

IAT-3

4. $V_s = 5V$
 $V_a = 15V$
 $I = 0.5A$
 $f = 25kHz$
 $L = 220\mu H$
 $C = 220\mu F$

1. Duty Cycle:-

$$V_a - V_a k = V_s$$

$$V_a = \frac{V_s}{1-k}$$

~~$V_a = V_s$~~

$$15 = \frac{5}{1-k}$$

$$1-k = \frac{5}{15}$$

$$1 - \frac{5}{15} = k$$

$$k = 0.6667$$

(i) The ripple current of inductor.

$$\Delta I = \frac{V_s (V_a - V_s)}{LfV_a} = \frac{5(15-5)}{220 \times 10^{-6} \times 25 \times 10^3 \times 15} = 0.606A$$

(ii) The ripple voltage of capacitor.

$$\Delta V = \frac{I_a (V_a - V_s)}{fC I_a} = \frac{0.606(15-5)}{220 \times 10^{-6} \times 25 \times 10^3 \times 0.5} = 2.202V$$

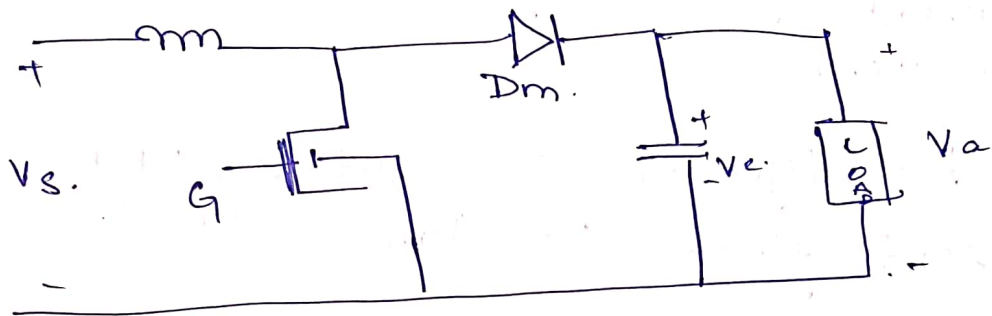
Critical values of L & C .

$$L = \frac{k(1-k)R}{2f} = \frac{0.667(1-0.667) \times 30}{2 \times 25 \times 10^3} = 133.266 \mu H$$

$$C = \frac{k}{2fR} = \frac{0.667}{2 \times 25 \times 10^3 \times 30} = 0.446 \mu F$$

$$R = \frac{V_{avg}}{I_{avg}} = \frac{15}{0.5} = 30 \Omega$$

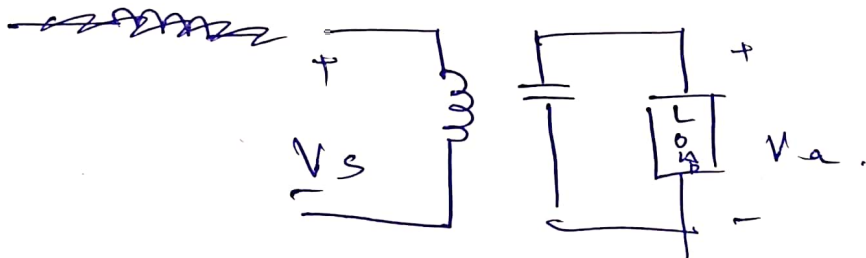
3. Boost Regulator



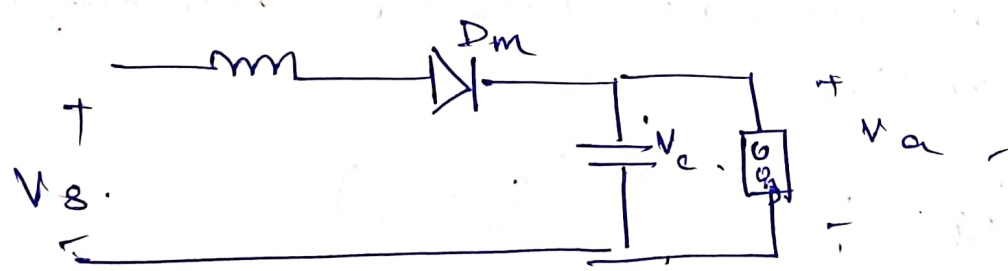
⇒ Boost Regulator, the output voltage is greater than the input voltage, hence called a boost Regulator.

