unit height and duration 'T' is applied to a series R-C combination at  $t = 0$ . Determine the voltage across the capacitance 'C' as a function of time. Use Laplace transformation method. (10 Marks)
- b. Find the Laplace transforms of the two different functions given below and sketch the waveforms. i)  $\sin(\omega t) u(t - t_0)$  ii)  $\sin \omega(t - t_0) u(t - t_0)$ . (10 Marks)

**Module-5**

- 9 a. A symmetrical 3 -  $\phi$ , 100V, 3-wire supply feeds an unbalanced star-connected load with impedances of the load as  $Z_R = 5 \angle 0^\circ \Omega$ ,  $Z_Y = 2 \angle 90^\circ \Omega$  and  $Z_B = 4 \angle -90^\circ \Omega$ . Find the line currents, voltage across the impedances and the displacement natural voltage. Also calculate the power consumed by the load. Draw the phasor diagram sequence RYB. Take  $V_{RY}$  as ref. (10 Marks)
- b. For the circuit of Fig.9(b) find Z-parameters. Hence calculate transmission (ABCD) parameters. Find whether the network is symmetrical? Reciprocal?

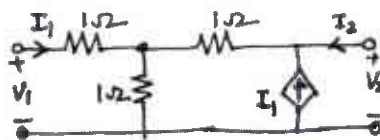


Fig.Q9(b)

(10 Marks)

**OR**

- 10 a. A 3- $\phi$  delta connected load has  $Z_{RY} = (100 + j50)\Omega$ ,  $Z_{YB} = (20 - j75)\Omega$  and  $Z_{BR} = (70.7 + j70.7)\Omega$  and it is connected to balanced 3 -  $\phi$ , 400V supply. Determine the line currents, power consumed by the load. Sketch the phasor diagram. Assume RYB phase sequence and take  $V_{YB}$  as the reference phasor. (10 Marks)
- b. For the circuit shown in Fig.Q10(b) find Y-parameters. Is the network symmetrical? Reciprocal?

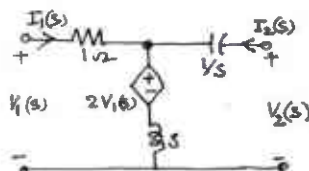


Fig.10(b)

(10 Marks)

**Modification in Scheme and solutions in subjects Electrical Circuit Analysis**

message

fr. **A.Manjunath** <manjuprinci@gmail.com>  
to: pmanjunath p <pmanjunathvtu@gmail.com>

Mon, Jan 13, 2020 at 1:12 PM

Good Morning

The modifications in Scheme and solutions of subjects 18EE32 Electrical Circuit Analysis

Q.no.5b. Full marks may be awarded for steps with wrong solution.

Q.no.6a. Full marks may be awarded for steps with wrong solution.

Q.no.7b. Full marks may be awarded for steps with wrong solution.

