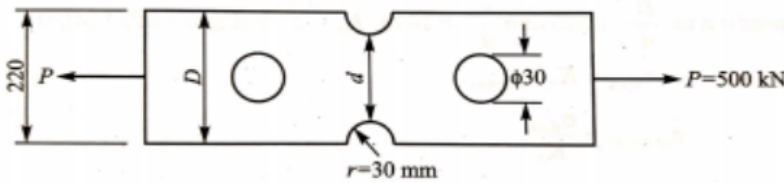


- 2 A mild steel shaft of 60 mm diameter is subjected to a bending moment of 25×10^5 N-mm and a torque M_t . If the yield point of steel in tension is 230 MPa, find the maximum value of this torque without causing yielding of shaft according to
 (i) Maximum principal stress theory of failure
 (ii) Maximum shear stress theory of failure
 (iii) Maximum distortion energy theory of failure
 Adopt a factor of safety of 1.5.

[15]

CO2	L3

- 3 A bar of rectangular cross section is subjected to an axial pull of 500 kN. Calculate its thickness if the allowable tensile stress in the bar is 200 MPa.



[15]

CO2	L3

4. What is stress concentration? Briefly explain the methods of reducing stress concentration.

[5]

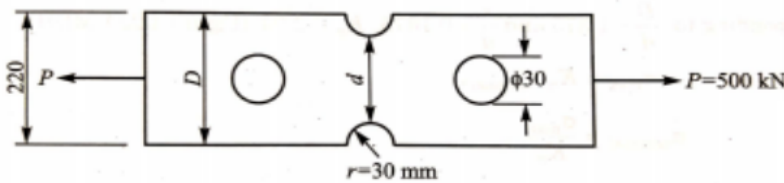
CO2	L3

- 2 A mild steel shaft of 60 mm diameter is subjected to a bending moment of 25×10^5 N-mm and a torque M_t . If the yield point of steel in tension is 230 MPa, find the maximum value of this torque without causing yielding of shaft according to
 (i) Maximum principal stress theory of failure
 (ii) Maximum shear stress theory of failure
 (iii) Maximum distortion energy theory of failure
 Adopt a factor of safety of 1.5.

[15]

CO2	L3

- 3 A bar of rectangular cross section is subjected to an axial pull of 500 kN. Calculate its thickness if the allowable tensile stress in the bar is 200 MPa.



[15]

CO2	L3

4. What is stress concentration? Briefly explain the methods of reducing stress concentration.

[5]

CO2	L3

18MES2 - Design of Machine Elements - I

Scheme of evaluation

Q. No :	Scheme	
1.	Bending Moment- M_b Bending stress $\sigma_b = \sigma_x$ Torque M_t Shear stress $\tau = \tau_{xy}$ $\sigma_1 \rightarrow$ normal stress $\tau_{max} \rightarrow$ Maxin shear stress	2 3 2 3 2 3
2.	(i) Maxin principal stress theory (ii) Maxin shear stress theory (iii) Maxin Distortion Energy theory	5 5 5
3.	<u>Note</u> $\rightarrow K_t, \sigma_{nom}, h$ <u>Hole</u> $\rightarrow K_t, \sigma_{nom}, h$ Recommended thickness	2+2+2 2+2+2 3
4	Definition Methods with sketch	2 3

18MESA → DME-I → solutions for IAT-1

Q no: 1

Bending stress due to load at section AA

$$\sigma_b = \frac{M_b}{I} \times C \quad \text{--- (1)}$$

$$M_b = 12000 \times (60 + 30 + 30) = 144 \times 10^4 \text{ N-mm}$$

$$I = \frac{\pi d^4}{64} = 1.128 \times 10^6 \text{ mm}^4$$

$$C = \frac{d}{2} = 35 \text{ mm}$$

Substituting all the above values in (1)

$$\sigma_b = 42.78 \text{ N/mm}^2$$

Torque M_t due to load is given by

$$M_t = 12000 \times 150 = 1.8 \times 10^6 \text{ N-mm}$$

$$\text{Max shear stress } \tau_{xy} = \frac{16 M_t}{\pi d^3} = 26.72 \text{ N/mm}^2$$

