

Internal Assessment Test 1 – Sept. 2019

Sub: NETWORK THEORY

Sub Code: 18EC32

Branch: ECE

Date: 06/09/2019

Duration: 90 min's

Max Marks: 50

Sem / Sec: III

III

OBE

Answer any FIVE FULL Questions

MARKS

CO

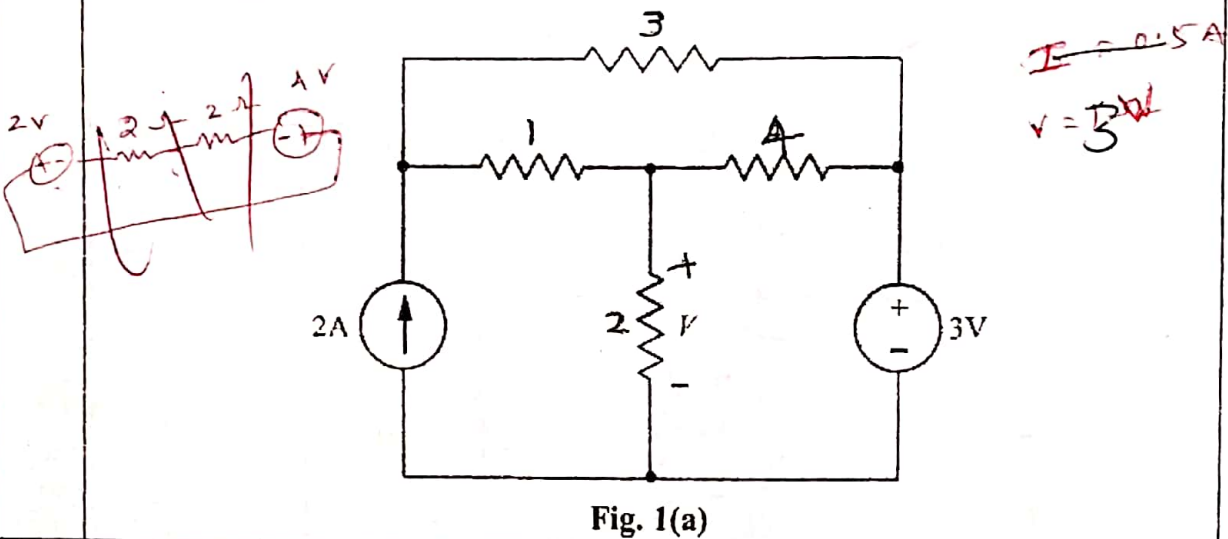
RBT

1 (a) Use source shifting and transformation techniques to find voltage across 2Ω resistor shown in Fig 1(a). All resistor values are in ohms

[05]

CO1

L3

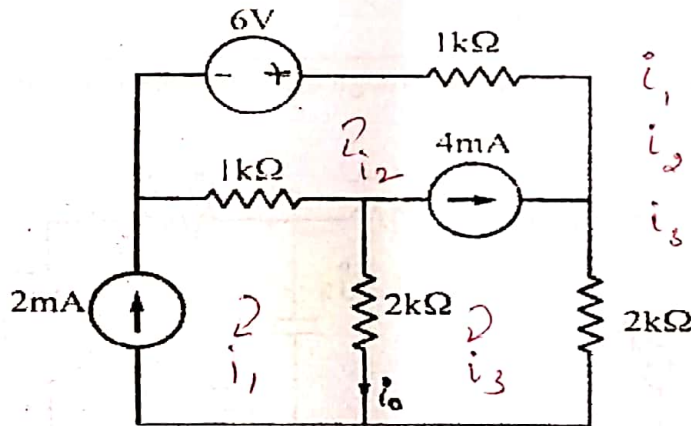


(b) Find the current i_0 using Mesh analysis in the circuit shown in Fig. 1(b).

[05]

CO1

L3



2. Find the power supplied by dependent source in the circuit of Fig.2

[10]

CO1

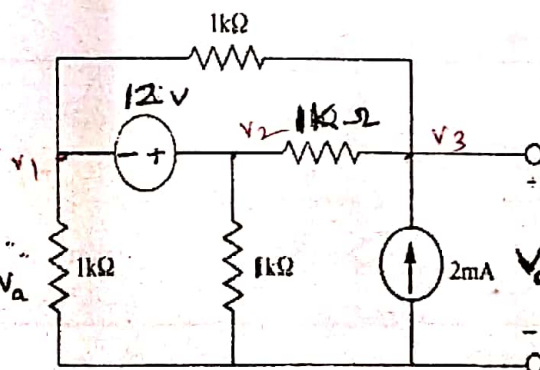
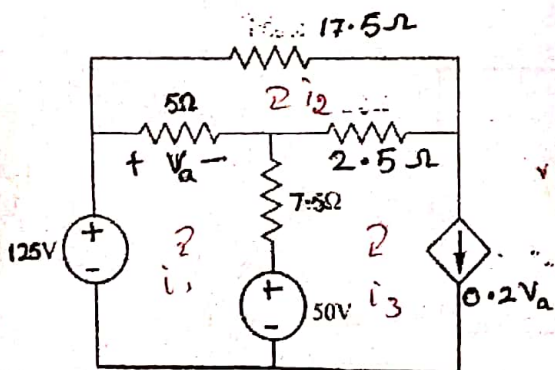
L3

3. Use nodal analysis to find v_0 in the network of Fig.3.

[10]

CO1

L3



4. Use the principle of superposition to solve for v_x for the circuit shown in Fig.4. Find the power delivered by 4A current source.

