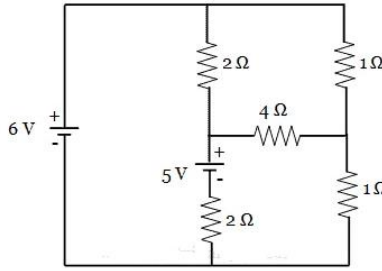
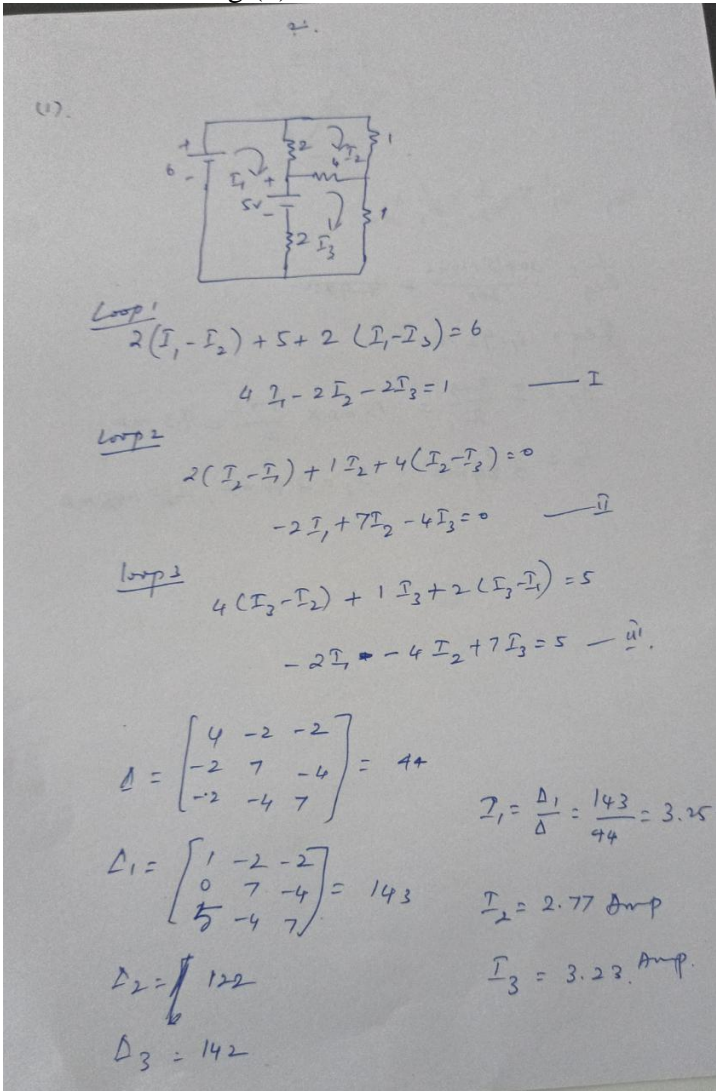


## Internal Assessment Test 1 – Dec. 2021

Sub:	Network Theory				Sub Code:	18EC32	Branch:	ECE		
Date:	16-12-2021	Duration:	90 Minutes	Max Marks:	50	Sem / Sec:	3/A, B,C,D		OBE	
Answer any FIVE FULL Questions							MARKS	CO	RBT	
1	a. Determine the mesh currents in the given circuit Fig.1					[7]	CO1	L3		
 <p style="text-align: center;">Fig (1)</p>							[3]	CO1	L3	
 <p> <math display="block">\Delta = \begin{bmatrix} 4 &amp; -2 &amp; -2 \\ -2 &amp; 7 &amp; -4 \\ -2 &amp; -4 &amp; 7 \end{bmatrix} = 44</math> <math display="block">\Delta_1 = \begin{bmatrix} 1 &amp; -2 &amp; -2 \\ 0 &amp; 7 &amp; -4 \\ 5 &amp; -4 &amp; 7 \end{bmatrix} = 143</math> <math display="block">\Delta_2 = \begin{bmatrix} 1 &amp; 2 &amp; 2 \\ 0 &amp; 7 &amp; -4 \\ 0 &amp; -4 &amp; 7 \end{bmatrix} = 122</math> <math display="block">\Delta_3 = 142</math> <math display="block">I_1 = \frac{\Delta_1}{\Delta} = \frac{143}{44} = 3.25</math> <math display="block">I_2 = 2.77 \text{ Amp}</math> <math display="block">I_3 = 3.23 \text{ Amp}</math> </p>										
b. Find the branch current in the given Fig 2.										