⇒ It has two modes of operation.

Mode 1

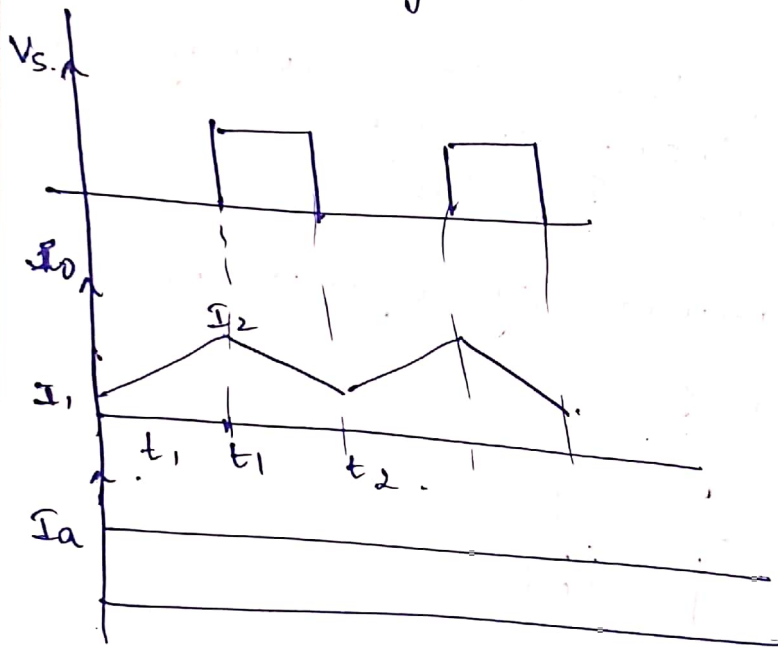


Mode 2



⇒ When the thyristor is switched on, it reverse biases the Dm diode, hence the current flows from source → ~~Capa~~ Inductor.

⇒ When the thyristor is switched OFF, the current flows $L \rightarrow Dm \rightarrow Load$.



Derivation

⇒ Consider current increases linearly in the inductor.

$$V_s = \frac{L(I_2 - I_1)}{t_1}$$

$$\boxed{V_s = \frac{L \Delta I}{t_1}} \rightarrow \textcircled{1}$$

⇒ Consider current decreases linearly in the inductor.

$$V_s - V_a = -L \frac{(I_2 - I_1)}{t_2}$$

$$\boxed{V_s - V_a = -L \frac{\Delta I}{t_2}} \rightarrow \textcircled{2}$$

From ① & ②.



$$\Delta I = \frac{V_s t_1}{L}$$

$$\Delta I = -\frac{(V_s - V_a) t_2}{L}$$

$$\cancel{V_s t_1} = \cancel{(V_a - V_s) t_2}$$

$$\boxed{V_s t_1 = (V_a - V_s) t_2} \rightarrow \textcircled{3}$$

$$V_s t_1 = V_a t_2 - V_s t_2$$

$$V_s (t_1 + t_2) = V_a t_2$$

$$\Rightarrow \boxed{V_a = \frac{V_s T}{t_2}}$$



Substitute $t_1 = kT$ & $t_2 = (1-k)T$ in (3)

$$V_s(kT) = (V_a - V_s)(1-k)T$$

$$V_s k = (V_a - V_s)(1-k)$$

$$= V_a - kV_a - V_s + V_s k$$

$$\frac{V_a - V_s}{V_s} = \frac{1-k}{k}$$

For Time period $T = t_1 + t_2$

$$T = \frac{L \Delta I}{V_s} + \left(- \frac{\Delta I L}{V_s - V_a} \right)$$

$$= \frac{L \Delta I}{V_s} + \frac{\Delta I L}{V_a - V_s}$$

$$T = \frac{L \Delta I V_a - L \Delta I V_s + \Delta I V_s}{V_s(V_a - V_s)}$$

$$T \times V_s (V_a - V_s) = \frac{\Delta I (L V_a - L V_s + L V_s)}{L V_a f}$$

$$\boxed{\Delta I = \frac{V_s (V_a - V_s)}{L V_a f}} \rightarrow \text{Ripple Current}$$