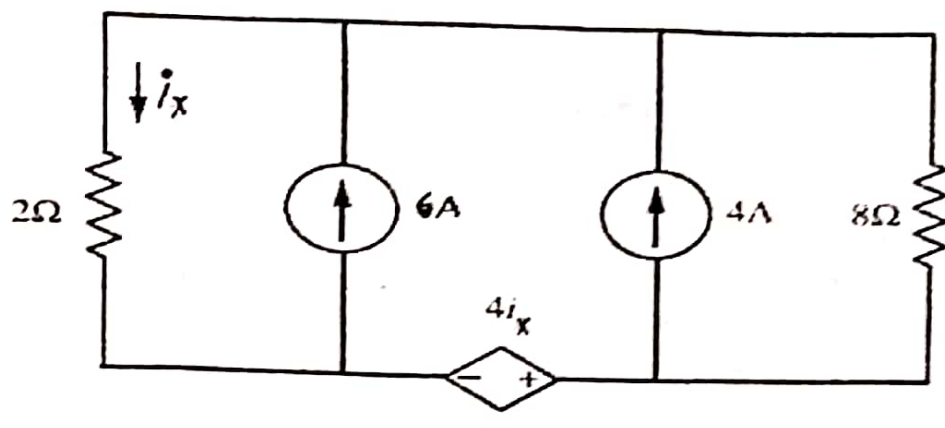


Fig.4

$6A: v_{x1} = 46V$
 $4A: v_{x2} = -\frac{32}{3}V$
 $v_x = 55.33V$
 $16 \div \frac{2}{3}$