Dr.A.Manjuantha  
Chairman BOE,EEE

APPROVED

 13/1/2020

Registrar (Evaluation)  
Visvesvaraya Technological University  
BELAGAVI - 18



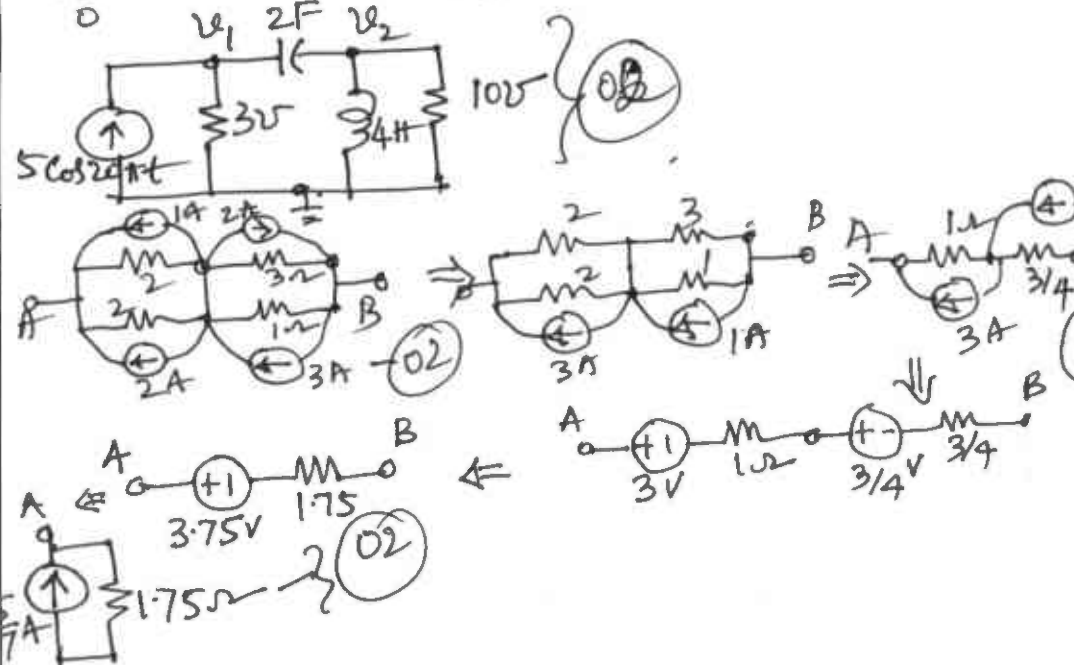
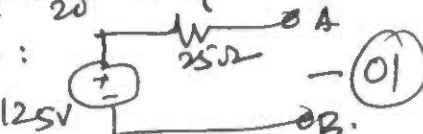
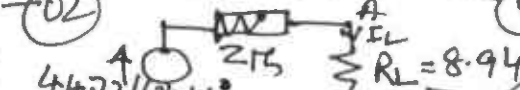
Scheme & Solution

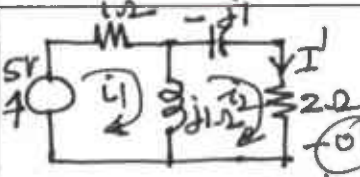
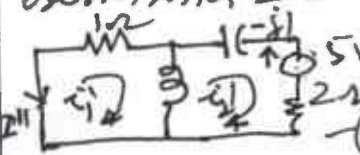
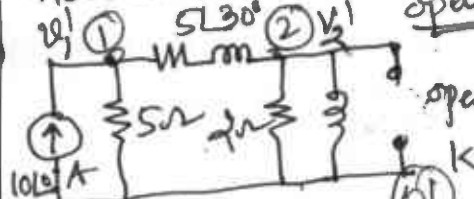
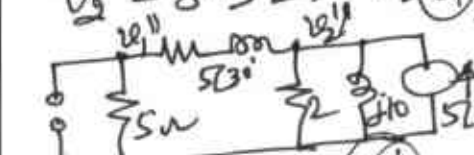
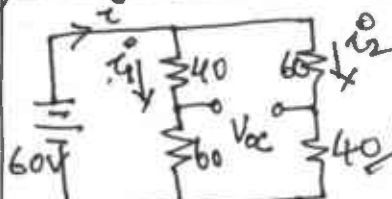
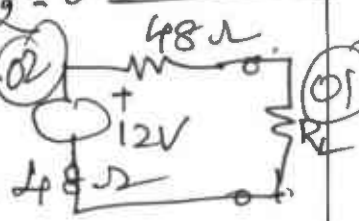
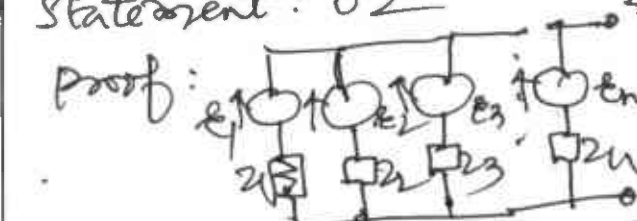
Signature of Scrutinizer