Ripple Voltage

$$\Delta V = \frac{I_s (V_a - V_s)}{I_a f C}$$

Critical Value of Inductor

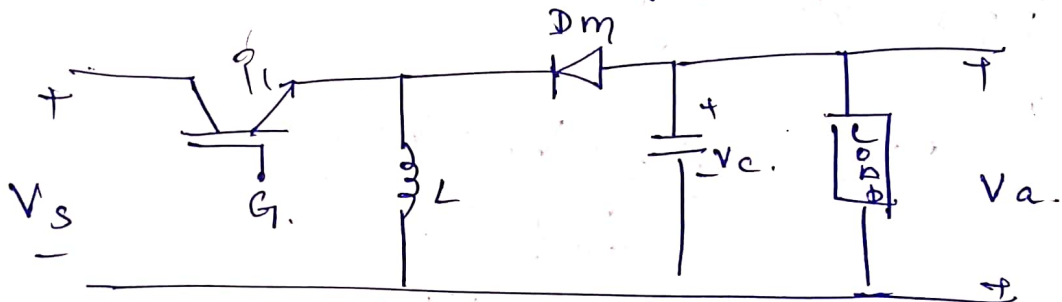
$$L_c = \frac{k(1-k)R}{2f}$$

Critical Value of Capacitor

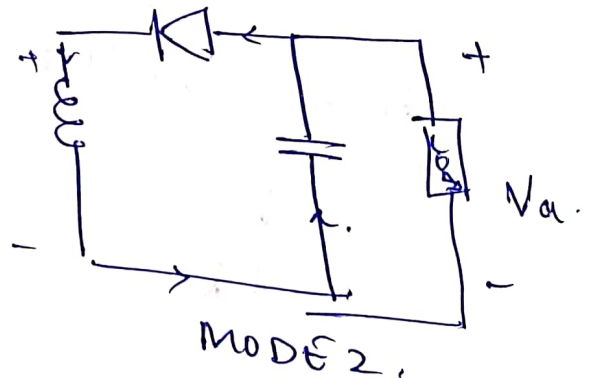
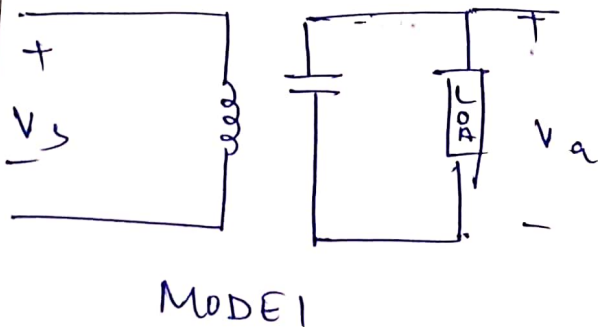
$$C = \frac{k}{2fR}$$

6. Buck-Boost regulator :-

- ⇒ The output voltage can be either more than or less than the input voltage.
- ⇒ The output ~~to~~ polarity is opposite to the input polarity, hence it is also called as an inverting chopper.