5. Find the voltage V_1 using the superposition principle. Refer the circuit shown in Fig. 5.

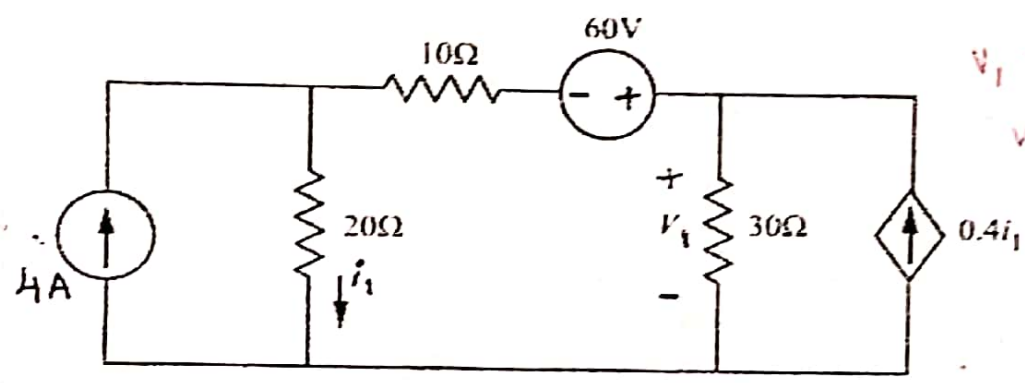


Fig. 5

$V_1 = 60V$
 $V_2 = 22.5V$
 $V = 82.5V$

6. Determine the value of V_2 such that the current through the impedance $(3+j4)$ ohm is Zero.

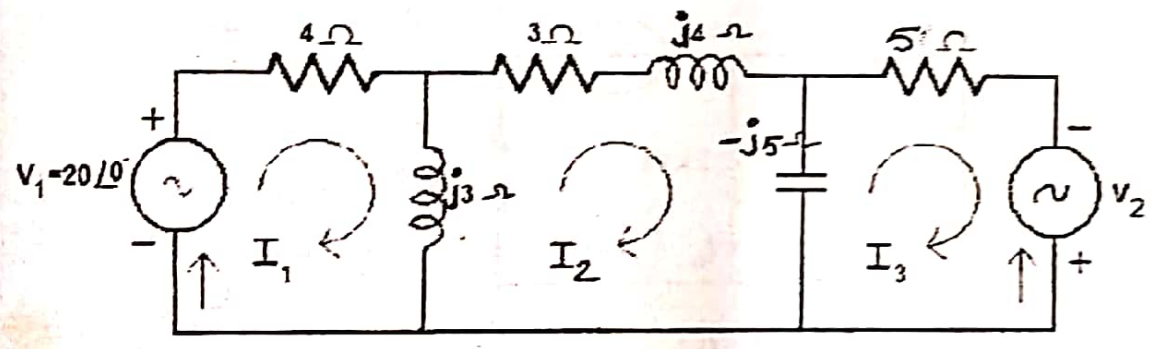


Fig. 6

$V_2 = 12\sqrt{2}$
 $V_2 = 16.97$
 $2 \cdot 4 = 16.8$

7. Obtain the equivalent resistance R_{ab} for the circuit of Fig. 7 and hence find i .

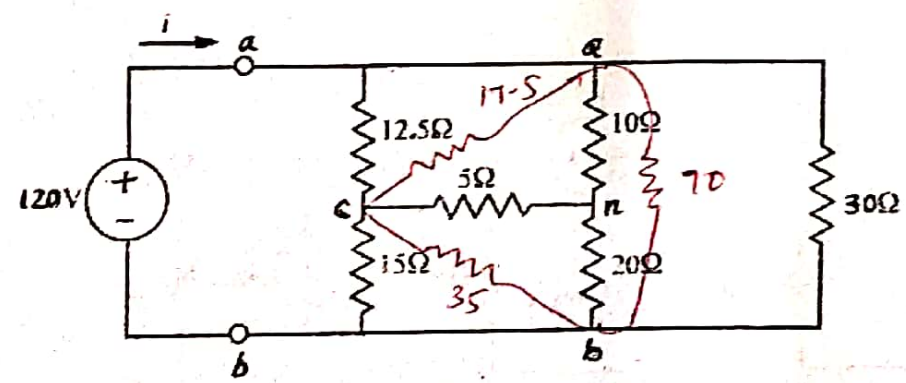
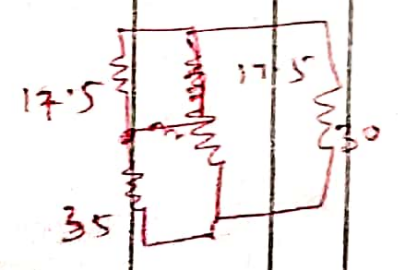


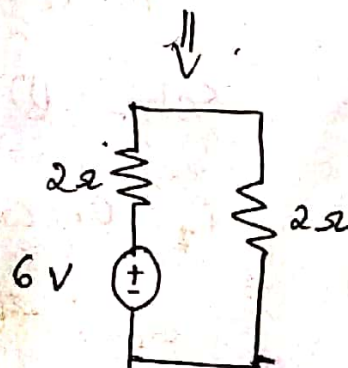
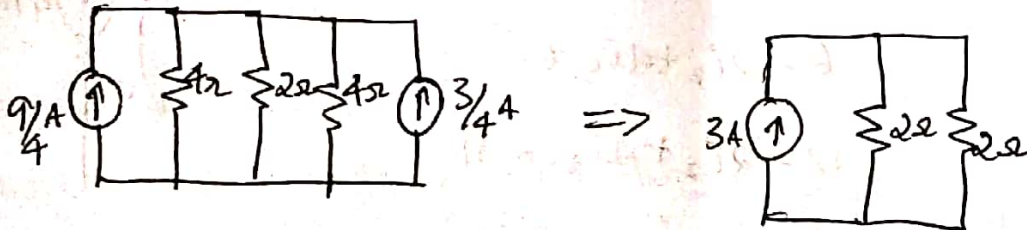
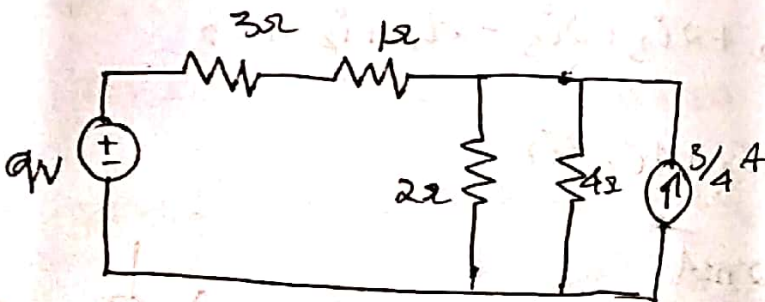
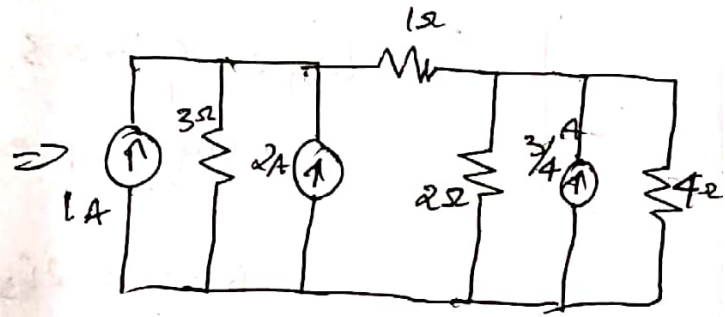
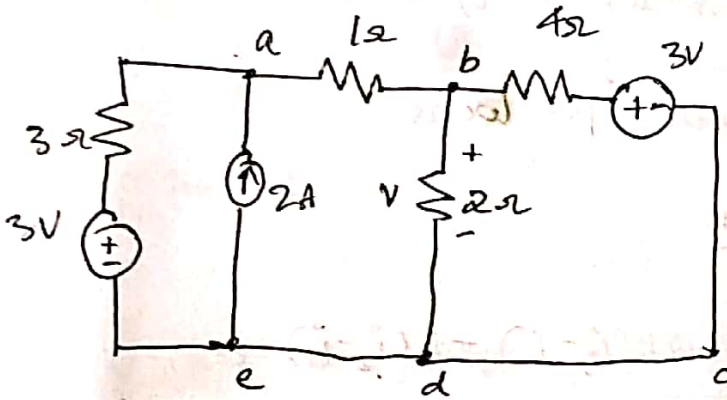
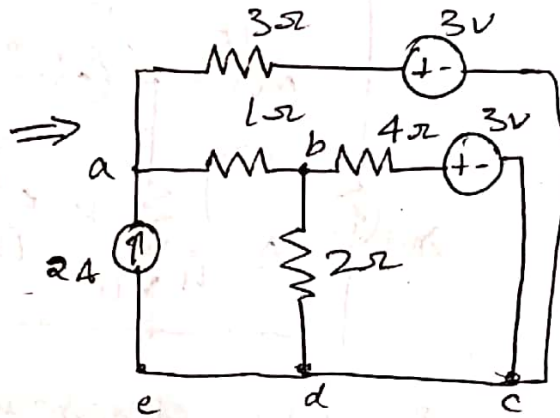
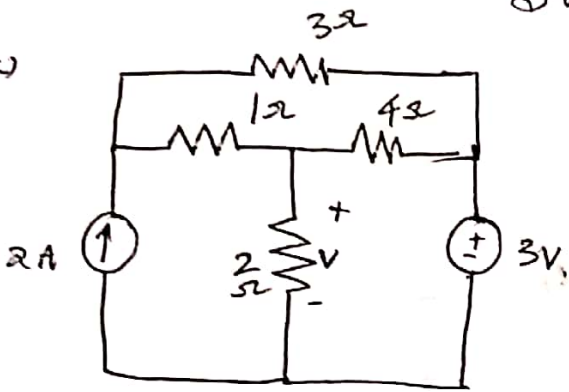
Fig. 7



