## Sixth Semester B.E. Degree Examination, Feb./Mar. 2022

## Digital Signal Processing

Time: 3 hrs. ORE

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

## Module-1

1 a. Compute 4-point DFT of an input sequence :  $x(n) = \cos\left(\frac{n\pi}{4}\right)$  and plot its magnitude and

b. Obtain the linear convolution of the sequences  $x(n) = \{1, 2, -1, 2, 3, -2, -3, -1, 1, 1, 2, -1\}$  and  $h(n) = \{1, 2\}$ , using overlap save method with 4 -point circular convolution. (10 Marks)

OR

- 2 a. Find the circular convolution of input sequence  $x(n) = \{1, 2, 3, 4\}$  with impulse response  $h(n) = \{2, 1, 2, 1\}$  using Stockham's method. (07 Marks)
  - b. State and prove circular time shifting property of Discrete Fourier transform. (03 Marks)
  - c. X(k) is a 14-point DFT of the sequence x(n), the first 8-samples of X(k) are given as: X(0) = 12; X(1) = (-1 + j3); X(2) = (3 + j4); X(3) = (1 j5) X(4) = (-2 + j2); X(5) = (6 + j3) X(6) = (2 j3); X(7) = 10. Compute the remaining samples of X(k) and find the value of  $\sum_{i=1}^{13} |x(n)|^2$ . (06 Marks)

Module-2

- a. Show that FFT is computationally efficient than direct computation of DFT. (04 Marks)
  - b. What are the similarities and differences between DIT and DIF algorithms of FFT?

(04 Marks)

c. Compute 8-point DFT of the sequence x(n) = {1, 1, 1, 1} using Radix - 2 DIT - FFT algorithm. (08 Marks)

OR

4 a. If  $x_1(n) = \{1, 2, 0, 1\}$  and  $x_2(n) = \{1, 3, 3, 1\}$ , obtain the circular convolution of  $x_1(n)$  and  $x_2(n)$  using Radix -2 DIT - FFT algorithm. (08 Marks)

b. If DFT X(k) is given as:

 $X(k) = \{0, 2\sqrt{2}(1-j), 0, 0, 0, 0, 2\sqrt{2}(1+j)\}$ , determine the corresponding time sequence x(n) and draw the signal flow graph with all intermediate results, using inverse Radix -2 DIF – FFT algorithm. (08 Marks)

## Module-3

5 a. The system function of an along filter is given as:  $H_a(s) = \frac{s + 0.1}{(s + 0.1)^2 + 9}$ . Obtain the system

function of the HR digital filter using impulse invariance method. (06 Marks)

b. Design an analog filter with maximally flat response in the passband and an acceptable attenuation of -2dB at 20 radians/sec. The attenuation in the stopband should be more than 10dB beyond 30 radians/sec. (10 Marks)

OR

- 6 a. Design a lowpass 1rad/sec bandwidth Chebyshev filter with an acceptable passband ripple of 2dB, cut-off frequency of 1 rad/sec and stopband attenuation of 20dB or greater beyond 1.3 rad/sec. (10 Marks)
  - b. Use Bilinear transformation to design a fist order lowpass Butterworth filter that has a 3dB cut-off frequency at  $W_c = 0.2\pi$ . The normalized filter is given as:

$$H_{an}(s) = \frac{1}{s+1}.$$
 (06 Marks)

Module-4

- 7 a. Design a digital lowpass filter using Chebyshev filter design procedure that meets the following specifications: passband magnitude characteristics that is constant to 1dB for frequencies below  $w = 0.2\pi$  and stopband attenuation of at least 15dB for frequencies between  $w = 0.3\pi$  and  $\pi$ . Use Bilinear transformation. (10 Marks)
  - b. Obtain the general realization of parallel form for an IIR system. (06 Marks)

OR

8 a. Design a Chebyshev filter for the following specifications using impulse invariance method.  $0.8 \le |H(e^{j\omega})| \le 1$  for  $0 \le \omega \le 0.2\pi$ 

$$|H(e^{j\omega})| \le 1$$
 for  $0 \le \omega \le 0.2\pi$   
 $|H(e^{j\omega})| \le 0.2$  for  $0.6\pi \le \omega \le \pi$  (12 Marks)

b. A difference equation describing a filter is given as

$$y(n) - \frac{3}{4}y(n-1) + \frac{1}{8}y(n-2) = x(n)\frac{1}{2}x(n-1)$$

Draw Direct form – I and Direct form – II structures for an IIR system. (04 Marks)

Module-5

- 9 a. Design a normalized linear phase FIR filter having the phase delay of  $\tau = 4$  and at least 40dB attenuation in the stopband. Also obtain the magnitude/frequency response of the filter.

  (12 Marks)
  - b. Obtain the cascade realization of the system function:

$$H(z) = 1 + \frac{5}{2}z^{-1} + 2z^{-2} + 2z^{-3}$$
. (04 Marks)

OR

- 10 a. Design a low pass FIR filter using frequency sampling technique having cut-off frequency of  $\frac{\pi}{2}$  rad/sample. The filter should have a linear phase with length M = 17. (12 Marks)
  - b. Determine the direct form realization of the system function:  $H(z) = 1 + 2z^{-1} - 3z^{-2} - 4z^{-3} + 5z^{-4}.$ (04 Marks)