Subject Title : Electric circuit Analysis

Subject Code : 18EE32

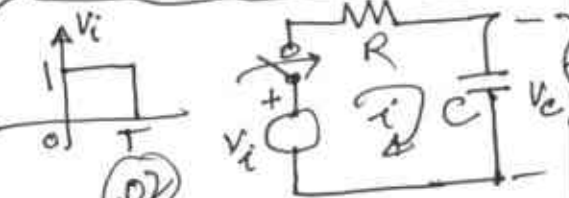
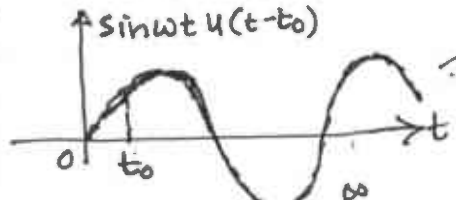
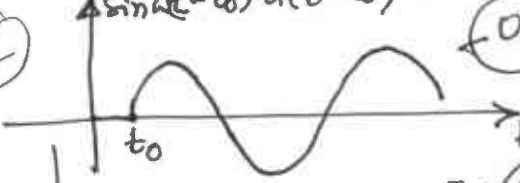
Question Number	Solution	Marks Allocated
Q1 a	<p>KCL at node ① : <math>9V_1 - 6V_2 = -25</math>            KCL at node ② : <math>-10V_1 + 11V_2 = 40</math>  <math>V_1 = -0.8974V</math> ; <math>V_2 = 2.8205V</math>            Power supplied <math>= P_{5V} = 5 \times 4 \times 1.282</math>  <math>P_{5V} = 25.6W</math></p> <p><math>P_{5V} = 5 \times (V_x/4)</math>            where <math>V_x = V_1 + 5 - V_2</math>  <math>V_x = 1.282V</math></p> <p>(b) </p> <p><math>\therefore V_x = 5I_x = 5 \times 7/31 = 1.129V</math></p>	02 08 06
Q2 a	<p>Loop ① : <math>5I_1 + 10I_2 + 10(I_1 - I_2) + 5I_1 - 5 = 0</math>  <math>5I_1 + 10I_2 + 10I_1 - 10I_2 + 5I_1 - 5 = 0</math>  <math>20I_1 = 5 \therefore I_1 = 0.25A</math></p> <p>Loop ② : <math>5I_2 + 10 - 5I_1 + 10(I_2 - I_1) = 0</math>  <math>5I_2 + 10 - 5I_1 + 10I_2 - 10I_1 = 0</math>  <math>-15I_1 + 15I_2 = -10 \therefore I_2 = -0.4667A</math></p> <p>Since <math>I_2 = I_2</math> &amp; <math>I_1 = I_1</math>  <math>I_1 = 0.25A</math>  <math>I_2 = -0.4667A</math>  <math>I_3 = 0.6667A</math></p> <p>Converting DBC to star  </p>	02 06 06

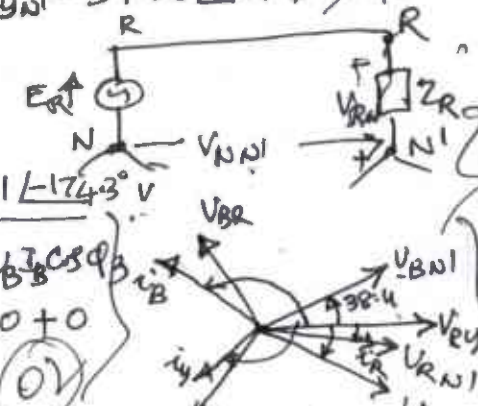
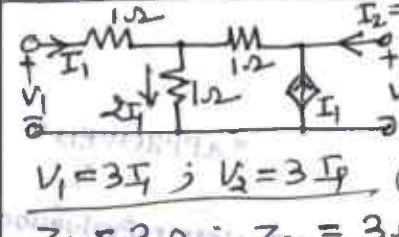
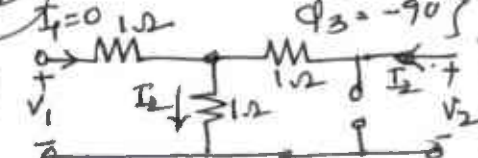
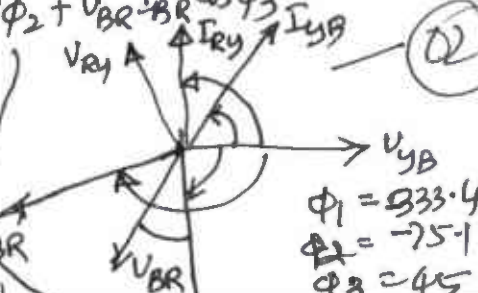

