

USN

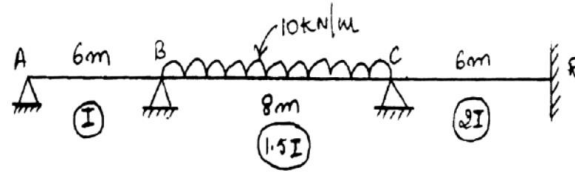
Internal Assessment Test 1 – Nov. 2021

|       |                                      |           |          |            |        |            |       |
|-------|--------------------------------------|-----------|----------|------------|--------|------------|-------|
| Sub:  | Analysis of Indeterminate Structures |           |          | Sub Code:  | 18CV52 | Branch:    | Civil |
| Date: | 11/11/2021                           | Duration: | 90 min's | Max Marks: |        | Sem / Sec: | 5A    |
|       |                                      |           |          |            |        |            | OBE   |

**Answer TWO FULL Questions**

1.

Analyze the continuous beam shown in fig 1. using the slope deflection method. Sketch BMD and SFD. support B and C settles by 8mm and 5mm respectively,  $EI = 20000 \text{ kN/m}^2$



## Step 1: Fixed end Moments

$$M_{FAB} = 0 \text{ KNm}$$

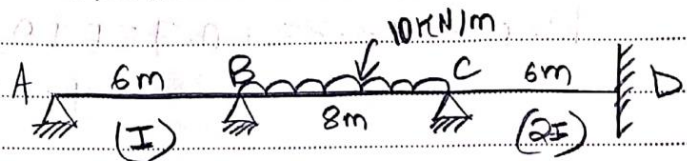
$$M_{FBC} = -53.34 \text{ KNm}$$

$$M_{FBA} = 0 \text{ KNm}$$

$$M_{FCB} = 53.34 \text{ KNm}$$

$$M_{FCD} = 0 \text{ KNm}$$

$$M_{FDC} = 0 \text{ KNm}$$



## Step 2: Slope deflection eqn ; $\delta = 8 \times 10^{-3}$

$$M_{AB} = M_{FAB} + \frac{2EI}{L} \left[ 2\theta_B + \theta_A - \frac{3\delta}{L} \right]$$

$$= 0 + \frac{2EI}{6} \left[ 2\theta_A + \theta_B - 3 \frac{(8 \times 10^{-3})}{6} \right]$$

$$M_{AB} = 0.667 EI \theta_A + 0.334 EI \theta_B - 1.334 \times 10^{-3} EI \quad \text{--- (1)}$$

$$M_{BA} = M_{FBA} + \frac{2EI}{L} \left[ 2\theta_B + \theta_A - \frac{3\delta}{L} \right]$$

$$= 0 + \frac{2EI}{6} \left[ 2\theta_B + \theta_A - 3 \frac{(8 \times 10^{-3})}{6} \right]$$

$$M_{BA} = 0.667 EI \theta_B + 0.334 EI \theta_A - 1.334 \times 10^{-3} EI \quad \text{--- (2)}$$

for span BC

$$M_{BC} = M_{FBC} + \frac{2EI}{L} \left[ 2\theta_B + \theta_C - \frac{3\delta}{L} \right]$$

$$= -53.33 + \frac{2E(1.5I)}{8} \left[ 2\theta_B + \theta_C - 3 \frac{(8 \times 10^{-3})}{8} \right]$$

$$M_{BC} = -53.33 + 0.375 EI \theta_B + 0.375 EI \theta_C + 4.21 \times 10^{-4} EI \quad \text{--- (3)}$$

$$M_{CB} = M_{FCB} + \frac{2EI}{l} \left[ 2\theta_C + \theta_B - \frac{3\delta}{l} \right]$$

$$= 53.33 + \frac{2E(1.5I)}{8} \left[ 2\theta_C + \theta_B - 3 \frac{(-3 \times 10^{-3})}{8} \right]$$

$$M_{CB} = 53.33 + 0.75EI\theta_C + 0.375EI\theta_B + 4.218 \times 10^{-4} EI \quad \text{--- (4)}$$

For span CD

$$M_{CD} = M_{FCD} + \frac{2EI}{l} \left( 2\theta_C + \theta_D - \frac{3\delta}{l} \right)$$

$$= 0 + \frac{2E(2I)}{6} \left( 2\theta_C + \theta_D - 3 \frac{(-5 \times 10^{-3})}{6} \right)$$

$$M_{CD} = 1.334EI\theta_C + 1.667 \times 10^{-3} EI \quad \text{--- (5)}$$

$$M_{DC} = M_{FDC} + \frac{2EI}{l} \left( 2\theta_D + \theta_C - \frac{3\delta}{l} \right)$$

$$= 0 + \frac{2E(2I)}{6} \left[ \theta_C - 3 \frac{(-5 \times 10^{-3})}{6} \right]$$

$$M_{DC} = 0.667EI\theta_C + 1.667 \times 10^{-3} EI \quad \text{--- (6)}$$

Step 3 : Joint Equilibrium Condition

@ Joint 'B',  $M_{BA} + M_{BC} = 0$

$$0.667EI\theta_B + 0.334EI\theta_A - 1.334 \times 10^{-3} EI$$

$$- 53.33 + 0.75EI\theta_B + 0.375EI\theta_C$$

$$+ 4.218 \times 10^{-4} EI = 0$$

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$$-71.574 + 0.334 EI\theta_A + 1.417EI\theta_B + 0.375EI\theta_C \quad \text{--- (7)}$$

