$1 \mid C \mid R$ ÈE **CMRIT**

Dept. of Civil Engineering

Internal Assessment Test III – January 2022

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URBAN TRANSPORT PLANNING

PROBLEMS ON GRAVITY MODEL

Problem-1

A self-contained town consists of four residential areas A, B, C and D and two industrial estates X and Y. Generation equations show that, for the design year in question, the trip from home to work generated by each residential area per 24 hour day are as follows :

Calculate and tabulate the inter zonal trips for journeys from home to work.

There are 3700 jobs in industrial estate X and 4,500 in industrial estate Y. It is know that the attraction between zones is inversely proportional to the square of the journey times between zones. The journey times in minutes from home to work to work are :

SOLUTION;

$$
\mathbf{T}_{\mathbf{i} \mathbf{-j}} = \frac{Pi \frac{AJ}{(d_{\mathbf{i} - \mathbf{j}})^2}}{\sum_{\substack{d \\ (d_{\mathbf{i} - n})^2}}}
$$

$$
T_{A-x} = \frac{1000 \times \frac{3700}{(15)^2}}{\frac{3700}{(15)^2} + \frac{4500}{(20)^2}} = \frac{1000 \times 16.5}{16.5 + 11.25} = 594
$$

$$
T_{A-y} = \frac{1000 \times \frac{4500}{(20)^2}}{\frac{3700}{(15)^2} + \frac{4500}{(20)^2}} = 406
$$

$$
T_{B-X} = \frac{2250 \times \frac{3700}{(15)^2}}{\frac{3700}{(15)^2} + \frac{4500}{(10)^2}} = 602
$$

$$
T_{B-Y} = \frac{2250 \times \frac{4500}{(10)^2}}{\frac{3700}{(15)^2} + \frac{4500}{(10)^2}} = 1648
$$

$$
T_{C-X} = \frac{1750 \times \frac{3700}{(10)^2}}{\frac{3700}{(10)^2} + \frac{4500}{(10)^2}} = 790
$$

$$
T_{C-Y} = \frac{1750 \times \frac{4500}{(10)^2}}{\frac{3700}{(10)^2} + \frac{4500}{(10)^2}} = 960
$$

$$
T_{D-X} = \frac{3200 \times \frac{3700}{(15)^2}}{\frac{3700}{(15)^2} + \frac{4500}{(20)^2}} = 1900
$$

$$
T_{D-Y} = \frac{3200 \times \frac{4500}{(20)^2}}{\frac{3700}{(15)^2} + \frac{4500}{(20)^2}} = 1300
$$

The result are tabulated in the matrix below:

	X	Υ	$\mathbf{T_{i-i}}$ FOR ORIGIN ZONE A,B,C,D. TOTAL PRODUCTIONS
\overline{A}	594	406	1000
B	602	1648	2250
C	790	960	1750
\Box	1900	1300	3200
TOTAL CALCULATED ATTRACTIONS, C_i	3886	4314	8200
TOTAL PREDICTED ATTRACTIONS, A_i	3700	4500	8200

It can be seen that the total attractions do not tally with the predicted attractions therefore the total attractions first adjusted ,using the fallowing formula

$$
A_{jk} = \frac{A_j}{C_{j(m-1)}} \cdot A_{j(m-1)}
$$

For second iteration m=2:

$$
A_{jk} = \frac{A_j}{C_{j(m-1)}} * A_{j(m-1)}
$$

A_{j2} for zone x =
$$
\frac{3700}{3886}
$$
 * 3700 = 3523

A_{j2} for zone Y =
$$
\frac{4500}{34314} \times 4500 = 4694
$$

Recalculating:

$$
\mathbf{T}_{i-j} = \frac{Pi \frac{Aj}{(d_{i-j})^2}}{\sum \frac{Ai}{(d_{i-n})^2}}
$$

$$
T_{A-x} = \frac{1000 \times \frac{3523}{(15)^2}}{\frac{3523}{(15)^2} + \frac{4694}{(20)^2}} = 572
$$

$$
T_{C-X} = \frac{1750 \times \frac{3523}{(10)^2}}{\frac{3523}{(10)^2} + \frac{4694}{(10)^2}} = 750
$$

$$
T_{C-Y} = \frac{1750 \times \frac{4694}{(10)^2}}{\frac{3523}{(10)^2} + \frac{4694}{(10)^2}} = 999
$$

$$
T_{A-y} = \frac{1000 \times \frac{4694}{(20)^2}}{\frac{3523}{(15)^2} + \frac{4694}{(20)^2}} = 429
$$

$$
T_{B-X} = \frac{2250 \times \frac{3523}{(15)^2}}{\frac{3523}{(15)^2} + \frac{4694}{(10)^2}} = 563
$$

$$
T_{D-X} = \frac{3200 \times \frac{3523}{(15)^2}}{\frac{3523}{(15)^2} + \frac{4694}{(20)^2}} = 1829
$$

$$
T_{B-Y} = \frac{2250 \times \frac{4694}{(10)^2}}{\frac{3523}{(15)^2} + \frac{4694}{(10)^2}} = 1687
$$

$$
T_{D-Y} = \frac{3200 \times \frac{4694}{(20)^2}}{\frac{3523}{(15)^2} + \frac{4694}{(20)^2}} = 1371
$$

The result are tabulated in the matrix below:

The results now closer to the total predicted attraction if more accuracy is needed further iteration can be done

PROBLEM 2

The total trips produced in and attracted to the three zones A,B and C of a

survey area in the design year are tabulated as

It is known that the trips between two zones are inversely proportional to the second power of the travel time between zones which is uniformly 20 minutes. If the trip interchange between zones B and C is known to be 600 , calculate the trip interchange between zones A and B , A and C , B and A , and C and B.