$$\text{Normal stress } \sigma_1 = \frac{1}{2} \left[\sigma_n + \sqrt{\sigma_n^2 + 4\tau_{xy}^2} \right]$$

$$\sigma_1 = 55.6 \text{ N/mm}^2$$

Max shear stress $\tau_{max} = \frac{1}{2} \sqrt{\sigma_x^2 + 4\tau_{xy}^2}$

$\tau_{max} = 34.227 \text{ N/mm}^2$

Min principal stress

$$\sigma_2 = \frac{1}{2} \left[\sigma_x - \sqrt{\sigma_x^2 + 4\tau_{xy}^2} \right]$$

$\sigma_2 = -12.83 \text{ N/mm}^2$

Q no: 2

Data :

$d = 60 \text{ mm}; M_b = 25 \times 10^5 \text{ N-mm}; \sigma_y = 230 \text{ N/mm}^2; \text{FOS} = n = 1.5$

Solution :

From the general expression for bending load (Equation 2.52 Old DDHB; 2.90 New DDHB)

Bending stress $\sigma = \frac{M_b}{I} \cdot c$

$\therefore \sigma = \frac{25 \times 10^5}{\frac{\pi}{64} 60^4} \times \frac{60}{2} = 117.893 \text{ N/mm}^2 = \sigma_x$

From the general expression for torsional load (Equation 2.50 Old DDHB; 2.86 New DDHB)

Torsional shear stress $\tau = \frac{M_t}{J} \cdot r$

$\tau = \frac{M_t}{\frac{\pi}{32} \times 60^4} \times \frac{60}{2} = 2.358 \times 10^{-5} M_t = \tau_{xy}$

$\sigma_y = 0$

Maximum principal stress $\sigma_1 = \frac{\sigma_x}{2} + \sqrt{\left(\frac{\sigma_x}{2}\right)^2 + \tau_{xy}^2} \quad (\because \sigma_y = 0) \quad \text{---- 2.32 (Old DDHB)}$

$= \frac{117.893}{2} + \sqrt{\left(\frac{117.893}{2}\right)^2 + (2.358 \times 10^{-5} M_t)^2}$

$= 58.9465 + \sqrt{3474.69 + 5.56 \times 10^{-10} M_t^2} \quad \text{---- 2.34 (New DDHB)}$

Minimum principal stress $\sigma_2 = \frac{\sigma_x}{2} - \sqrt{\left(\frac{\sigma_x}{2}\right)^2 + \tau_{xy}^2} \quad (\because \sigma_y = 0) \quad \text{---- 2.33 (Old DDHB)}$

$= \frac{117.893}{2} - \sqrt{\left(\frac{117.893}{2}\right)^2 + (2.358 \times 10^{-5} M_t)^2}$

$$= 58.9465 - \sqrt{3474.69 + 5.56 \times 10^{-10} M_t^2}$$

(i) **Maximum principal stress theory**

Since $\sigma_1 > \sigma_2$, the design equation is $\sigma_1 = \frac{\sigma_{yt}}{n}$

$$\therefore 58.9465 + \sqrt{3474.69 + 5.56 \times 10^{-10} M_t^2} = \frac{230}{1.5}$$

$$\therefore \text{Maximum torque } M_t = 3.1263 \times 10^6 \text{ N-mm} = 3.1263 \text{ kN-m}$$

(ii) **Maximum shear stress theory**

For bi-axial stress state system τ_{\max} is the largest among the three values of $\frac{\sigma_1 - \sigma_2}{2}$, $\frac{\sigma_1}{2}$ and $\frac{\sigma_2}{2}$.

