



2. State and explain unification algorithm Unify(L1,L2).

[10]

If  $L1$  or  $L2$  are both variables or constants, then:

- (a) If  $L1$  and  $L2$  are identical, then return NIL.
- (b) Else if  $L1$  is a variable, then if  $L1$  occurs in  $L2$  then return {FAIL}, else return  $(L2/L1)$ .
- (c) Else if  $L2$  is a variable then if  $L2$  occurs in  $L1$  then return {FAIL}, else return  $(L1/L2)$ .
- (d) Else return {FAIL}.

2. If the initial predicate symbols in  $L1$  and  $L2$  are not identical, then return {FAIL}.

3. If  $L1$  and  $L2$  have a different number of arguments, then return {FAIL}.

4. Set  $SUBST$  to NIL.

5. For  $i \leftarrow 1$  to number of arguments in  $L1$ :

- (a) Call Unify with the  $i$ th argument of  $L1$  and the  $i$ th argument of  $L2$ , putting result in  $S$ .
- (b) If  $S$  contains FAIL then return {FAIL}.
- (c) If  $S$  is not equal to NIL then:
  - (i) Apply  $S$  to the remainder of both  $L1$  and  $L2$ .
  - (ii)  $SUBST := APPEND(S, SUBST)$ .

6. Return  $SUBST$ .

3. Write the algorithm for conversion of a first order logic formula to clause form.

[10]

Algorithm : Convert to Clause Form

1. Eliminate  $\rightarrow$ , using:  $a \rightarrow b = \neg a \vee b$ .
2. Reduce the scope of each  $\neg$  to a single term, using:
  - $\neg(\neg p) = p$
  - deMorgan's laws:  $\neg(a \wedge b) = \neg a \vee \neg b$   
 $\neg(a \vee b) = \neg a \wedge \neg b$
  - $\neg\forall x : P(x) = \exists x : \neg P(x)$
  - $\neg\exists x : P(x) = \forall x : \neg P(x)$
3. Standardize variables.
4. Move all quantifiers to the left of the formula without changing their relative order.
5. Eliminate existential quantifiers by inserting Skolem functions.
6. Drop the prefix.
7. Convert the matrix into a conjunction of disjuncts, using associativity and distributivity.
8. Create a separate clause for each conjunct.
9. Standardize apart the variables in the set of clauses generated in step 8, using the fact that  
 $(\forall x : P(x) \wedge Q(x)) = \forall x : P(x) \wedge \forall x : Q(x)$

4a. Explain Resolution Algorithm for First Order Logic. [06]

Convert all the statements of  $F$  to clause form.

2. Negate  $P$  and convert the result to clause form. Add it to the set of clauses obtained in 1.

3. Repeat until either a contradiction is found, no progress can be made, or a predetermined amount of effort has been expended.

Select two clauses. Call these the parent clauses.

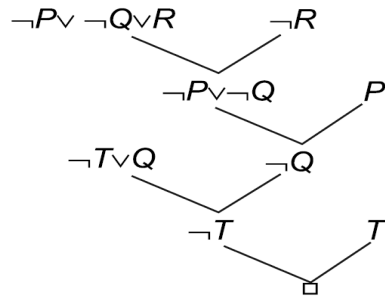
Resolve them together. The resolvent will be the disjunction of all the literals of both parent clauses with appropriate substitutions performed and with the following exception: If there is one pair of literals  $T_1$  and  $\neg T_2$  such that one of the parent clauses contains  $T_2$  and the other contains  $T_1$  and if  $T_1$  and  $T_2$  are unifiable, then neither  $T_1$  nor  $T_2$  should appear in the resolvent. If there is more than one pair of complimentary literals, only one pair should be omitted from the resolvent.

If the resolvent is the empty clause, then a contradiction has been found. If it is not, then add it to the set of clauses available to the procedure.

4b. Given the following axioms: [04]

$P$   
 $(P \wedge Q) \rightarrow R$   
 $(S \vee T) \rightarrow Q$   
 $\neg T$

Where  $P, Q, R, S, T$  are propositions, Prove that  $R$  is true using Resolution.



5 (a) Explain the limitations of close world assumption [05]

The CWA says that only objects that satisfy any predicate are those that must.

CWA can fail to produce an appropriate answer for either of the two reasons:

a) The assumptions are not true in the real world. CWA will yield appropriate results exactly to the extent that the assumptions that all the relevant positive facts are present in the knowledge base is true.

b) CWA is purely syntactic reasoning process.

$A(\text{Joe}) \text{ OR } B(\text{Joe})$

We can include NOT  $A(\text{Joe})$

We cannot include NOT  $B(\text{Joe})$ , as that would lead to a contradiction.

5 (b) Explain Bayes Theorem. [05]

$P(H_i | E)$  = the probability that hypothesis  $H_i$  is true given evidence  $E$

$P(E | H_i)$  = the probability that we will observe evidence  $E$  given that hypothesis  $i$  is true

$P(H_i)$  = the *a priori* probability that hypothesis  $i$  is true in the absence of any specific evidence. These probabilities are called prior probabilities or *prlors*.

$k$  = the number of possible hypotheses

Bayes' theorem then states that

$$P(H_i | E) = \frac{P(E | H_i) \cdot P(H_i)}{\sum_{n=1}^k P(E | H_n) \cdot P(H_n)}$$

6 Explain justification based truth maintenance system.

[10]

If we want to derive a fact F, which cannot be derived monotonically from what we know, then we derive F on the basis of an assumption A.

Later a new fact comes, which invalidates A.

In non-monotonic reasoning, it is necessary to have dependency based backtracking

Dependency based backtracking is implemented by adding justifications at each node.

Each justification corresponds to the process that led to the node.

A TMS provides a problem solver system with both assertions and dependencies among assertions.

Each justification consists of two parts: IN list and OUT list

Assertions in IN list are connected to justifications by a +

Assertions in OUT list are connected to justifications by a -

Assertions in a TMS network are believed, when they have valid justification.

A justification is valid, if every assertion in the IN list is believed and none in the OUT list is.