@ Joint "C",  $M_{CB} + M_{CD} = 0$

$$53.33 + 0.75EI\theta_C + 0.375EI\theta_B + 4.218 \times 10^{-4} + 1.334EI\theta_C + 1.667 \times 10^{-3}EI = 0$$

$$95.09 + 2.084EI\theta_C + 0.375EI\theta_B \quad \text{--- (8)}$$

@ Joint "D",  $M_{DC} = 0$

$$0.667EI\theta_C + 1.667 \times 10^{-3}EI = 0$$

$$0.667EI\theta_C + 33.34 \quad \text{--- (9)}$$

$$\theta_A = \frac{167.7}{EI}$$

$$\theta_B = \frac{24.21}{EI}$$

$$\theta_C = \frac{-49.98}{EI}$$

Step 4: Final Moments

$$M_{AB} = 93.26 \text{ KN.m}$$

$$M_{CD} = -33.36 \text{ KN.m}$$

$$M_{BA} = 45.47 \text{ KN.m}$$

$$M_{DC} = 0 \text{ KN.m}$$

$$M_{BC} = -45.47 \text{ KN.m}$$

$$M_{CB} = 33.36 \text{ KN.m}$$

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Step 5: SFD &amp; BMD

$$\sum F_y = 0$$

$$V_A + V_B + V_C + V_D = 80 \text{ KN}$$

$$\sum M_B = 0 \text{ (LHS)}$$

$$V_A \times 6 + 93.266 + 45.47$$

$$V_A = -23.12 \text{ KN}$$

$$\sum M_C = 0 \text{ (RHS)}$$

$$-V_D \times 6 - 33.35 = 0$$

$$V_D = 5.55 \text{ KN}$$

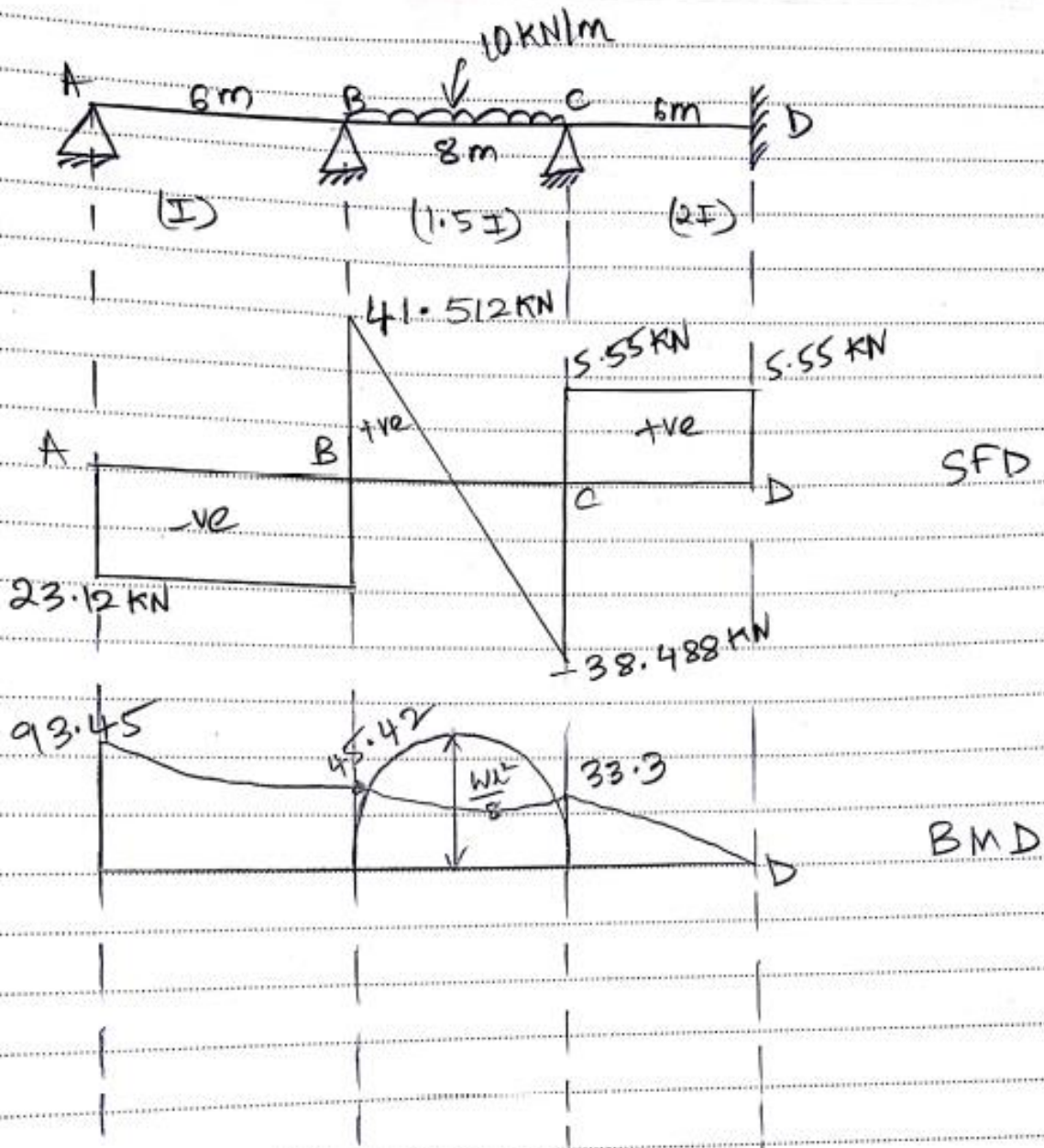
$$\sum M_C = 0 \text{ (LHS)}$$

$$V_A \times 14 - 10 \times 8 \times 4 + 93.262 + 33.35 + V_B \times 8$$

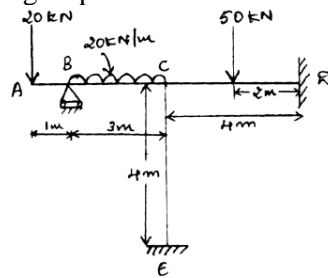
$$V_B = 64.632 \text{ KN}$$

$$V_C = 32.935 \text{ KN}$$

b



Analyze the Portal frame show in fig. using slope deflection method. Draw BMD and SFD



2.





For span CE,  $l = 4\text{m}$

$$M_{CE} = M_{FCE} + \frac{2EI}{l} \left( 2\theta_C + \theta_E - \frac{3\delta}{l} \right) \quad [\theta_E = 0]$$