Question Number	Solution	Marks Allocated
Q2(b)	<p>KVL for Loop ①: <math>3i_1 + 2 \frac{d(i_1 - i_2)}{dt} = 5 \cos 20\pi t</math> --- (1)</p> <p>KVL for Loop ②: <math>\frac{1}{4} \int_0^t i_2 dt + 10i_2 + 2 \frac{d(i_2 - i_1)}{dt} = 0</math> --- (2)</p> <p>The exact dual equations of ① &amp; ② are</p> <p><math>3v_1 + 2 \frac{d(v_1 - v_2)}{dt} = 5 \cos 20\pi t</math> --- (3)</p> <p><math>\frac{1}{4} \int_0^t v_2 dt + 10v_2 + 2 \frac{d(v_2 - v_1)}{dt} = 0</math> --- (4)</p>	<p>02</p> <p>08</p> <p>04</p>
Q2(c)	 <p>Diagram 1: Bridge network with resistors 2Ω, 3Ω, 1Ω, 2Ω and current sources 2A, 3A.</p> <p>Diagram 2: Simplified bridge network with resistors 2Ω, 3Ω, 1Ω, 2Ω and current sources 3A, 1A.</p> <p>Diagram 3: Thevenin equivalent circuit with a 3V source and 1.75Ω resistor.</p> <p>Diagram 4: Load circuit with a 1.75Ω resistor and a 3/4V source.</p>	<p>02</p> <p>02</p> <p>02</p> <p>06</p>
Q3(a)	<p>To find <math>V_{th}</math>: open ckt <math>v_o</math> at AB: Applying KVL in</p> <p><math>20 \left( \frac{V_1}{100} \right) - V_1 + 100 = 0 \therefore V_1 = V_{AB} = 125V</math> (02)</p> <p>To find <math>R_{th}</math>: short ckt terminals AB &amp; find <math>I_{sc}</math></p> <p><math>\therefore I_{sc} = \frac{100}{20} = 5A</math> (02)</p> <p><math>\therefore Z_{th} = \frac{V_{oc}}{I_{sc}} = \frac{125}{5} = 25\Omega</math> (01)</p> <p>The eq. ckt:  (01)</p>	<p>02</p> <p>08</p> <p>01</p>
3(b)	<p>Thevenin's eq. ckt at the terminals of <math>R_L</math> i.e. Remove <math>R_L</math> &amp; find the <math>V_{oc} = V_{th}</math> (01)</p> <p><math>\therefore V_{th} = \frac{100 \angle 0^\circ}{20 + j10} \times j10 = \frac{100 \angle 0^\circ \times 10 \angle 90^\circ}{22.36 \angle 26.56^\circ} = 44.72 \angle 63.44^\circ V</math> (04)</p> <p><math>Z_{th} = \frac{20 \times j10}{20 + j10} = 8.94 \angle 63.44^\circ \therefore R_L =  Z_{th}  = 8.94 \Omega</math> (02)</p> <p><math>I_L = \frac{V_{th}}{Z_{th} + R_L} = 2.94 \angle 31.72^\circ A</math> (01)</p> <p><math>P_{max} = I_L^2 R_L = 2.94^2 \times 8.94 = 77.27W</math> (01)</p> 	<p>01</p> <p>06</p> <p>01</p>

