18EC52

Fifth Semester B.E. Degree Examination, Feb./Mar.2022

Digital Signal Processing

Time: 3 hrs

Max. Marks: 100

BANG Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- Prove that the sampling of DTFT of a sequence x(n) result in N-point DFT with a neat 1 diagram. (10 Marks)
 - Find the 4-point DFT of the sequence $x(n) = \{1, 0, 0, 1\}$ using matrix method and verify the answer by taking the 4-point IDFT of the result. (10 Marks)

- (06 Marks) Derive the circular Time shift property.
 - Compute the circular convolution of the following sequences using DFT and IDFT method $x_1(n) = \{1, 2, 3, 4\}$ and $x_2(n) = \{4, 3, 2, 1\}$. (09 Marks)
 - $W(n) = \frac{1}{2} + \frac{1}{2}\cos\left|\frac{2\pi}{N}\left(n \frac{N}{2}\right)\right|$, what is the DFT of the window sequence y(n) = x(n).w(n)? Relate the answer in terms of X(K). (05 Marks)

- Find the output y(n) of a filter whose impulse response is $h(n) = \{1, 1, 1\}$ and the input signal $x(n) = \{3, -1, 0, 1, 3, 2, 0, 1, 2, 1\}$ using overlap-add method. Assume the length of each block N is 6.
 - What do you mean by computational complexity? Compare the direct computation and FFT algorithms. In the direct computation of 32-point DFT of x(n), How many
 - Complex multiplications
 - Complex additions.
 - (iii) Real multiplications.
 - Real additions and (iv)
 - Trigonometric function evaluations are required.

(10 Marks)

- Develop 8-point DIT-FFT Radix-2 algorithm and draw the signal flow graph. (10 Marks)
 - Given x(n) = n+1 for $0 \le n \le 7$. Find X(K) using DIF-FFT algorithm. (10 Marks)

Module-3

What are the different design techniques available for the FIR filters? Explain Gibbs phenomenon. Explain the four window techniques for the designing of FIR filters.

(10 Marks)

A low pass filter is to be designed with the following desired frequency response,

$$H_{d}(e^{J\omega}) = \begin{cases} e^{-J3\omega} & \text{, for } -\frac{3\pi}{4} \leq \omega \leq \frac{3\pi}{4} \\ 0 & \text{, } \frac{3\pi}{4} \leq \omega \leq \pi \end{cases}$$

Determine $H(e^{J\omega})$ for M = 7 using Hamming window.

(10 Marks)

6 a. A FIR filter is given by,

$$y(n) = x(n) + \frac{2}{5}x(n-1) + \frac{3}{4}x(n-2) + \frac{1}{3}x(n-3)$$

Draw the lattice structure.

(10 Marks)

b. Based on the frequency-sampling method, determine the coefficients of a linear-phase FIR filter of length M = 15 which has a symmetric unit sample response and a frequency response that satisfies the conditions.

$$H\left(\frac{2\pi}{15}K\right) = 1;$$
 $K = 0,1,2,3$
= 0.4; $K = 4$
= 0 ; $K = 5,6,7$ (10 Marks)

Module-4

7 a. The normalized transfer function of \overline{a} 2^{nd} order Butterworth filter is given by,

$$H_2(S) = \frac{1}{S^2 + 1.414S + 1}$$

Convert the analog filter into digital filter with cut-off frequency of 0.5π rad/sec using bilinear transformation. Assume T=1 sec. (10 Marks)

b. A filter is given by the difference equation $y(n) - \frac{1}{4}y(n-1) + \frac{1}{8}y(n-2) = x(n) + \frac{1}{2}x(n-2)$. Draw direct form – I and direct form – II realizations. Also obtain the transfer function of the filter. (10 Marks)

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- 8 a. Derive mapping function used in transforming analog filter to digital filter by bilinear transformation, preserves the frequency selectivity and stability properties of analog filter.
 - b. Design an IIR digital Butterworth filter that when used in the analog to digital with digital to analog will satisfy the following equivalent specification.
 - (i) Low pass filter with -1 dB cut off 100π rad/sec.
 - (ii) Stop band attenuation of 35 dB at $1000 \, \pi \, \text{rad/sec}$.
 - (iii) Monotonic in stop band and pass band.
 - (iv) Sampling rate of 2000 rad/sec.
 - (v) Use bilinear transformation.

(10 Marks)

Module-5

- 9 a. With the block diagram, explain Digital Signal processors based on the Harvard architecture.
 (10 Marks)
 - b. Discuss briefly the following special digital signal processor hardware units:
 - (i) Multiplier and Accumulator (MAC) unit.
 - (ii) Shifters.
 - (iii) Address Generators.

(10 Marks)

OR

0 a. Discuss the following IEE Floating-point formats:

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- (i) Single precision format.
 - (ii) Double precision format.

(10 Marks)

b. With the diagram, explain the basic architecture of TMS320C54X family processor.

(10 Marks)