Network Theory IAT 1

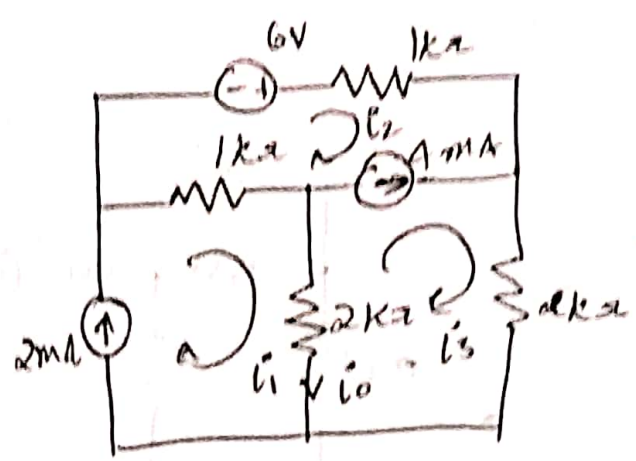
Solution

(a)



Across 2Ω
 $\Rightarrow \frac{6 \times 2}{3} = 3V$

b.



By direct observation $\Rightarrow i_1 = 2\text{mA}$

loop 2 & loop 3 are super loops -
superloop equ.

$$6 - 1k - 2i_3k - 2k(i_3 - i_1) - k(i_2 - i_1) = 0$$

$$6 = i_2 + 2i_3 + 2i_3 - 2i_1 + i_2 - i_1 = 0$$

$$6 = (2i_2 + 4i_3 - 3i_1)$$

$$i_1 = 2\text{mA}$$

$$6 = 2i_2 + 4i_3 - 6$$

$$12 = 2i_2 + 4i_3 \quad \text{--- (1)}$$

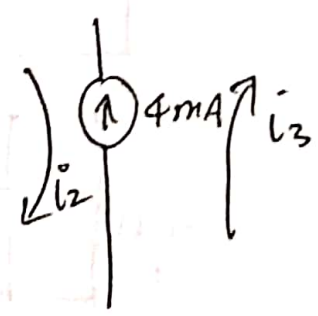
$$4 = i_3 - i_2 \quad \text{--- (2)}$$

Solve (1) and (2)