Question Number	Solution	Marks Allocated
3 (c)	 $(1+j1)I_1 - j1I_2 = 5; -j1I_1 + 2I_2 = 0$ $I_2 = \frac{j5}{3+j2} = I_1 \downarrow \quad (02)$ <p>5V source is placed in series with 2-j2</p>  $(1+j1)V_1' - j1V_2' = 0$ $-j1V_1' + 2V_2' = -5$ $V_1' = \frac{-5j}{3+j2} = -I'' = \frac{j5}{3+j2} \downarrow \quad (02)$	06
Q4 (a)	<p>Hence the theorem.</p>  <p>open 5∠0° A</p> <p>KCL at (1): <math>(\frac{1}{5} + \frac{1}{5\angle 30^\circ})V_1' - \frac{1}{5\angle 30^\circ}V_2' = 10\angle 0^\circ \quad (1)</math></p> <p>KCL at (2): <math>-\frac{1}{5\angle 30^\circ}V_1' + [\frac{1}{5\angle 30^\circ} + \frac{1}{2} + \frac{1}{j10}]V_2' = 0 \quad (2)</math></p> <p>open 10∠0° A source</p>  <p>at node (1): <math>(\frac{1}{5} + \frac{1}{5\angle 30^\circ})V_1'' - \frac{1}{5\angle 30^\circ}V_2'' = 0 \quad (3)</math></p> <p>at node (2): <math>-\frac{1}{5\angle 30^\circ}V_1'' + (\frac{1}{5\angle 30^\circ} + \frac{1}{2} + \frac{1}{j10})V_2'' = 5\angle 0^\circ \quad (4)</math></p> <p><math>V_2'' = 8.14 \angle 12^\circ V</math> (01) By Superposition</p> <p><math>V_2 = V_2' + V_2'' = 16.45 \angle 4.35^\circ</math></p>	08
Q4 (b)	<p>To find <math>V_{oc}</math> open <math>R_L</math></p>  <p><math>I_1 = \frac{60}{100+100} = \frac{6}{5} A; I_2 = \frac{3}{5} A</math> (02)</p> <p><math>40I_1 + V_{oc} - 60I_2 = 0</math> (01)</p> <p><math>V_{oc} = (60-40)I_1 = 20 \times \frac{3}{5} = 12V</math> (02)</p>  <p><math>\Rightarrow \frac{(60+40) \times (60+40)}{200} = 48\Omega</math> (02)</p>	08
(c)	<p>Statement: 02</p> <p>Proof:</p>  <p><math display="block">E_2 = \frac{E_1Y_1 + E_2Y_2 + \dots}{Y_1 + Y_2 + \dots}</math></p>	04



