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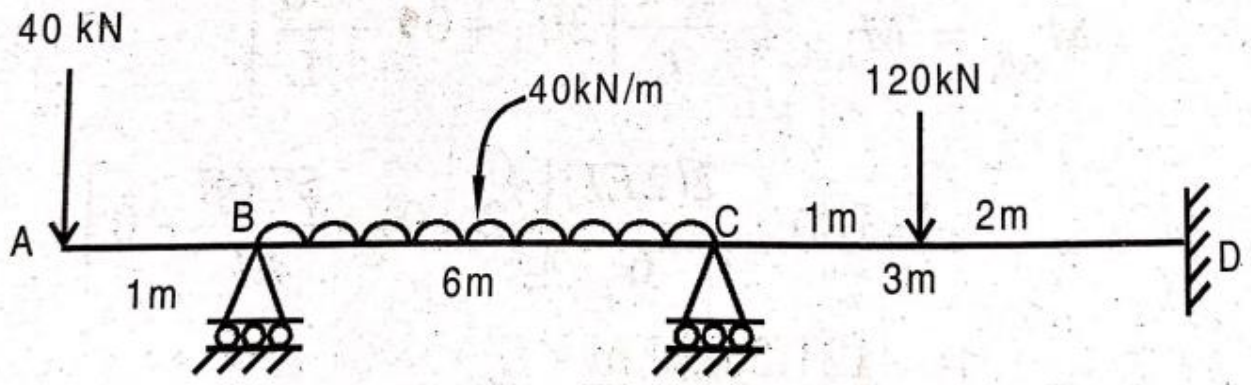
Internal Assessment Test 3 –Jan. 2022

Sub:	Analysis of Indeterminate Structures					Sub Code:	18CV52	Branch:	Civil		
Date:	24/1/2022	Duration:	90 min's	Max Marks:	50	Sem / Sec:	5A		OBE		
<b>Answer TWO FULL Questions</b>									MARKS	CO	RBT
1.	<p>Analyze the continuous beam shown in fig by stiffness matrix method. The support C sinks by 9mm, Take <math>EI= 1000kN.m^2</math>. Draw BMD and SFD</p> <p style="text-align: right;">fig 1</p>							[25]	CO1	L3	
2.	<p>Analyze the truss shown in fig 2. by flexibility matrix method choosing the force member AD as redundant. Assume EA constant for all members</p> <p style="text-align: right;">fig 2</p>							[25]	CO 2	L3	

CI  
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CCI

Problem 1: Analyze the continuous beam shown in fig by stiffness matrix method. The support C sinks by 9mm, Take  $EI= 1000kN.m^2$



1. Fixed end moment:

$$M_{fbc} = -40 \cdot 6 \cdot 6 / 12 - 6EI\delta / l^3 = -120 - 6 \cdot 1000 \cdot 0.009 / 6 \cdot 6 = -121.5 \text{ kN.m}$$

$$M_{fcb} = 120 - 6 \cdot 1000 \cdot 0.009 / 6 \cdot 6 = 118.5 \text{ kN.m}$$

$$M_{fcd} = -120 \cdot 1 \cdot 2 \cdot 2 / 3 \cdot 3 - 6 \cdot 1000 \cdot (-0.009) / 3 \cdot 3 = -47.33$$

$$M_{fcb} = 120 \cdot 1 \cdot 1 \cdot 2 / 3 \cdot 3 - 6 \cdot 1000 \cdot (-0.009) / 3 \cdot 3 = 32.67 \text{ kN.m}$$

2.  $[\Delta]$ ,  $[P]$ ,  $[P_L]$

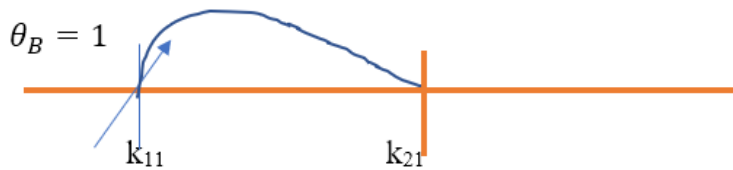
$$[\Delta] = \text{unknown displacement matrix} = \begin{bmatrix} \theta_B \\ \theta_C \end{bmatrix}$$

$$[P] = \text{moments acting -External} = \begin{bmatrix} -40 \\ 0 \end{bmatrix}$$

$$[P_L] = \text{joint moments} = \begin{bmatrix} M_{FBA} + M_{FBC} \\ M_{FCB} + M_{FCD} \end{bmatrix} = \begin{bmatrix} -121.5 \\ 118.5 - 47.33 \end{bmatrix} = \begin{bmatrix} -121.5 \\ 71.17 \end{bmatrix}$$