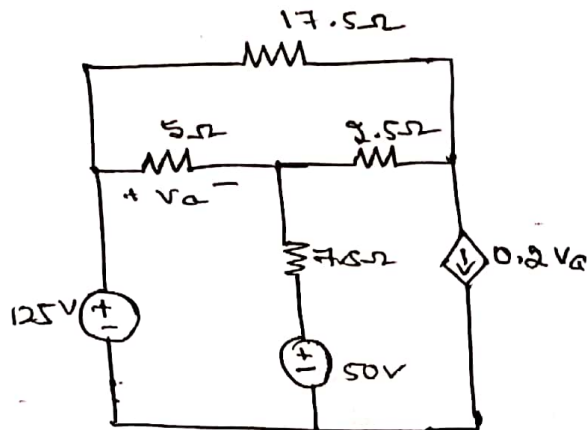
$$i_2 = 0.66\text{mA} \quad i_3 = 3.34\text{mA}$$

$$I_0 = i_1 - i_3$$

$$I_0 = (2 - 3.34)\text{mA}$$



9) Find the power supplied by dependent source in the circuit



By direct observation

$$i_3 = 0.2V_a \text{ A} \rightarrow \textcircled{1}$$

KVL for loop 1 and loop 2

Loop-1

$$125 = 5(i_1 - i_2) + 7.5(i_1 - i_3) + 50$$

$$125 - 50 = 5i_1 - 5i_2 + 7.5i_1 - 7.5i_3$$

$$75 = 12.5i_1 - 5i_2 - 7.5i_3 \rightarrow \textcircled{2}$$

$$i_1 = 13.2 \text{ A}$$

$$i_2 = 3.6 \text{ A}$$

$$i_3 = 9.6 \text{ A}$$

Loop-2

$$0 = 17.5i_2 + 2.5(i_2 - i_3) + 5(i_2 - i_1)$$

$$0 = 25i_2 - 5i_1 - 2.5i_3 \rightarrow \textcircled{3}$$

$$V_a = 5(i_1 - i_2) \rightarrow \textcircled{4}$$

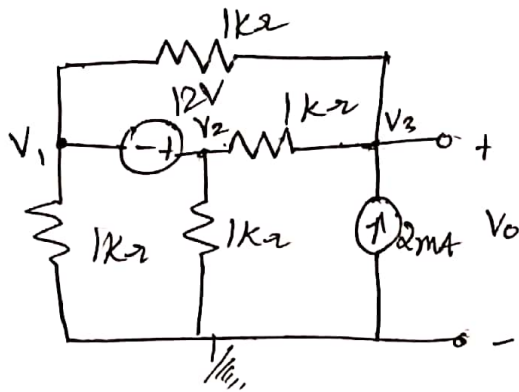
V_a in $\textcircled{1}$

$$i_3 = 0.2(5i_1 - 5i_2)$$

$$i_3 = i_1 - i_2$$

$$i_1 - i_2 - i_3 = 0$$

3.



V_2 and V_3 are super node.

$$\frac{V_2 - V_3}{1} + \frac{V_2 - 0}{1} + \frac{V_1 - 0}{1} + \frac{V_1 - V_3}{1} = 20 \quad \text{--- (1)}$$

~~$\frac{V_3 - V_1}{1} + \frac{V_3 - V_2}{1} = 2$~~

~~$$\frac{V_3 - V_1}{1} + \frac{V_3 - V_2}{1} = 2 \quad \text{--- (2)}$$~~

We know - $V_2 - V_1 = 0 \text{ } 12\text{V}$
 $V_2 = V_1$

~~$$V_2 - V_3 + V_2 + V_2 + V_2 - V_3 = 0 \quad \text{--- (1)}$$~~

~~$$4V_2 - 2V_3 = 0 \quad \text{--- (a)}$$~~

~~$$V_3 - V_2 + V_3 - V_2 = 2 \quad \text{--- (2)}$$~~

~~$$2V_3 - 2V_2 = 2 \quad \text{--- (b)}$$~~

So we (a) and (b)

$$V_2 = 1\text{V}$$

$$V_3 = 2\text{V}$$

Super node eqn:

$$\frac{V_1}{1k} + \frac{V_2}{1k} + \frac{V_2 - V_3}{1k} + \frac{V_1 - V_3}{1k} = 0$$

@ node V_3 :