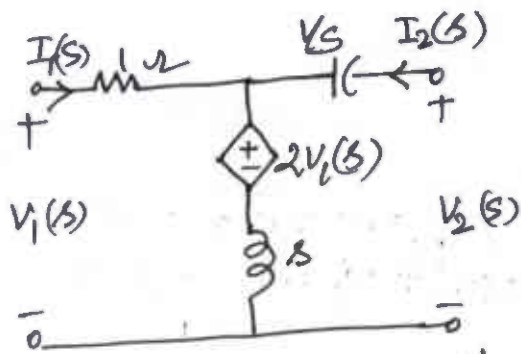
Question Number	Solution	Marks Allocated
Q5 (a)	$Y_{in} = \left( \frac{R_L}{R_L^2 + X_L^2} + \frac{R_C}{R_C^2 + X_C^2} \right) + j \left( \frac{X_C}{R_C^2 + X_C^2} - \frac{X_L}{R_L^2 + X_L^2} \right)$ <p>j term is zero at Resonance <math>\omega = \omega_0</math></p> $\frac{X_C}{R_C^2 + X_C^2} = \frac{X_L}{R_L^2 + X_L^2} \implies X_C R_L^2 + X_C X_L^2 = X_L R_C^2 + X_L X_C^2$ $\omega_0 = \frac{1}{\sqrt{LC}} \sqrt{\frac{4LC - R_L^2}{4LC - R_C^2}}$	08
(b)	<p>Eq. ext at <math>t=0^+</math></p> <p>for <math>t &gt; 0</math> <math>R_1 i_1 + \frac{1}{C} \int (i_1 - i_2) dt = V</math> ; <math>L \frac{di_2}{dt} + R_2 i_2 + \frac{1}{C} \int (i_2 - i_1) dt = 0</math></p> <p><math>i_1(0^+) = \frac{V}{R_1}</math> ; <math>i_2(0^+) = 0</math> ; <math>V_1(0^+) = 0</math> ; <math>V_2(0^+) = 0</math></p> <p><math>\frac{dV_2}{dt}(0^+) = R_2 \frac{di_2}{dt}(0^+) = 0</math> ; <math>\frac{dV_1}{dt}(0^+) = \frac{V}{R_1 C}</math></p> <p>At <math>t = \infty</math> : <math>V_1(\infty) = 0</math> ; <math>i_2 = \frac{V}{R_1 + R_2}</math> ; <math>V_2(\infty) = \frac{V R_2}{R_1 + R_2}</math></p> <p>KCL eq. for <math>V</math> : <math>C \frac{dV}{dt} + GV + \frac{1}{L} \int V dt = I</math></p> <p><math>\frac{d^2 V}{dt^2} + 4 \frac{dV}{dt} + 4V = 0 \implies s^2 + 4s + 4 = 0 ; s_1 = -2, s_2 = -2</math></p> <p><math>V(t) = K_1 e^{-2t} + K_2 t e^{-2t}</math> ; <math>V(0^+) = 0</math> &amp; <math>\frac{dV}{dt}(0^+) = \frac{1}{3} V / s</math></p> <p><math>\therefore V(t) = \frac{1}{3} t e^{-2t}</math> ; <math>K_1 = 0</math> &amp; <math>K_2 = \frac{1}{3}</math></p>	02 01 02 02 02 02 02 12
Q6	<p>(i) <math>f_0 = \frac{1}{2\pi\sqrt{LC}}</math> ; <math>C = \frac{1}{400 \times 10^6 \times f_0^2} = 105.54 \mu F</math></p> <p>(ii) <math>I_0 = V/R = 20,000 A</math> ; <math>V_C = I_0 X_C = 151 kV</math></p> <p>(iii) Maximum instantaneous energy <math>= W = \frac{1}{2} L I_0^2</math></p> <p><math>W = \frac{1}{2} \times 0.006 \times (20,000 \sqrt{2})^2 = 24 \times 10^6 J</math></p> <p><math>Q_0 = \frac{\omega_0 L}{R} = 377</math> ; <math>\Delta f = \frac{f_0}{Q_0} = 0.53 Hz</math></p> <p><math>f_1 = f_0 - \frac{1}{2} \Delta f = 199.74 Hz</math> ; <math>f_2 = f_0 + \frac{1}{2} \Delta f = 200.26 Hz</math></p>	02 02 02 02 02 02 08
(c)	<p>Definition -</p> <p>Eq. ext: </p>	02 02 04

