Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.

GBGS SCHEME

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20MCA14

First Semester MCA Degree Examination, Jan./Feb. 2021 Mathematical Foundation for Computer Applications

Time: 3 hrs.

Max. Marks: 100

Note: 1. Answer FIVE full questions, choosing ONE full question from each module.
2. Use of Statistical table is permitted.

Module-1

- 1 a. Define a set, empty set and a singleton set with example for each. (04 Marks)
 - b. Define union and intersection of two sets with example. (04 Marks)
 - c. Find the eigen values and eigen vectors of the matrix.

$$\begin{pmatrix}
2 & 1 & -2 \\
1 & 0 & 0 \\
0 & 1 & 0
\end{pmatrix}$$

(12 Marks)

OR

- 2 a. What is the cardinality of a set? Find the cardinality of the sets A and B where $A = \{2, 3, 4, 5, 6, 7, 8, 9, 9\}$ and $B = \{a, e, i, o, u\}$. (04 Marks)
 - b. A total of 1232 students have taken a course in Java, 879 in C and 114 have taken a course in C++. Further 103 have taken courses in both Java and C, 23 have taken courses in both. Java and C++ and 14 have taken courses in both C and C++. If 2092 students have taken atleast one of Java, C and C++, how many students have taken a course in all the three subjects.

 (08 Marks)
 - c. For any three sets A, B, C prove that i) $\overline{A \cup B} = \overline{A} \cap \overline{B}$ ii) $\overline{A \cap B} = \overline{A} \cup \overline{B}$ (06 Marks)
 - d. State and explain Pigeon hole principle.

(02 Marks)

Module-2

3 a. What is a Proposition? Let p and q be the propositions "swimming in the new jersy seashore is allowed and sharks have been near the sea shore". Express each of the following compound propositions as an English sentence.

i) $p \rightarrow \sim g$ ii) $\sim p \rightarrow \sim q$ iii) $p \leftrightarrow q$ (06 Marks)

- b. Write the contra positive, the converse and the inverse of the conditional statement "If the home team wins, then it is raining". (06 Marks)
- c. Show that the compound proposition $[(p \leftrightarrow q) \land (q \leftrightarrow r) \land (r \leftrightarrow p)]$ is logically equivalent to $[(p \to q) \land (q \to r) \land (r \to p)]$. (08 Marks)

OR

- 4 a. Show that the following argument is valid. If Today is Tuesday, I have a test in Mathematics (or) Economics. If my Economics professor is sick, I will not have a test in Economics. Today is Tuesday and my Economics professor is sick. Therefore I have a test in Mathematics.

 (08 Marks)
 - b. Give the proof of the following statement, "If n is an odd integer, then n² is odd using direct and indirect proof method". (07 Marks)
 - c. What is the truth value of $\forall x(x^2 > = x)$,
 - i) If the domain consists of all real numbers.
 - ii) If the domain consists of all integers.

(05 Marks)

Module-3

- 5 a. Let $A = \{1, 2, 3, 4\}$, let $R = \{(1, 3), (1, 1), (3, 1), (1, 2), (3, 3), (4, 4)\}$ be a relation on A. Determine whether R is reflexive, symmetric, anti-symmetric (or) transitive. (08 Marks)
 - b. Give the directed graph of the relation $R = \{(1, 1), (1, 3), (2, 1), (2, 3), (2, 4), (3, 1), (3, 2), (4, 1)\}$ on the set $\{1, 2, 3, 4\}$ (04 Marks)
 - c. Let R₁ and R₂ be the relations represented by the matrices

$$\mathbf{M}_{R_1} = \begin{pmatrix} 1 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} \text{ and } \mathbf{M}_{R_2} = \begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \end{pmatrix}$$

Determine:

i) $R_1 \cup R_2$

 $ii) \ R_1 \cap R_2$

iii) R

iv) R

(08 Marks)

OF

6 a. Discuss briefly on partitions and equivalence classes.

Find the minimum value of K so that $P(X \le 2) > 0.3$.

(08 Marks)

b. Draw the Hasse diagram representing the partial ordering {(a, b)/a divides b} on {1, 2, 3, 4, 6, 8, 12}. (12 Marks)

Module-4

7 a. A random variable X has the following probability distribution:

X 0 1 2 3 4 5 6

P(x) k 3k 5k 7k 9k 11k 13k

- i) Find k
- ii) Evaluate P(X < 4), $P(X \ge 5)$, $P(3 < X \le 6)$.

(11 Marks)

b. The probability that a pen manufactured by a company will be defective is 1/10. If 12 such pens are manufactured find the probability that i) exactly two will be defective ii) at least two will be defective iii) None will be defective. (09 Marks)

OR

8 a. For the probability density function f(x), where

$$f(x) = \begin{cases} x^2/3, & -1 < x < 2 \\ 0, & \text{else where} \end{cases}$$

find F(x) and use it to evaluate $P(0 \le X \le 1)$.

(06 Marks)

- b. The probability that a patient recovers from a rare blood disease is 0.4. If 15 people are known to have contracted the diseases. What is the probability that
 - i) Atleast 10 survive
 - ii) From 3 to 8 survive
 - iii) Exactly 5 survive.

(09 Marks)

- c. Given a standard normal distribution find the value of K such that
 - i) P(z > K) = 0.3015
 - ii) P(K < z < -0.18) = 0.4197

(05 Marks)

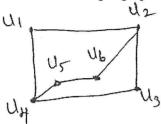
Module-5

- 9 a. Define the following with suitable examples:
 - i) Simple graph
 - ii) Complete graph
 - iii) Bipartite graph
 - iv) Complete bipartite graph.

(06 Marks)

b. Check whether the following 2 graphs are Isomorphic with each other.

(06 Marks)



c. Explain the Konigsberg bridge problem.

VI3

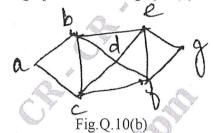
(08 Marks)

OR

- 10 a. Define the terms:
 - i) Hamilton path
 - ii) Eulers path
 - iii) Planar graphs
 - iv) Subgraph of a graph with suitable example for each.

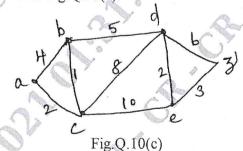
(06 Marks)

b. Give the graph colouring of the graph shown in Fig.Q.10(b).



(04 Marks)

c. Use Dijkstra's algorithm to find the length of a shortest path between the vertices a and z in the graph given below, shown in Fig.Q.10(c).



(10 Marks)