$$\frac{V_3 - V_1}{1k} + \frac{V_3 - V_2}{1k} = 2\text{mA}$$

By solving

$$V_1 = 7\text{V}$$

$$V_2 = 7\text{V}$$

$$V_3 = 2\text{V} = V_0$$

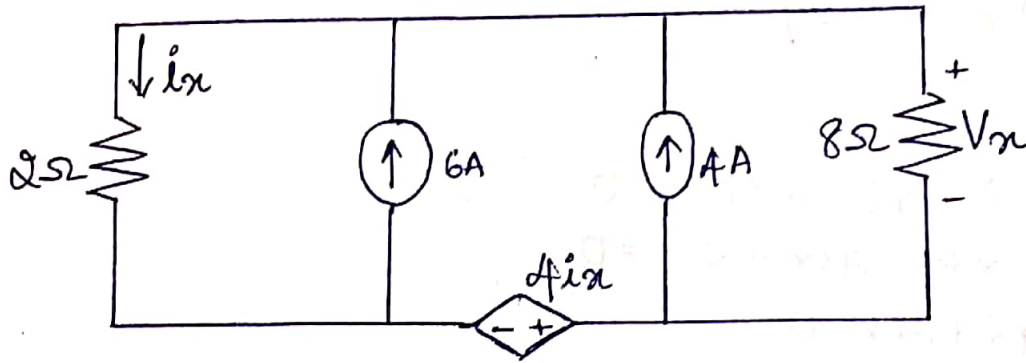
$$V_3 = V_0 = 2\text{V}$$

$$V_2 = V_1$$

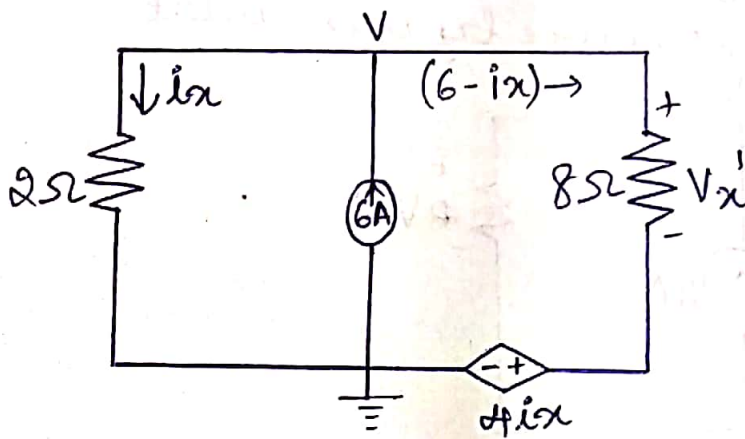
$$V_1 = 1\text{V}$$

NETWORK THEORY

4th SOLⁿ



Case 1: Considering 6A current source alone,
Replace 4A current source with open circuit.



By nodal analysis

$$\frac{V_x}{2} + \frac{V - 4i_x}{8} = 6$$

$$4V + V - 4i_x = 48$$

$$5V - 4i_x = 48$$

$$i_x = \frac{V}{2}$$

$$\Rightarrow 5V - 4\left(\frac{V}{2}\right) = 48 \Rightarrow 3V = 48 \Rightarrow V = \frac{48}{3}$$

$$\Rightarrow V = 16V$$

$$i_x = \frac{V}{2} = \frac{16}{2} = 8A \quad \therefore \boxed{i_x = 8A}$$

P.T.O

By KVL : $V - V_{x'} - 4i_x = 0$

$$V_{x'} = V - 4i_x = 16 - 32 = -16V$$

$$\boxed{V_{x'} = -16V}$$

i_x by KVL :

$$-8(6 - i_x) - 4i_x + 2i_x = 0$$

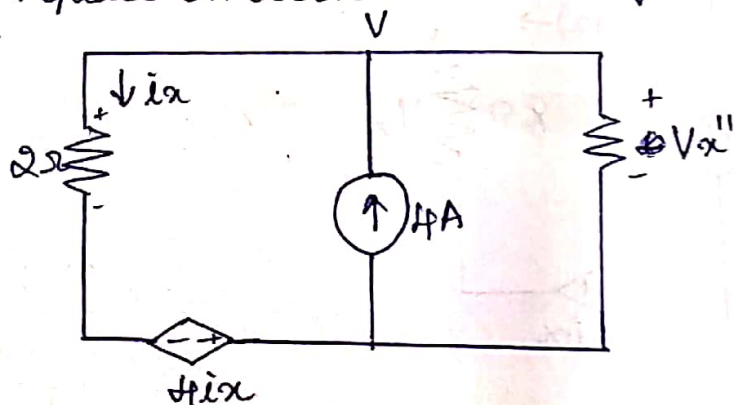
$$-48 - 8i_x - 4i_x + 2i_x = 0$$

$$-48 + 6i_x = 0$$

$$\Rightarrow i_x = \frac{48}{6}$$

$$\therefore \boxed{i_x = 8A}$$

Case 2 : Consider 4A current source alone,
Replace 6A current source by open circuit



By KVL : $-8(4 - i_x) - 4i_x + 2i_x = 0$

$$-32 + 8i_x - 4i_x + 2i_x = 0$$

$$6i_x = 32$$

$$i_x = \frac{32}{6} \Rightarrow \underline{\underline{i_x = 5.33A}}$$

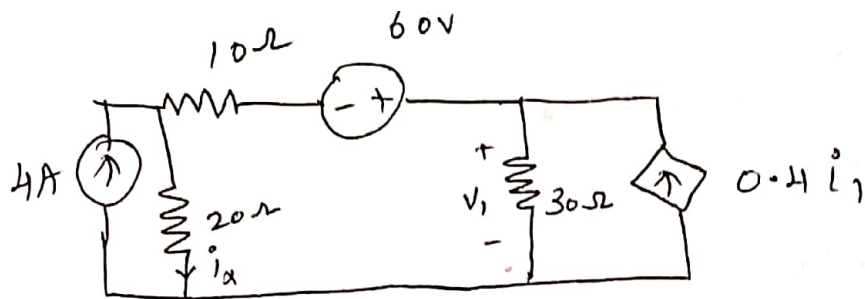
$$V_{x''} = 8(4 - i_x) = 8(4 - 5.33)$$

$$\boxed{V_{x''} = -10.64V}$$

By SPT,

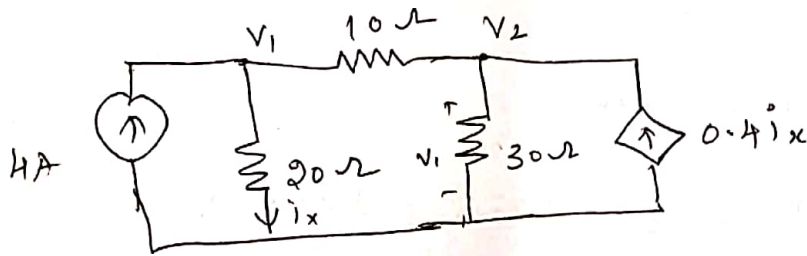
$$V_x = V_{x'} + V_{x''} = -16 - 10.64$$

$$\Rightarrow \boxed{V_x = -26.64V}$$



Case 1:

Consider 4A source active alone.



$$\frac{V_1 - V_2}{10} + \frac{V_1}{10} - 4 = 0$$

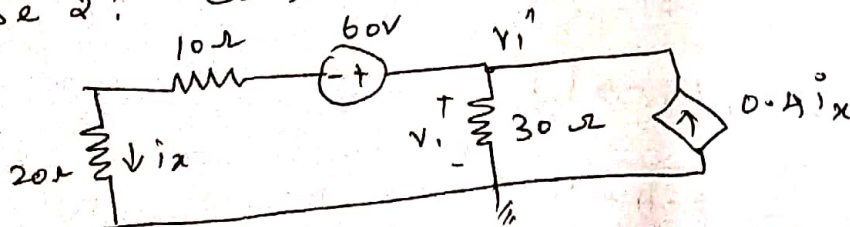
$$3V_1 - 2V_2 = 80$$

$$\frac{V_2 - V_1}{10} + \frac{V_2}{30} - 0.4\left(\frac{V_1}{20}\right) = 0$$

$$20V_2 - 18V_1 = 0$$

$$V_1' = 60 \text{ V}$$

Case 2: Consider 60V source active alone.



$$\frac{V_1'' - 60}{30} + \frac{V_1'}{30} = 0.4 i_x$$

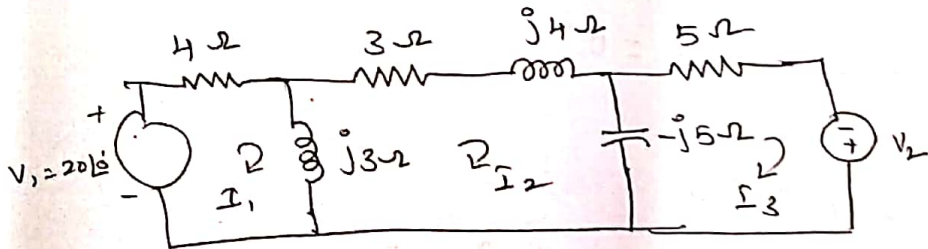
$$i_x = \frac{V_1'' - 60}{30}$$

$$\boxed{V_1'' = 22.5 \text{ V}}$$

O/P = case 1 + case 2

$$V = V' + V_1'' = 60 + 22.5 = 82.5 \text{ V}$$

eg: 6



Loop 1:
$$I_1 = \frac{20}{4 + 3j}$$

Loop 2:
$$I_2 = 0$$

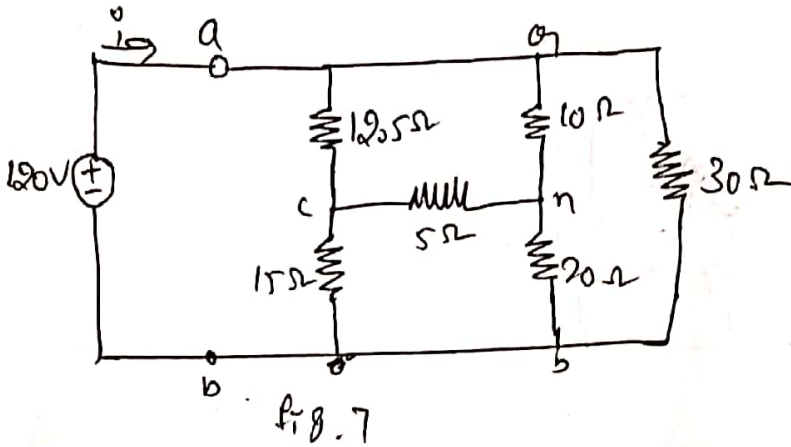
$$-3j i_1 + 0 + 5j i_3 = 0$$

$$i_3 = 1.92 - 1.44j \text{ A}$$

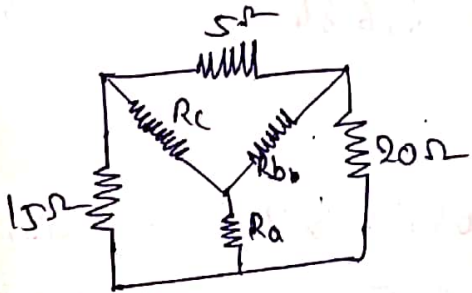
Loop 3:
$$V_2 = i_3 (5 - 5j)$$

$$\boxed{V_2 = 2.4 - 16.8j \text{ V}}$$

⑦ Obtain the equivalent resistance, R_{ab} for the circuit of fig. 7. & hence find i_0 . [10 marks]



Soln Consider a Δ connection part.