Question Number	Solution	Marks Allocated
Q7 (a)	$f_1(t) = u(t) - 2u(t-a) + u(t-2a)$ $F_1(s) = \frac{1}{s}(1 - 2e^{-as} + e^{-2as}) = \frac{1}{s}(1 - e^{-as})^2$ <p><math>T = 2a</math>. LT of square wave</p> $F(s) = \frac{1}{1 - e^{-Ts}} F_1(s) = \frac{1}{s} \frac{(1 - e^{-as})^2}{(1 - e^{-2as})}$ $F(s) = \frac{1}{s} \tanh\left(\frac{as}{2}\right)$	<p>(02)</p> <p>(02)</p> <p>(02)</p> <p>(02)</p> <p>(01)</p>
Q7 (b)	<p>KVL eq. for t &gt; 0. ; <math>6i + \frac{di}{dt} + \frac{1}{0.04} \int i dt = 12 \sin t</math></p> <p>taking LT. <math>6I(s) + sI(s) + 25 \frac{I(s)}{s} + \frac{1}{s} = \frac{60}{s^2 + 25}</math></p> $I(s) = \frac{60s}{(s^2 + 25)(s^2 + 6s + 25)} + \frac{5s - 1}{s^2 + 6s + 25}$ <p>taking <math>L^{-1}</math></p> $i(t) = 5e^{-3t} \cos 4t - 6.5e^{-3t} \sin 4t + 2 \sin t$	<p>(02)</p> <p>(02)</p> <p>(02)</p> <p>(04)</p>
Q8 (c)	<p>statement - (02)</p> <p>proof - (02)</p>	 <p>(01)</p>
Q8 (a)	$RC \frac{dv_c}{dt} + v_c = v_i(t)$ $RC \frac{dv_c}{dt} + v_c = u(t) - u(t-T)$ <p>taking inverse LT</p> $RC [sV_c(s) - v_c(0^+)] + v_c(s) = \frac{1}{s}(1 - e^{-Ts})$ <p>since <math>v_c(0^+) = 0</math></p> $(RCs + 1)V_c(s) = \frac{1}{s}(1 - e^{-Ts})$ $V_c(s) = \frac{1 - e^{-Ts}}{s(RCs + 1)}$ $v_c(t) = (1 - e^{-t/RC})u(t) - (1 - e^{-(t-T)/RC})u(t-T)$	<p>(02)</p> <p>(01)</p> <p>(02)</p>
Q8 (b)	  $\mathcal{L}[\sin wt u(t-t_0)] = \int_{t_0}^{\infty} \sin wt e^{-st} dt$ $= \frac{1}{2j} \int_{t_0}^{\infty} \left( \frac{e^{(s+jw)t}}{(s+jw)t} - \frac{e^{(s-jw)t}}{(s-jw)t} \right) dt$ $= e^{-t_0 s} \left[ \frac{w \cos wt_0 + s \sin wt_0}{s^2 + w^2} \right]$ $\mathcal{L}[\sin w(t-t_0) u(t-t_0)] = e^{-t_0 s} \mathcal{L}[\sin wt] = e^{-t_0 s} \left( \frac{w}{s^2 + w^2} \right)$	<p>(02)</p> <p>(02)</p> <p>(01)</p> <p>(02)</p> <p>(02)</p>