Since σ_1 and σ_2 are of opposite sign,

$$\tau_{\max} = \frac{\sigma_1 - \sigma_2}{2} = \sqrt{3474.69 + 5.56 \times 10^{-10} M_t^2}$$

The design equation is, $\tau_{\max} = \frac{\tau_y}{\text{FOS}} = \frac{\sigma_{yt}}{2 \times \text{FOS}}$

$$\therefore \sqrt{3474.69 + 5.56 \times 10^{-10} M_t^2} = \frac{230}{2 \times 1.5}$$

$$\therefore \text{Maximum torque } M_t = 2.079 \times 10^6 \text{ N-mm} = 2.079 \text{ kN-m}$$

(iii) **Maximum distortion energy theory**

According to this theory, the design equation for bi-axial stress state system is,

$$\left(\frac{\sigma_{yt}}{n} \right)^2 = \sigma_1^2 + \sigma_2^2 - \sigma_1 \sigma_2$$

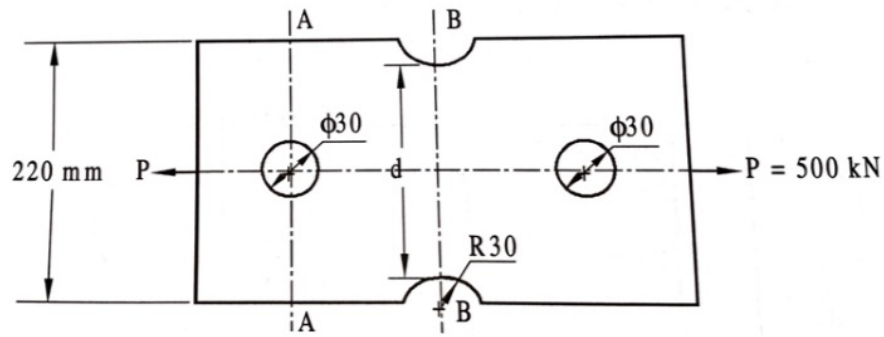
$$\text{i.e., } \left(\frac{230}{1.5} \right)^2 = \left\{ 58.9465 + \sqrt{3474.69 + 5.56 \times 10^{-10} M_t^2} \right\}^2 + \left\{ 58.9465 - \sqrt{3474.69 + 5.56 \times 10^{-10} M_t^2} \right\}^2 - \left\{ 58.9465 + \sqrt{3474.69 + 5.56 \times 10^{-10} M_t^2} \right\} \left\{ 58.9465 - \sqrt{3474.69 + 5.56 \times 10^{-10} M_t^2} \right\}$$

$$\text{i.e., } \left(\frac{230}{1.5} \right)^2 = 2(58.9465^2 + 3474.69 + 5.56 \times 10^{-10} M_t^2) - \{ 58.9465^2 - (3474.69 + 5.56 \times 10^{-10} M_t^2) \}$$

$$= 58.9465^2 + 3 \times 3474.69 + 3 \times 5.56 \times 10^{-10} M_t^2$$

$$\therefore \text{Maximum torque } M_t = 2.4 \times 10^6 \text{ N-mm} = 2.4 \text{ kN-m}$$

3)



Given:

Allowable tensile stress $\sigma_{max} = 200 \text{ MPa}$

Solution:

At section A-A, there is a hole and at section B-B, there is a notch.

To find: Thickness of the plate, h

Consider Section A-A:

Axial Load: $F = 500 \text{ kN} = 500 \times 10^3 \text{ N}$

Width of the plate $w = 220 \text{ mm}$

Diameter of the hole, d or a = 30 mm

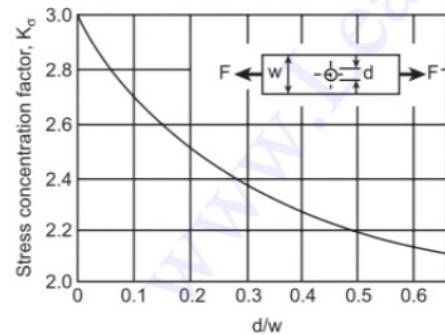
$$\therefore \frac{d}{w} = \frac{a}{w} = \frac{30}{220} = 0.1364$$

from Fig. 4.5 (DHB), for $\frac{d}{w} = 0.1364$

stress concentration factor, $K_\sigma = 2.65$

$$\sigma_{nom} = \frac{F}{(w-d)h}$$

$$\sigma_{nom} = \frac{500 \times 10^3}{(220 - 30)h} \text{ ---> (1)}$$



$$K_\sigma = \frac{\sigma_{max}}{\sigma_{nom}} ; \sigma_{nom} = \frac{F}{(w-d)h}$$