3. Stiffness matrix = to find the  $\theta_B, \theta_C$

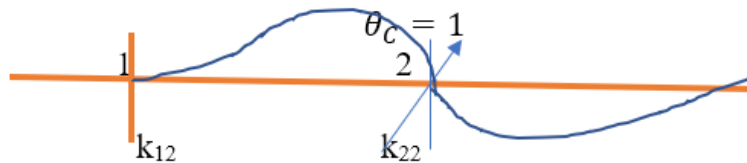
Applying the unit rotation along the co-ordinate 1



$$k_{11} = \frac{4EI}{6} = 0.67EI$$

$$k_{21} = \frac{2EI}{6} = 0.33EI$$

Apply unit rotation at B = coordinate 2



$$k_{12} = \frac{2EI}{6} = 0.33EI$$

$$k_{22} = \frac{4EI}{6} + \frac{4EI}{3} = 2EI$$

$$\begin{bmatrix} k_{11} & k_{12} \\ k_{21} & k_{22} \end{bmatrix} = [EI] \begin{bmatrix} 0.67 & 0.33 \\ 0.33 & 2 \end{bmatrix}$$

$$[\Delta] = [k]^{-1} [P - P_L]$$

$$\begin{bmatrix} \theta_B \\ \theta_C \end{bmatrix} = \frac{1}{EI} \begin{bmatrix} 0.67 & 0.33 \\ 0.33 & 2 \end{bmatrix}^{-1} \begin{bmatrix} -40 - 121.5 \\ 0 + 71.17 \end{bmatrix}$$

$$\theta_B = \frac{151.75}{EI}, \theta_C = \frac{-60.91}{EI}$$

4. Substitute the above values in the slope deflection equation

$$M_{BC} = M_{FBC} + \frac{2EI}{l}(2\theta_B + \theta_C - \frac{3\delta}{l})$$

$$= -121.5 + 2 * 1000 / 6 (2 * \frac{151.75}{1000} - \frac{60.91}{1000}) = -40.63 \text{ kN.m}$$

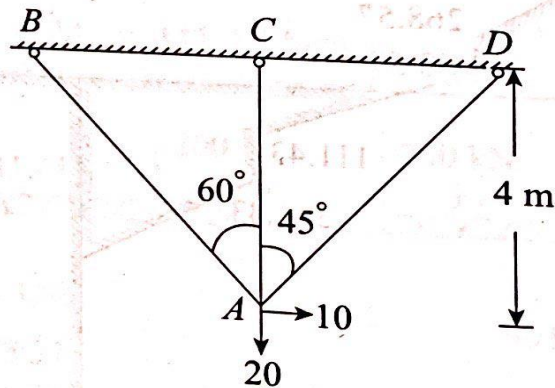
$$M_{CB} = M_{FCB} + \frac{2EI}{l}(2\theta_C + \theta_B - \frac{3\delta}{l})$$

$$= 121.5 + 2 * 1000 / 6 (\frac{151.75}{1000} - 2 * \frac{60.91}{1000}) = 128.47 \text{ N.m}$$

$$M_{CD} = -128.47 \text{ kN.m}$$

$$M_{DC} = -7.93 \text{ kN.m}$$

**Example 4.18** Analyse the truss shown in Fig. 4.129 by the flexibility matrix method choosing the force member AD is redundant. Assume EA constant for all members



Steps:

**1. Determine the static indeterminacy**

$$3 - 2 = 1$$

**2. Selection of redundant: member AD considered as redundant**

Length of the members

$$AB = 8 \text{ m}$$

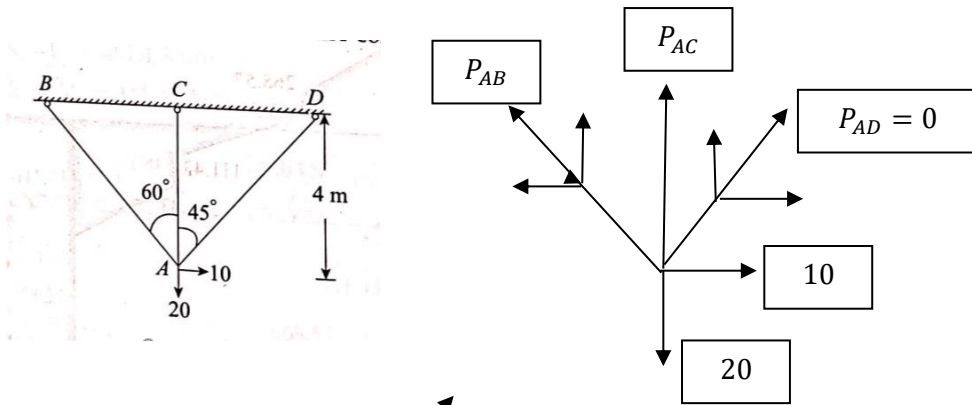
$$AC = 4 \text{ m}$$

$$AD = 5.65 \text{ m}$$

**3. Computing the axial force- actual force (P): by method of joint =**

$$P_{AD} = 0$$

**Consider the joint A**



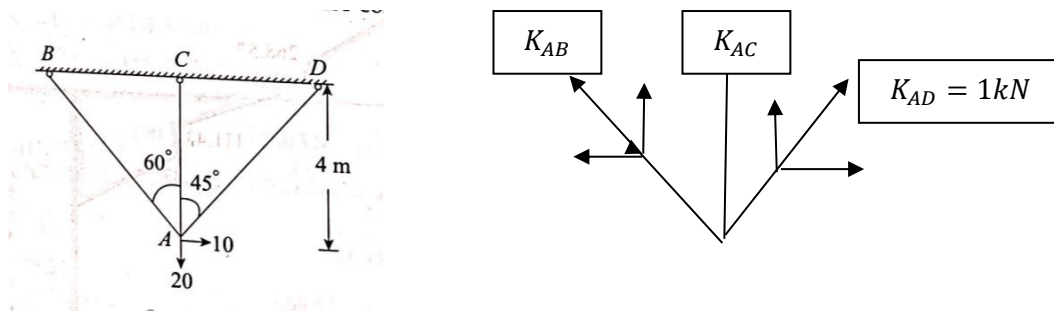
Horizontal forces  $\sum H = 0, = P_{AD}\sin 45 + 10 - P_{AB}\sin 60 = 0$

$$10 = P_{AB}\sin 60$$

$$P_{AB} = 11.54(T)$$

$\sum V = 0, = P_{AD}\cos 45 - 20 + P_{AB}\cos 60 + P_{AC} = 0$

#### 4. Computing the axial force – Unit load application at redundant (K)



Horizontal forces = 0, =  $K_{AD}\sin 45 - K_{AB}\sin 60 = 0$

$$1\sin 45 - K_{AB}\sin 60 = 0$$

$$K_{AB} = 0.816\text{kN}$$

$\sum V = 0, = K_{AD}\cos 45 + K_{AB}\cos 60 + K_{AC} = 0$

$$1\cos 45 + 0.816\cos 60 + K_{AC} = 0$$

#### 5. Force in the member – actual load and unit load

Member	Length(L) m	Area (mm <sup>2</sup> )	E (kN/mm <sup>2</sup> )	P (kN)	K(kN)	$\frac{PKL}{AE}$	$\frac{K^2L}{AE}$
AB	8	A	E	11.54	0.816	75.33/AE	5.32/AE
AC	4	A	E	14.22	-1.11	-63.13/AE	4.92/AE
AD	5.65	A	E	00	1	0	5.65/AE
						12.26/AE	15.89/AE

6. Calculation of deflection

$$\Delta_L = \sum \frac{PKL}{AE} = 12.26/AE$$

7. Compatibility equation

$$F = \sum \frac{K^2L}{AE} = 15.89/AE$$

$$\{\Delta - \Delta_L\} = [F] \{R\}$$

$$\{0 - 12.26\} * [15.89]^{-1} = \{R\}$$

$$\frac{-12.26}{15.89} = -0.77$$

8. Final moment

Member	P (kN)	K(kN)	R(kN)	P <sub>F</sub> =P+KR (kN)	Nature of force
AB	11.54	0.816	-0.77	10.91	T
AC	14.22	-1.11	-0.77	15.07	T
AD	0	1	-0.77	-0.77	C