Question Number	Solution	Marks Allocated
Q 9(a)	<p> <math>V_{Ry} = 100 \angle 0^\circ</math> ref. <math>V_{yB} = 100 \angle 120^\circ</math>; <math>V_{BR} = 100 \angle -120^\circ = 100 \angle 120^\circ</math>                      Line currents: <math>i_R = 27.05 \angle -8.7^\circ</math> A; <math>i_y = 19.7 \angle -121.1^\circ</math> A  <math>i_B = 26.69 \angle 128.4^\circ</math> A.                      Voltage across the impedances (i.e. phase voltages)  <math>V_{RN1} = 135.25 \angle -8.7^\circ</math> V; <math>V_{yN1} = 39.38 \angle -31.7^\circ</math> V } (02)  <math>V_{BN1} = 106.75 \angle 38.4^\circ</math> V  <math>V_{N1} + V_{RN1} = V_{RN} = E_R</math>  <math>\therefore V_{N1} = E_R - V_{RN1} = 84.11 \angle -174.3^\circ</math> V  <math>P = V_R I_R \cos \phi_1 + V_y I_y \cos \phi_2 + V_B I_B \cos \phi_3</math>  <math>= 135.25 \times 27.05 \times \cos 0^\circ + 0 + 0</math>  <math>P = 3.6585</math> kW                 </p> 	<p>10</p>
b	 <p> <math>V_1 = 3I_1</math>; <math>V_2 = 3I_2</math> (01)  <math>Z_{11} = 3 \Omega</math>; <math>Z_{21} = 3 \Omega</math>  <math>\therefore Z_{12} = 1 \Omega</math>; <math>Z_{22} = 2 \Omega</math>                      ABCD parameters: <math>A = \frac{Z_{11}}{Z_{21}} = \frac{3}{3} = 1</math>; <math>B = \frac{\Delta Z}{Z_{21}} = \frac{3}{3} = 1</math>  <math>C = \frac{1}{Z_{21}} = \frac{1}{3}</math>; <math>D = \frac{\Delta Z}{Z_{21}} = \frac{3}{3} = 1</math>; <math>T = \begin{bmatrix} 1 &amp; 1 \\ 1/3 &amp; 1 \end{bmatrix}</math>  <math>Z_{11} \neq Z_{22} \therefore</math> Not symmetrical; <math>Z_{12} \neq Z_{21}</math> not Reciprocal.                 </p> 	<p>10</p>
Q 10 (a)	<p> <math>V_{yB} = 400 \angle 0^\circ</math>; <math>V_{BR} = 400 \angle 120^\circ</math>; <math>V_{Ry} = 400 \angle 120^\circ</math>  <math>I_{Ry} = 3.58 \angle 93.4^\circ</math>; <math>I_{yB} = 5.15 \angle 75.1^\circ</math> (02)  <math>I_{BR} = 4 \angle 165^\circ</math>                      Line currents: <math>i_R = 5.88 \angle 51.6^\circ</math> A  <math>i_y = 2.09 \angle 42.4^\circ</math> A; <math>i_B = 7.95 \angle -130.8^\circ</math> A } (02)  <math>P = V_{Ry} I_{Ry} \cos \phi_1 + V_{yB} I_{yB} \cos \phi_2 + V_{BR} I_{BR} \cos \phi_3</math>  <math>P = 2941.2</math> W : (02)                 </p> 	<p>10</p>
10(b)	<p> <math>V_1(s) = -(s+1)I_1(s) - sI_2(s)</math> (01)  <math>V_2(s) = 2V(s) = \left(\frac{s+1}{s}\right)I_2(s) + sI_1(s)</math> (02)                 </p> 	<p>10</p>

PTD

(02) (02)



To find y-parameters.  $V_2(s) = 0$ .  
Using ns eq (1) & (2)

$$I_1(s) = \frac{-1}{s^2 + s + 1} V_1(s) \quad \& \quad I_2(s) = \frac{-s}{s^2 + s + 1} V_1(s)$$

$$y_{11} = \frac{I_1(s)}{V_1(s)} \Big|_{V_2=0} = \frac{-1}{s^2 + s + 1} ; \quad y_{21} = \frac{I_2(s)}{V_1(s)} \Big|_{V_2=0} = \frac{-s}{s^2 + s + 1} \quad \left. \vphantom{\frac{I_2(s)}{V_1(s)}}} \right\} \textcircled{04}$$

Short circuiting input port:  $V_1(s) = 0$ :

$$I_1(s) = \frac{-s^2}{s^2 + s + 1} V_2(s) ; \quad I_2(s) = \frac{s(s+1)}{s^2 + s + 1} V_2(s)$$

$$\frac{I_1(s)}{V_2(s)} \Big|_{V_1=0} = y_{12} = \frac{-s^2}{s^2 + s + 1} ; \quad \frac{I_2(s)}{V_2(s)} \Big|_{V_1=0} = y_{22} = \frac{s(s+1)}{s^2 + s + 1} \quad \left. \vphantom{\frac{I_2(s)}{V_2(s)}}} \right\} \textcircled{04}$$

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