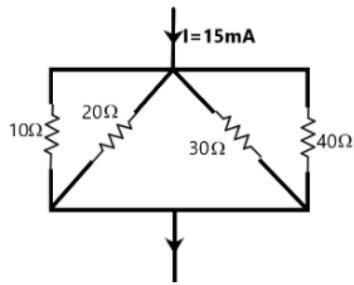


Fig (2)

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4}$$

$$\frac{1}{R_{eq}} = \frac{30 + 15 + 10 + 4}{300} = \frac{59}{300}$$

$$R_{eq} = 4.92 \Omega$$

$$I_1 = I \frac{R_{eq}}{R_1} = 15 \text{ mA} \times \frac{4.92}{10} = 7.38 \text{ mA}$$

$$I_2 = 3.66 \text{ mA}, I_3 = 2.46 \text{ mA}, I_4 = 1.48 \text{ mA}$$

2 Determine the nodal analysis to determine  $V_1$ ,  $V_2$  and in Fig.3.

[10]

CO1

L3

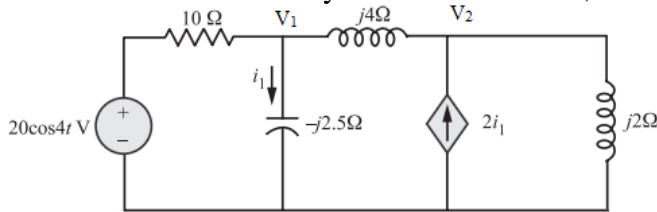


Fig.3

The phasor equivalent circuit is as shown in Fig. 1.88(a).

KCL at node  $V_1$ :

$$\frac{V_1 - 20 \angle 0^\circ}{10} + \frac{V_1}{-j2.5} + \frac{V_1 - V_2}{j4} = 0$$

$$\Rightarrow (1 + j1.5)V_1 + j2.5V_2 = 20$$

KCL at node  $V_2$ :

$$\frac{V_2 - V_1}{j4} + \frac{V_2}{j2} = 2I_1$$

But

$$I_1 = \frac{V_1}{-j2.5}$$

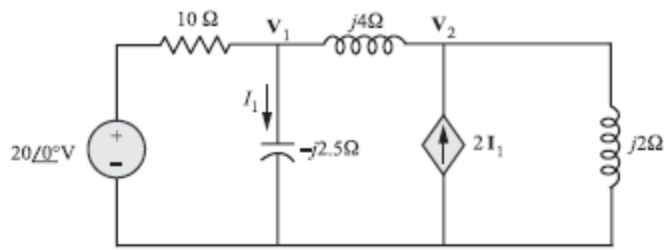


Figure 1.88(a)

Hence,

$$\frac{V_2 - V_1}{j4} + \frac{V_2}{j2} = \frac{2V_1}{-j2.5}$$

$$\Rightarrow -j0.55V_1 - j0.75V_2 = 0$$

Multiplying throughout by  $j20$ , we get

$$11V_1 + 15V_2 = 0$$

Putting the two nodal equations in matrix form, we get

$$\begin{bmatrix} 1 + j1.5 & j2.5 \\ 11 & 15 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} 20 \\ 0 \end{bmatrix}$$