SOLUTION:

$$
T_{i-j} = \frac{KPiA_j}{t^n}
$$

$$
\text{T}_{\text{B-C}} = \frac{K P_A A_C}{t^2}
$$

$$
600 = \frac{K*3000*2000}{20^2}
$$

$$
T_{B-A} = \frac{0.04*2000*3000}{20^2} = 900
$$

$$
T_{C-B} = \frac{0.04*4000*4000}{20^2} = 1600
$$

K=0.04

$$
T_{A-B} = \frac{0.04*2000*4000}{20^2} = 800
$$

$$
T_{A-C} = \frac{0.04*2000*2000}{20^2} = 400
$$

The number of trips produced in and attracted to the three zones 1, 2 and 3 are tabulated as:

As a result of calibration, the friction factors to be associated with the impedance values between the various zones have been found to be follows :

Distribute the trips between the various zones

The impedance values between the various zones can be taken from the following matrix:

$$
T_{(i-j)m} = \frac{P_i A_{jm} F_{i-j}}{\sum (A_{jm} F_{i-j})}
$$

\n
$$
T_{1-1} = \frac{P_1 A_2 F_{1-1}}{A_1 F_{1-1} + A_2 F_{1-2} + A_3 F_{1-3}}
$$

\n
$$
T_{1-1} = \frac{14*33*13}{33*13+28*82+14*41} =
$$

= 1.82

$$
T_{1-2} = \frac{14 \times 28 \times 82}{3299} = 9.74
$$

$$
T_{1-3} = \frac{14*14*41}{3299} = 2.44
$$

$$
T_{2-1} = \frac{P_2 A_1 F_{2-1}}{A_1 F_{2-1} + A_2 F_{2-2} + A_3 F_{2-3}}
$$

$$
T_{2-1} = \frac{33*33*50}{33*50+28*26+14*39} = 18.62
$$

$$
T_{2-2} = \frac{33 \times 28 \times 26}{2924} = 8.22
$$

$$
T_{2-3} = \frac{33*14*39}{2924} = 2.44
$$

$$
T_{3-1} = \frac{P_3 A_2 F_{3-1}}{A_1 F_{3-1} + A_2 F_{3-2} + A_3 F_{3-3}}
$$

$$
T_{3-1} = \frac{28*33*52}{33*52+28*20+14*41} = 16.86
$$

$$
T_{3-2} = \frac{28 \times 28 \times 20}{2850} = 5.50
$$

$$
T_{3-3} = \frac{28*14*41}{2850} = 5.64
$$

Second iteration

It will be seen that the total trip attraction do not equal the desired attractions. Further iterations are, therefore, necessary. The following formula can be used to adjust the attraction factors :

$$
A_{jm} = \frac{A_j}{C_{J(m-1)}} \times A_{j(m-1)}
$$

Using the above values of $A_{J(2)}$

$$
T_{1-1} = \frac{14*29.19*13}{29.19*13+33.41*82+13.76*41} = 1.44
$$

$$
T_{1-2} = \frac{14*33.41*82}{3683.25} = 10.41
$$

$$
T_{1-3} = \frac{14*13.79*41}{3683.25} = 2.15
$$

Third iteration

It will be seent hat the attraction figures, though considerably closer to the desired values then the first iteration , need still further to be adjusted. The adjusted attration, $A_{(3)}$ are calculated as below

The process is continued with new values of $A_{J(3)}$ till a satisfactory agreement is reached between the desired and actual attraction figures

PROBLEMS ON OPPURTUNITY MODEL

1.The number of trips produced in an attracted to the three zones 1,2, and 3 are tabulated below:

The order of closeness of the zones is including by the fallowing matrix:

The zonal L factors are given below :

Distribute the trips between the zones:

SOLUTION:

$$
T_{i-j} = Q_i (e^{-LB} - e^{-LA})
$$

$$
T_{11}=14\left(e^{-0.04*0}-e^{-0.04*33}\right)=10.26\,\text{say}\,10
$$

$$
T_{12}=14\left(e^{-0.04*33}-e^{-0.04*(32+28)}\right)=2.52 \text{ say } 3
$$

$$
T_{13}=14\left(e^{-0.04*(32+28)}-e^{-0.04*(33+28+14)}\right)=2.52 \text{ say } 3
$$

$$
T_{21} = 33 \left(e^{-0.02 \times 28} - e^{-0.02 \times (28 + 33)} \right) = 9.11 \text{ say } 9
$$

$$
T_{22}=33\ (e^{-0.02*0}-e^{-0.02*28})=14.15\ say\ 14
$$

$$
T_{23}=33\left(e^{-0.02*(33+28)}-e^{-0.02*(33+28+14)}\right)=2.3 \text{ say } 2
$$

$$
T_{31} = 28 \left(e^{-0.04 \times 14} - e^{-0.04 \times (14 + 28 + 33)} \right) = 14.5 \text{ say } 14
$$

$$
T_{32} = 28 \left(e^{-0.04*(14+33)} - e^{-0.04*(14+28+33)} \right) = 2.87 \text{ say } 3
$$

$$
T_{33}=28(e^{-0.04*0}-e^{-0.04*14})=12.00
$$

It is seen that only 67 out of 75 trips have been distributed by this stage. Further iteration are needed. The destination total can be adjusted by the formula

$$
D_{j(m)} = \frac{D_j}{D_{j(m-1)}} * D_{j(m-1)}
$$

The iteration is carried until a reasonable closeness is obtained between the total trips and calculated trips.