

18EE63

Sixth Semester B.E. Degree Examination, Feb./Mar. 2022

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Digital Signal Processing

Time: 3 hrs.

Digital Signal Processing

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

# Module-1

- 1 a. Prove the following properties of DFT.
  - i) Linearity ii) circular item shift.

(06 Marks)

b. Compute N-point DFT of  $x(n) = a^n$  for  $0 \le n \le N - 1$ .

(04 Marks)

c. Compute 6-point DFT of the sequence  $x(n) = \{4, 3, 2, 1, 0, 0\}$ . Also plot magnitude and phase spectrum. (10 Marks)

#### OR

- a. Compute the circular convolution using DFT and IDFT for the following sequences  $x_1(n) = \{2, 1, 2, 1\}$  and  $x_2(n) = \{1, 2, 3, 4\}$ . (10 Marks)
  - b. A long sequence x(n) is filtered through a filter with impulse response h(n) to yield to output y(n). If  $x(n) = \{1, 4, 3, 0, 7, 4, -7, -7, -1, 3, 4, 3\}$  and  $h(n) = \{1, 2\}$ . Compute y(n) using overlap add technique. Use only a 5-point circular convolution in your approach. (10 Marks)

# Module-2

- 3 a. Develop an 8-point DIT FFT algorithm starting from the equation of DFT and also draw signal flow graph. (10 Marks)
  - b. Obtain 8-point DFT of the following sequence using radix -2 DIF-FFT algorithm.  $x(n) = \{2, 1, 2, 1\}.$  (10 Marks)

#### OR

- 4 a. First five points of the 8-point DFT of a real valued sequence is given by X(0) = 0, X(1) = 2 + j2, X(2) = -j4, X(3) = 2 j2, X(4) = 0. Determine the remaining points. Hence find the original sequence x(n) using DIF-FFT algorithm. (14 Marks)
  - b. Tabulate the number of complex multiplications and complex additions required for the direct computation of DFT and FFT algorithm for N = 8, 16, 32. (06 Marks)

### Module-3

- 5 a. Design an analog bandpass filter to meet the following frequency domain specifications:
  - i) a 3.0103dB upper and lower cut-off frequency of 50Hz and 20KHz
  - ii) a stopband attenuation of atleast 20dB and 20Hz and 45KHz
  - iii) a monotic frequency response.

(10 Marks)

b. Design a Chebyshev analog lowpass filter that has a -3dB cut-off frequency of 100rad/sec and a stopband attenuation of 25dB or greater for all radian frequencies past 250 rad/sec.

(10 Marks)

#### OR

- 6 a. Determine the system function H(z) of the lowest order Chebyshev filter that meets the following specifications:
  - i) 3dB ripple in the passband  $0 \le |\omega| \le 0.3\pi$
  - ii) Atleast 20dB attenuation in the stopband  $0.6\pi \le |\omega| \le \pi$  Use the bilinear transformation.

(10 Marks)

b. Transform the analog filter  $H_a(s) = \frac{(s+1)}{s^2 + 5s + 6}$  into H(z) using impulse invariant transformation take T = 0.1 sec. (10 Marks)

## Module-4

a. A Chebyshev – I filter of order N=3 and unit band width is known to have a pole at s=-1

i) Find the two other poles of the filter and parameter  $\varepsilon$ 

ii) The analog filter is mapped to the z-domain using the bilinear transformation with T = 2. (10 Marks) Find the transfer function H(z) of the digital filter.

b. Design a digital Chebyshev-I filter that satisfies the following constraints:

$$0.8 \le |H(\omega)| \le 1$$
  $0 \le \omega \le 0.2\pi$   
 $|H(\omega)| \le 0.2$   $0.6 \le \omega \le \pi$ 

Use impulse invariant transformation.

(10 Marks)

# OR

Obtain the direct form-I, direct form-II, cascade and parallel form realization for the 8 following system:

$$y(n) = 0.75y(n-1) - 0.125y(n-2) + 6x(n) + 7x(n-1) + x(n-2).$$
 (20 Marks)

Module-5
A low pass filter is to be designed with the following desired frequency response

$$H_{d}(e^{j\omega}) = H_{d}(\omega) = \begin{cases} e^{-j2\omega}, & |\omega| < \frac{\pi}{4} \\ 0, & \frac{\pi}{4} < |\omega| < \pi \end{cases}$$

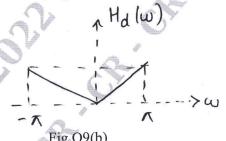
Determine the filter co-efficient  $h_d(n)$  and h(n) if  $\omega(n)$  is a rectangular window defined as

$$\omega_{R}(n) = \begin{cases} 1, & 0 \le n \le 4 \\ 0, & \text{otherwise} \end{cases}$$

Also find the frequency response  $H(\omega)$  of the resulting filter.

(10 Marks)

b. Use the window method with a hamming window to design a 7-tap differentiator. The magnitude response of an ideal differentiator is shown in Fig.Q9(b). Compute and plot the magnitude response of the resulting FIR differentiator.



(10 Marks)

Determine the impulse response h(n) of a filter having desired frequency response :

$$H_{d}(e^{j\omega}) = \begin{cases} e^{-j(N-1)\varpi/2} & \text{for } 0 \le |\omega| \le \pi/2 \\ 0, & \text{for } \pi/2 \le |\omega| \le \pi \end{cases}$$

N = 7. Use frequency sampling approach.

(12 Marks)

b. Obtain direct form and cascade form realization of the system function:

$$H(z) = 1 + \frac{5}{2}z^{-1} + 2z^{-2} + 2z^{-3}$$
. (08 Marks)