Solving the matrix equation, we get

$$V_1 = 18.97 \angle 18.43^\circ \text{ V}$$

$$V_2 = 13.91 \angle -161.56^\circ \text{ V}$$

The current 
$$I_1 = \frac{V_1}{-j2.5} = 7.59 \angle 108.4^\circ \text{ A}$$

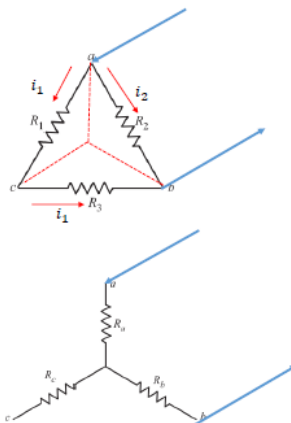
Transforming this to the time-domain, we get

$$i_1 = 7.59 \cos(4t + 108.4^\circ) \text{ A}$$

3

(a) Derive star to delta transformation.

### Delta to Star Conversion



Let us consider two terminal a-b in both network and calculate equivalent resistance of delta network

$$R_{eq} = R_2 \parallel (R_1 + R_3)$$

Similarly, for star network

$$R_{eq} = R_a + R_b$$

Terminal characteristics of delta network must be equivalent to that of a star network must

$$R_2 \parallel (R_1 + R_3) = R_a + R_b$$

$$\frac{R_2(R_1 + R_3)}{R_1 + R_2 + R_3} = R_a + R_b$$

$$\frac{R_1 R_2 + R_2 R_3}{R_1 + R_2 + R_3} = R_a + R_b$$

$$\frac{R_1 R_2 + R_2 R_3}{R_1 + R_2 + R_3} = R_a + R_b \quad (1)$$

Let us consider two terminal a-c

$$\frac{R_1 R_2 + R_1 R_3}{R_1 + R_2 + R_3} = R_a + R_c \quad (2)$$

Let us consider two terminal b-c

$$\frac{R_1 R_2 + R_2 R_3}{R_1 + R_2 + R_3} = R_b + R_c \quad (3)$$

adding (1) (2) (3)

$$\frac{2(R_1 R_2 + R_2 R_3 + R_1 R_3)}{R_1 + R_2 + R_3} = 2(R_a + R_b + R_c)$$

$$\frac{(R_1 R_2 + R_2 R_3 + R_1 R_3)}{R_1 + R_2 + R_3} = (R_a + R_b + R_c) \quad (4)$$

$$(4) - (1) \quad R_c = \frac{(R_1 R_2)}{R_1 + R_2 + R_3} \quad (5)$$

$$(4) - (2) \quad R_b = \frac{(R_2 R_3)}{R_1 + R_2 + R_3} \quad (6)$$

$$(4) - (3) \quad R_a = \frac{(R_1 R_3)}{R_1 + R_2 + R_3} \quad (7)$$

[04]  
[06]

CO1  
CO1

L2  
L3

**Star to Delta Conversion**

$$R_c = \frac{(R_1 R_2)}{R_1 + R_2 + R_3} \quad (5)$$

$$R_b = \frac{(R_2 R_3)}{R_1 + R_2 + R_3} \quad (6)$$

$$R_a = \frac{(R_1 R_3)}{R_1 + R_2 + R_3} \quad (7)$$

$$R_a R_b = \frac{(R_1 R_2^2 R_3)}{(R_1 + R_2 + R_3)^2} \quad (8)$$

$$R_b R_c = \frac{(R_1 R_2 R_3^2)}{(R_1 + R_2 + R_3)^2} \quad (9)$$

$$R_c R_a = \frac{(R_1^2 R_2 R_3)}{(R_1 + R_2 + R_3)^2} \quad (10)$$

$$R_a R_b + R_b R_c + R_c R_a = \frac{R_1 R_2 R_3 (R_1 + R_2 + R_3)}{(R_1 + R_2 + R_3)^2}$$

$$R_a R_b + R_b R_c + R_c R_a = \frac{R_1 R_2 R_3}{(R_1 + R_2 + R_3)} \quad (11)$$

$$(11) \div (5)$$

$$\frac{R_a R_b + R_b R_c + R_c R_a}{R_c} = \frac{R_1 R_2 R_3 / R_1 R_3}{(R_1 + R_2 + R_3) / (R_1 + R_2 + R_3)}$$