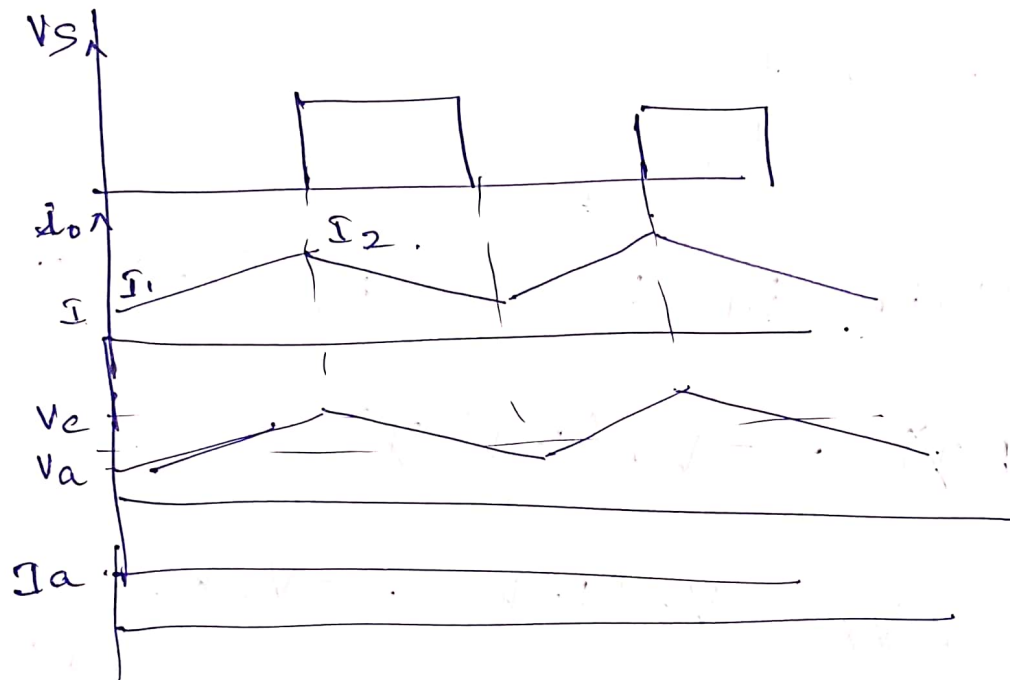


- ⇒ It has two modes of operation.



- ⇒ In mode 1, The Thyristor T_1 is turned on. hence the ~~diode~~ freewheeling diode is reverse biased.

⇒ In mode 2, the thyristor T_1 is turned off. The current starts flowing in the ~~the~~ direction $C \rightarrow D_m \rightarrow$ ~~the~~ L . As energy is stored in L . Hence an output is generated.



⇒ Derivation

Consider, current increases linearly in inductor.

$$V_s = L \frac{\Delta I}{t_1} \quad \rightarrow \textcircled{1}$$

Consider current decreases linearly in the inductor.

$$V_a = -L \frac{\Delta I}{t_2} \quad \rightarrow \textcircled{2}$$



From ① & ②. We get

$$\Delta I = \frac{V_s t_1}{K} = \frac{-V_a t_2}{K}$$

$$V_a = -V_s \frac{t_1}{t_2}$$

Substitute $t_1 = kT$ & $t_2 = (1-k)T$.

$$V_s (kT) = -V_a (1-k)T$$

~~$V_a = V_s$~~ $V_a(1-k) = -V_s k$

$$= V_a = \frac{-V_s k}{1-k}$$

$$V_a - V_a k = -V_s k$$

$$V_a = (V_a - V_s) k$$

$$k = \frac{V_a}{V_a - V_s}$$

Time period

$$T = t_1 + t_2$$

$$T = \frac{L \Delta I}{V_s} - \frac{L \Delta I}{V_a}$$

$$= \cancel{V_a} \frac{L \Delta I}{V_s} + \frac{L \Delta I}{V_s \frac{k}{(1-k)}}$$

$$= \frac{L \Delta I}{V_s} + \frac{L \Delta I (1-k)}{V_s \cdot k}$$

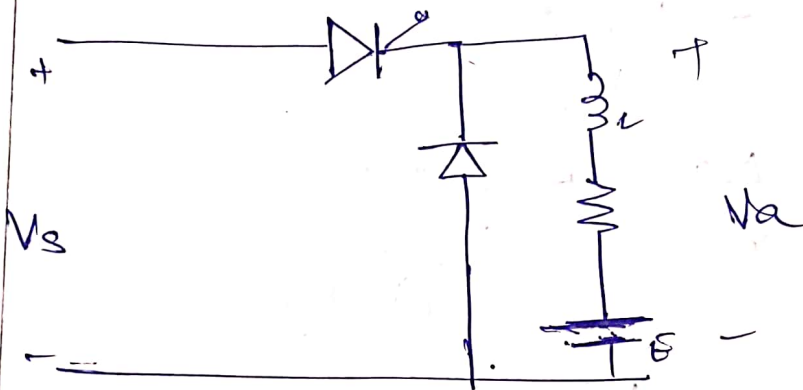
$$T = \frac{L \Delta I}{V_s} \left[1 + \frac{(1-k)}{k} \right]$$

$$T = \frac{L \Delta I}{V_s} \left[\frac{k + 1 - k}{k} \right]$$

$$\Delta I = \frac{V_s \cdot T \cdot k}{L}$$

$$\Delta I = \frac{V_s \cdot k}{L \cdot f}$$

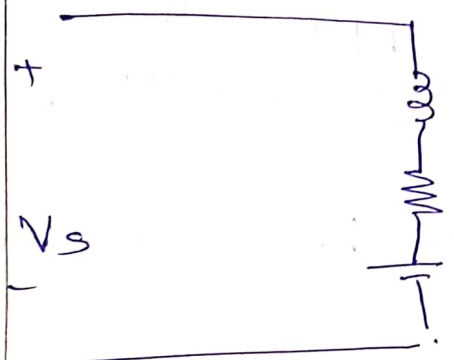
2. Step down chopper. having RL load.



