

**Internal Assessment Test III – May 2019**

**Sub:** Finite Element Methods  
**Date:** 15/05/2019 **Duration:** 90 mins **Max Marks:** 50 **Sem:** VI  
**Note:** Answer any five questions.

**Code:** 15ME61  
**Branch:** MECH

**Marks**      OBE  
                     CO    RBT

1 Derive the Hermite shape functions for a beam element. 10    CO3    L2

2 For the beam and loading shown in Figure 1, determine  
 i. Slopes at 2 and 3  
 ii. The vertical deflection at the midpoint of the distributed load.  
 Take  $E = 200 \text{ GPa}$ ,  $I = 4 \times 10^6 \text{ mm}^4$ .

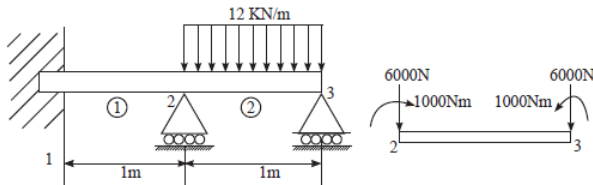


Figure 1

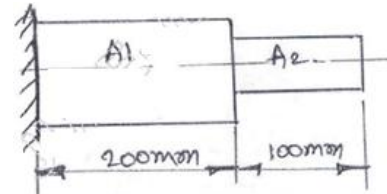


Figure 2

3 Derive torsional stiffness matrix for a circular shaft subjected to pure torsion 10    CO4    L3

4 For a stepped bar shown in figure 2. Determine the eigen values and eigen vector. Take  $A_1 = 400 \text{ mm}^2$ ,  $A_2 = 200 \text{ mm}^2$ ,  $\rho = 7850 \text{ kg/m}^3$ ,  $E = 200 \text{ GPa}$  10    CO4    L3

5 Deduce the governing differential equation for a one dimensional fluid flow through a porous medium 10    CO5    L2

6 For the smooth pipe of variable c/s shown in figure 3. Determine the potential at the junction the velocities in each section of pipe and the volumetric flow rate. The potential at the left end is  $P_1 = 12 \text{ m}^2/\text{s}$  and that at right end is  $P_4 = 3 \text{ m}^2/\text{s}$ . Take  $K_x = 1$

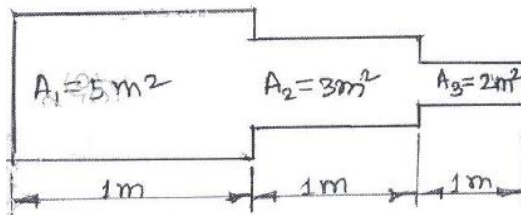


Figure 3

**10**      CO5    L3