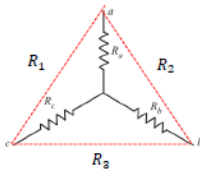
$$R_2 = \frac{R_a R_b + R_b R_c + R_c R_a}{R_c}$$

$$(11) \div (6)$$

$$R_1 = \frac{R_a R_b + R_b R_c + R_c R_a}{R_b}$$

$$(11) \div (7)$$

$$R_3 = \frac{R_a R_b + R_b R_c + R_c R_a}{R_a}$$



(b) Find  $I_0$  in the circuit shown in Fig.4 using source transformation.

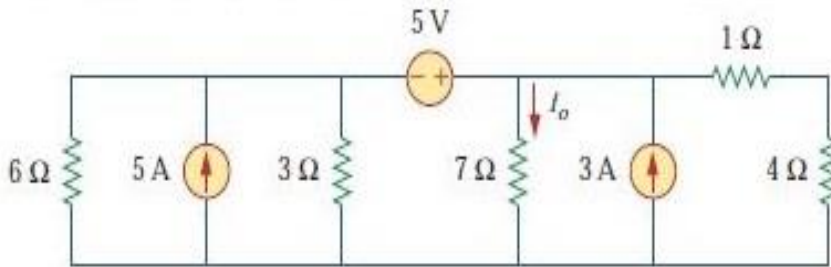


Fig. 4

4 The wheat stone bridge in the circuit shown in fig.5 is balanced when  $R_2=1200 \Omega$ . If the galvanometer has a resistance of  $30 \Omega$ , how much current will be detected by it when the bridge is unbalanced by setting  $R_2$  to  $1204 \Omega$  using Thevenin's theorem?

[10] CO2 L3

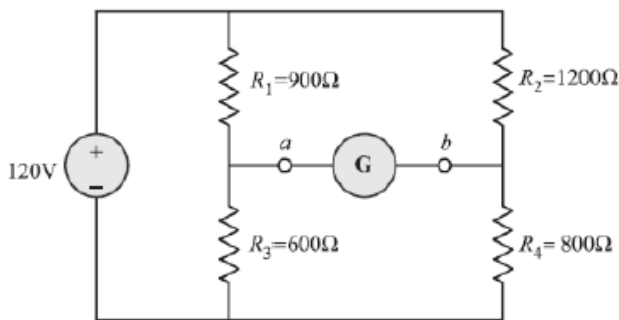
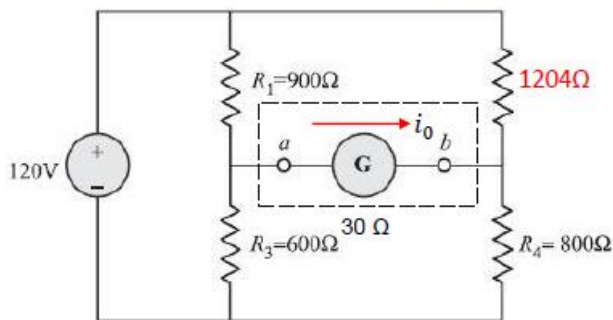
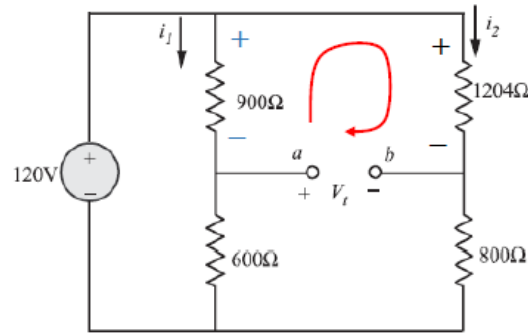