FIGURE 4-5 Reproduced with permission. Stress-concentration factor for a plate of finite width with a circular hole (cut-out) in tension. ("Design Factors for Stress Concentration," *Machine Design*, Vol. 23, Nos. 2 to 7, 1951.)

$$K_{\sigma} = \frac{\sigma_{max}}{\sigma_{nominal}} \Rightarrow$$

$$2.65 = \frac{200}{\sigma_{nom}} \Rightarrow$$

$$\sigma_{nom} = 75.472 \text{ N/mm}^2$$

From (1)

$$\frac{500 \times 10^3}{(220 - 30)h} = 75.472$$

$$h = 34.868 \text{ mm}$$

Consider section B-B

$$r = 30 \text{ mm}$$

$$d = w - 2r = 220 - 2(30) = 160 \text{ mm}$$

$$\frac{r}{d} = \frac{30}{160} = 0.1875$$

$$\frac{D}{d} = \frac{220}{160} = 1.375$$

from Fig 4.22 (DDB)., corresponding to $\frac{r}{d} = 0.1875$ and $\frac{D}{d} = 1.375$,

$$K_{\sigma} = 2.1$$

$$\text{Now, } K_{\sigma} = \frac{\sigma_{max}}{\sigma_{nom}} \Rightarrow 2.1 = \frac{200}{\sigma_{nom}} \Rightarrow \sigma_{nom} = 95.24 \text{ N/mm}^2$$

Also,

$$\sigma_{nom} = \frac{F}{A} = \frac{F}{h \cdot d}$$

$$95.24 = \frac{500 \times 10^3}{h \times 160}$$

$$h = 32.81 \text{ mm}$$

Thickness of the plate = $34.868 \approx 35 \text{ mm}$ (Choose the larger value)

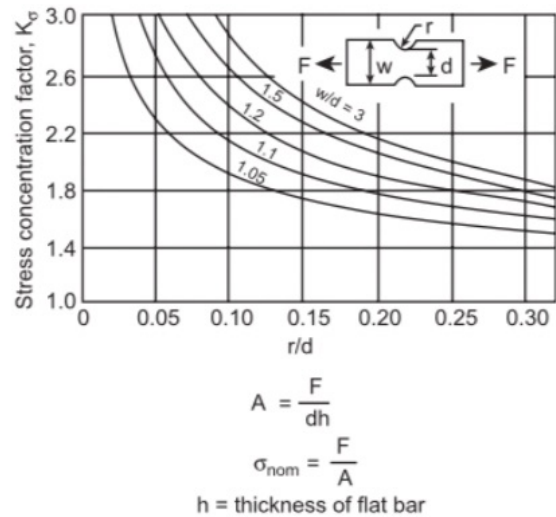
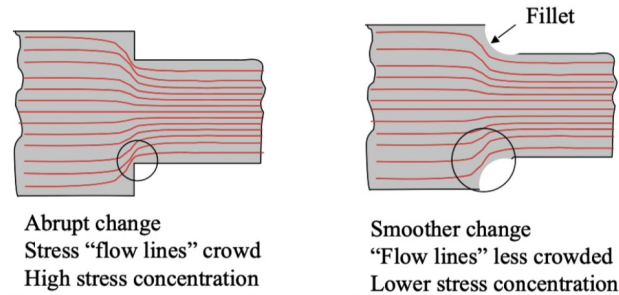


FIGURE 4-22 Reproduced with permission. Stress-concentri

4) Stress concentration is defined as any localization of maximum stress due to irregularities in cross section or any abrupt change in cross section. Any such discontinuity will affect the stress distribution in the neighbourhood and the discontinuity will act as a stress raiser.



Causes of stress concentration

- Geometric discontinuities such as holes, notches, fillets, grooves, keyways, threads etc.
- Internal defects such as cracks, voids, non-metallic inclusions etc
- Load Discontinuities
- Material discontinuities