→ In Step down chopper;

- ⇒ Choppers are static devices that are used to convert DC into varying/pulsating DC
- ⇒ A step down chopper, the output voltage is less than the input voltage.
- ⇒ An alternating DC voltage can be obtained by either
 - Varying T_{ON}
 - Varying the chopper frequency keeping constant T_{ON} or T_{OFF}

- ⇒ The Thyristor acts as a switch.
- ⇒ When it is turned on, it acts as a short circuit and the output follows the input.



⇒ Current flows through the inductor and it gets charged.

⇒ Continuous load current.

- ⇒ The chopper is switched ON, current flows through the load, the free wheeling diode is reverse biased and the current increases from i_1 to i_2 in the time period t_1 to t_2 .

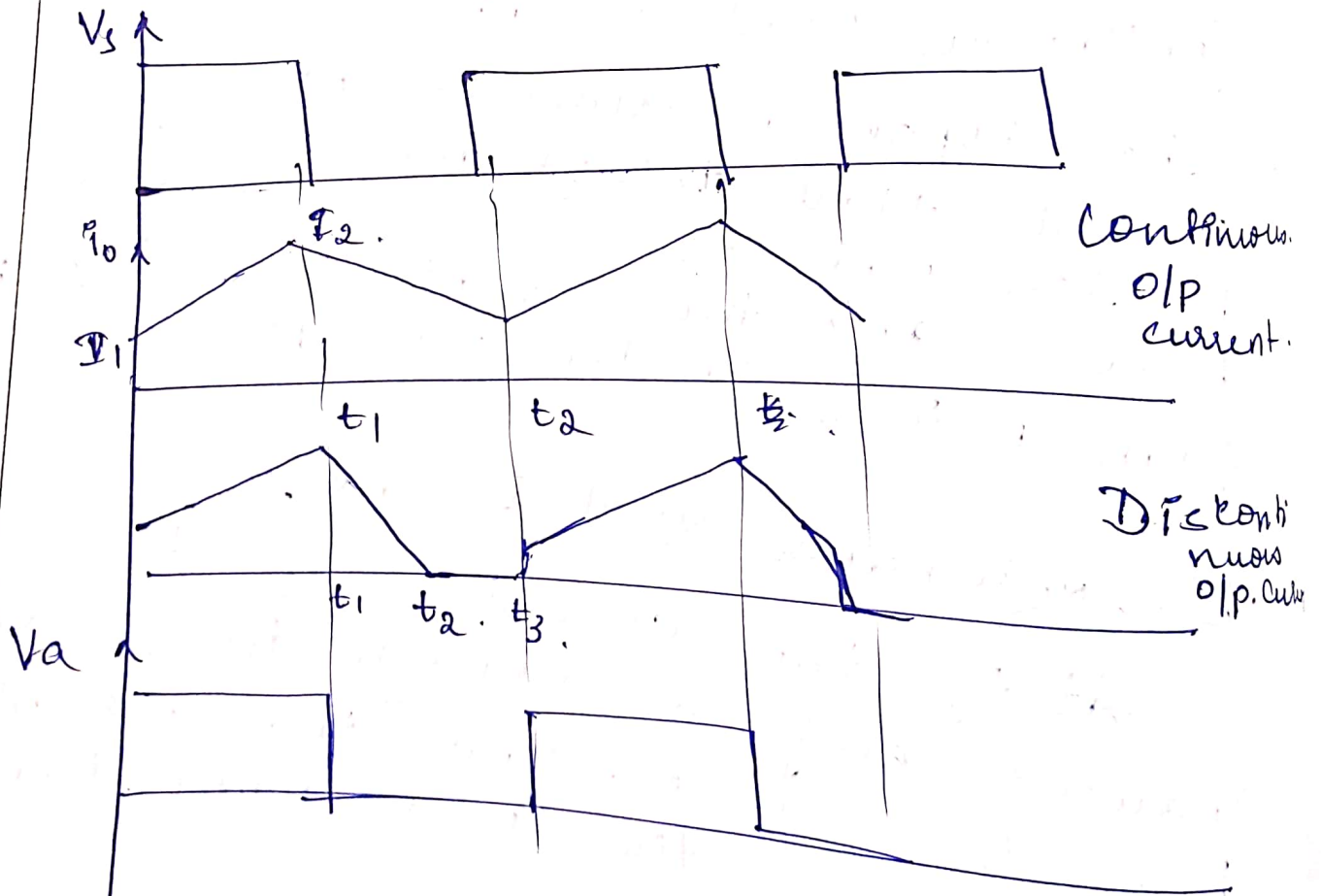
~~Discontinuous load current.~~

At t_2 the current is i_2 , the induced emf is enough to forward bias the diode and the current flows through the load, until the emf becomes zero.

Discontinuous Load current

⇒ If the Inductor has a very small value of Inductance, then during the OFF-period of the chopper, the induced emf will discharge faster from $(t_1 \text{ to } t_2)$

⇒ The output voltage will be zero for the time $t_2 - t_3$



~~$$V_a = V_s \left(\frac{T_{ON}}{T_{ON} + T_{OFF}} \right)$$~~

