

# CBBCS SCHEME

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## Fifth Semester B.E. Degree Examination, Feb./Mar. 2022

### Automata Theory and Computability

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

#### Module-1

- Define the following terms with examples :
    - Alphabet
    - String
    - Language
    - Concatenation at Languages
    - Power of an Alphabet. (10 Marks)
  - Define DFSM. Design DFSM
    - To accept strings having Even number of a's and even number b's
    - To accept binary numbers divisible by 5. (10 Marks)

OR

- Convert the following NDFSM of DFSM, [Refer Fig Q2(a)].

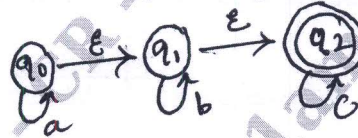


Fig Q2(a)

(08 Marks)

- Minimize the following DFSM by identifying Distinguishable and Non-distinguishable states.

	$\delta$	0	1
A	B	F	
B	G	C	
C	A	C	
D	C	G	
E	H	F	
F	C	G	
G	G	F	
H	G	C	

(12 Marks)

#### Module-2

- Define Regular Expression. Write RE for the following Languages. (10 Marks)
    - Strings of 0's and 1's ending with three consecutive zeroes.
    - Strings of a's and b's having substring aa.
  - Write DFSM to accept intersection of Languages  $L_1 = (a + b)^* a$  and  $L_2 = (a + b)^* b$  (10 Marks)

OR

- Using Kleen's theorem, prove that for any Regular Expression R, there exists a finite automata  $M = (Q, \Sigma, \delta, q_0, F)$  which accepts  $L(R)$ . (10 Marks)
  - State and prove pumping Lemma for Regular Languages. Show that the Language  $L = \{ww^r : w \in (0, 1)^*\}$  is not regular. (10 Marks)

Module-3

- 5 a. Define Context Free Grammar. Design CFG for the following Languages.  
 i)  $L_1 = \{w : |w| \text{ Mod } 3 = 0\}$  over  $\Sigma = \{a\}$   
 ii)  $L_2 = \{a^n b^m c^k : m = n + k\}$  over  $\Sigma = \{a, b, c\}$  (10 Marks)
- b. Define Ambiguity. Consider the grammar  
 $E \rightarrow E + E \mid E * E \mid (E) \mid id$   
 Find Leftmost and Rightmost derivations and parse tree for the string  $id + id * id$ , show that the grammar is ambiguous. (10 Marks)

OR

- 6 a. What is Chomsky Normal Form of CFG? Convert the following grammar to CNF.  
 $S \rightarrow ABC \mid BaB$   
 $A \rightarrow aA \mid BaC \mid aaa$   
 $B \rightarrow bBb \mid a \mid D$   
 $C \rightarrow CA \mid AC$   
 $D \rightarrow \epsilon$   
 Eliminate  $\epsilon$ - productions, Unit productions and useless symbols if any before conversion. (10 Marks)
- b. What is NPDA? Design NPDA for Language  $L = \{a^n b^n \mid n \geq 1\}$ . Draw transition diagram. Write sequence of moves made by NPDA to accept the string  $aaabbb$ . (10 Marks)

Module-4

- 7 a. Design TM for  $WCW^R$  over  $\Sigma = \{0, 1\}$ . Write transition diagram, and ID for  $w = 101C101$  (14 Marks)
- b. Explain : i) Multitape ii) Non-deterministic TM (06 Marks)

OR

- 8 a. Define Turning Machine. Explain the working of Turning Machine. (06 Marks)
- b. Design Turning machine to accept the Language  $L = \{0^n 1^n 2^n \mid n \geq 0\}$ . Draw the transition diagram. Write sequence of moves made by TM for string  $001122$ . (14 Marks)

Module-5

- 9 a. Explain Halting problem in Turning machine. (07 Marks)
- b. Write applications of Turning Machine. (06 Marks)
- c. Explain Recursively Enumerable Languages. (07 Marks)

OR

- 10 a. Explain Quantum Computers. (07 Marks)
- b. Explain P and NP classes. (07 Marks)
- c. Explain Church Turning Thesis. (06 Marks)

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