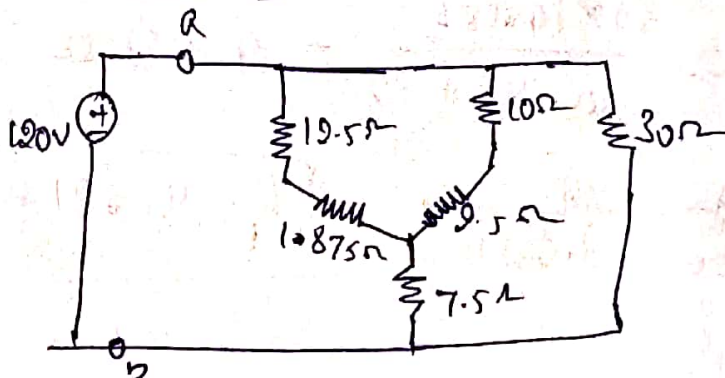


$$R_a = \frac{15 \times 20}{15 + 20 + 5} = 7.5 \Omega$$

$$R_b = \frac{5 \times 20}{15 + 20 + 5} = 2.5 \Omega$$

$$R_c = \frac{5 \times 15}{15 + 20 + 5} = 1.875 \Omega$$

Now circuit diagram is

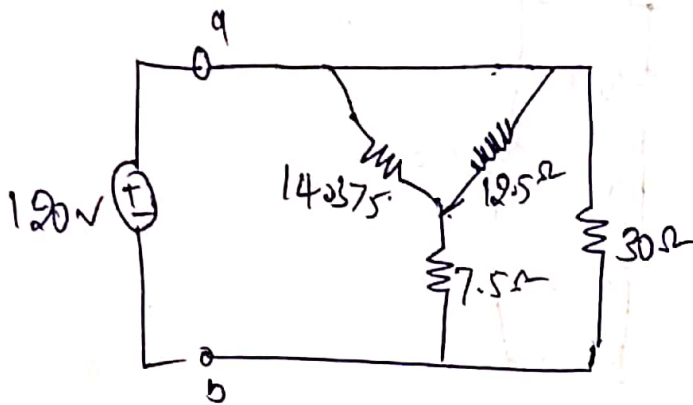


$10\ \Omega$ & $2.5\ \Omega$ are in series

$$10 + 2.5 = 12.5\ \Omega$$

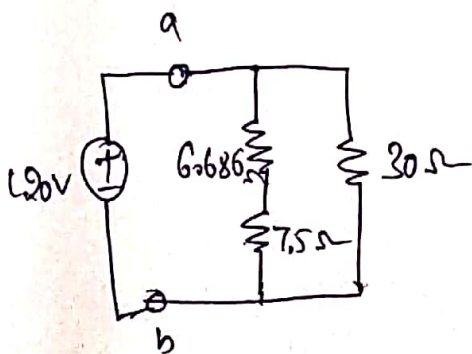
$12.5\ \Omega$ & $1.875\ \Omega$ are in series

$$12.5 + 1.875 = 14.375\ \Omega$$



$12.5\ \Omega$ & $14.375\ \Omega$ are in parallel.

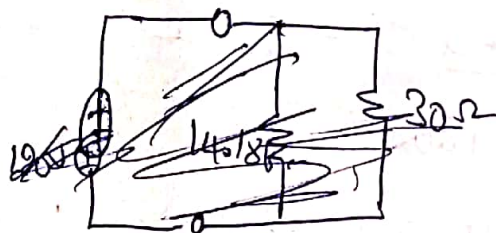
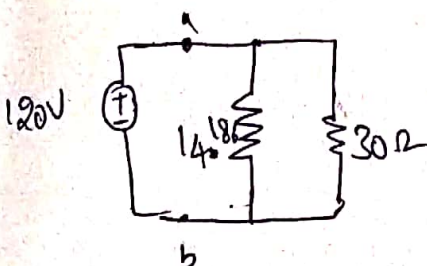
$$\frac{12.5 \times 14.375}{12.5 + 14.375} = 6.686$$



$6.686\ \Omega$ & $7.5\ \Omega$ are in series

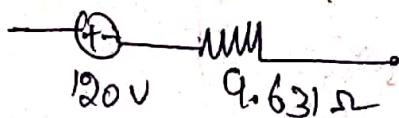
~~$$6.686 + 7.5 = 14.186\ \Omega$$~~

$$6.686 + 7.5 = 14.186\ \Omega$$



$14.186\ \Omega$ & $30\ \Omega$ are in parallel.

$$R_{eq} = \frac{30 \times 14.186}{14.186 + 30} = 9.631\ \Omega$$



$$R_{eq} = 9.631\ \Omega$$

$$I = \frac{V}{R}$$
$$= \frac{120}{9.631}$$

$$I = 12.4597 \text{ A}$$