$$V_a = V_s \left(\frac{T_{ON}}{T_{ON} + T_{OFF}} \right)$$

$$V_{rms} = \sqrt{d} V_s$$

$$I_{avg} = \frac{V_{avg}}{R}$$

5. Classifications.

1. $V_s = 200V$.

$R = 8 \Omega$.

thyristor - 2V.

$f = 800 \text{ Hz}$.

Duty cycle = 0.4.

i) Average output voltage :-

$$V_a = V_s d$$

$$= V_s \left(\frac{t_{ON}}{\text{time period}} \right) = (V_s - 2)$$

$$= \frac{(200 - 2)}{800} \times 0.4$$

$$\boxed{V_a = \cancel{80V}}$$

$$V_a = 79.2$$



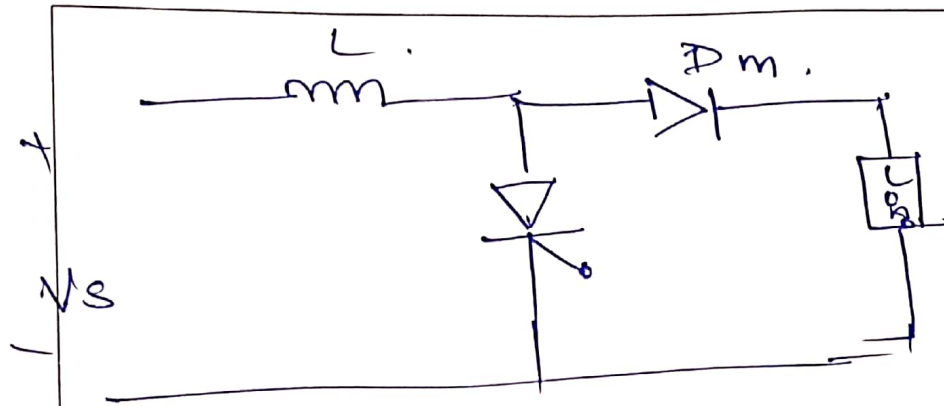
$$\begin{aligned} \text{ii)} \quad V_{\text{rms}} &= \sqrt{d} (V_s \cdot 2) \\ &= \sqrt{0.4 \times (200 \times 2)} = 125.22 \text{ V} \\ &= \cancel{125.49 \text{ V}} \end{aligned}$$

$$\begin{aligned} \text{iii)} \quad \text{Chopper Efficiency} &= \frac{V_a}{V_s} = \frac{79.02}{200} \\ &= 39.6\% \end{aligned}$$

$$\begin{aligned} \cancel{I_{\text{rms}}} \Rightarrow I_{\text{avg}} &= \frac{V_{\text{avg}}}{R} \\ &= \frac{79.02}{8} \\ &= 9.9 \text{ A} \end{aligned}$$

Step Up Chopper

⇒ It is a device whose output voltage is greater than the input voltage.



⇒ When the Chopper is turned ON, the inductor starts charging and stores energy.

⇒ When the Chopper is turned OFF, the inductor is forced to discharge through the load. D_m is forward biased.

⇒
$$V_{\text{out}} = V_s + L \frac{dI}{dt}$$