$$M_{CE} = 0 + EI\theta_C \quad \text{--- (5)}$$

$$M_{EC} = M_{FEC} + \frac{2EI}{l} \left( 2\theta_E + \theta_C - \frac{3\delta}{l} \right)$$

$$= 0 + \frac{2EI}{4} (\theta_C)$$

$$M_{EC} = 0.5EI\theta_C \quad \text{--- (6)}$$

ii) Step 3: Joint Equilibrium Condition

$$M_{BA} + M_{BC} = 0 \quad \text{@ Joint B}$$

$$20 + (-15) + 0.667EI\theta_C + 1.33EI\theta_B = 0$$

$$1.33EI\theta_B + 0.667EI\theta_C = -5 \quad \text{--- (7)}$$

$$M_{CB} + M_{CD} + M_{CE} \quad \text{@ Joint C}$$

$$15 + 1.33EI\theta_C + 0.667EI\theta_B - 25 + EI\theta_C + EI\theta_C = 0$$

$$0.667EI\theta_B + 3.33EI\theta_C = 10 \quad \text{--- (8)}$$

$\therefore$  By solving eq (7) & (8), we get

$$\theta_B = \frac{-5.833}{EI}, \quad \theta_C = \frac{4.167}{EI}$$



### Step 4: Final Moments

Sub  $\theta_B, \theta_C$  in eq ①, ②, ③, ④, ⑤, ⑥

$$\begin{aligned} \text{We get, } M_{BC} &= -20 \text{ KNm} \\ M_{CB} &= 16.66 \text{ KNm} \\ M_{CD} &= -20.80 \text{ KNm} \\ M_{DC} &= 27.08 \text{ KNm} \\ M_{CE} &= 4.16 \text{ KNm} \\ M_{EC} &= 2.08 \text{ KNm} \end{aligned}$$

### Step 5: SFD & BMD

$$V_A + V_B + V_C + V_D = 20 + 20 \times 3 + 50$$

$$\text{@ B } \sum M_B = 0$$

$$V_A \times 1 - 20 \times 1 = 0$$

$$V_A = 20$$

$$\sum M_C \text{ @ RHS}$$

$$-V_D \times 4 + 50 \times 2 + 27.08 - 20.8$$

$$V_D = 26.57$$

$$\sum M_C \text{ @ LHS}$$

$$V_A \times 4 - 20 \times 4 + V_B \times 3 - 20 \times 3 \times 1.5 - 20 + 16.6$$

$$V_B = 23.33$$

$$V_C = 60.09$$