Fig.5

**Sol: i)** We are interested in the galvanometer current



1) To find  $V_t$



$$i_1 = \frac{120}{900 + 600} = \frac{120}{1500} A$$

$$i_2 = \frac{120}{1204 + 800} = \frac{120}{2004} A$$

Applying KVL in the outer loop

$$-1204i_2 = V_t + 900i_1$$

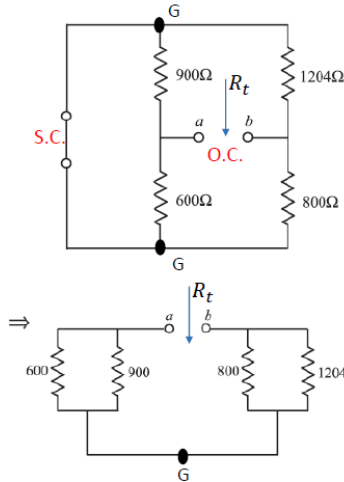
$$-V_t = -1204 \left( \frac{120}{2004} \right) + 900 \left( \frac{120}{1500} \right)$$

$$V_t = 1204 \left( \frac{120}{2004} \right) - 900 \left( \frac{120}{1500} \right)$$

$$V_t = 95.8mV$$

$$V_t = 95.8mV$$

ii) To find  $R_t$  deactivate all the sources



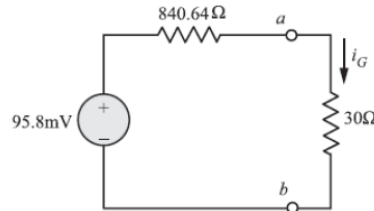
$$R_t = (600 || 900) + (800 || 1204)$$

$$R_t = \frac{600(900)}{600 + 900} + \frac{800(1204)}{800 + 1204}$$

$$R_t = 840.64\Omega$$

iii) Thevenin's equivalent circuit

Hence, the Thevenin equivalent circuit consists of the 95.8 mV source in series with 840.64Ω resistor.



$$i_G = \frac{95.8m}{840.64 + 30}$$

$$i_G = 110.03\mu A$$

- 5 a. List out the steps involved in the millman's theorem for circuit reduction.  
 b. For the circuit shown in Fig. 6, find the load impedance  $Z_L$  that absorbs the maximum power. Calculate that maximum power.

[4]

CO2

L2

[6]

CO2

L3

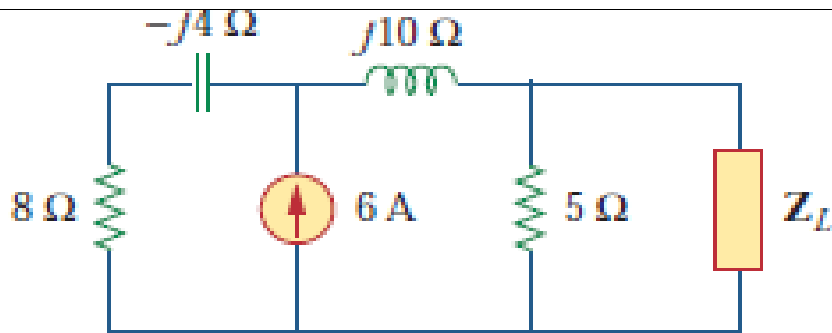
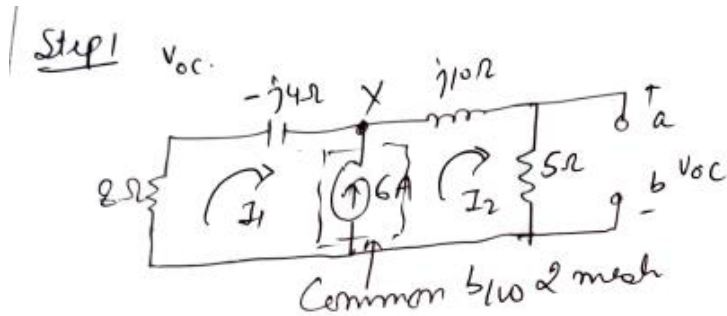


Fig.6

Solution:



Supermesh Eq<sup>n</sup>

$$-8I_1 - (-j4)I_1 - j10I_2 - 5I_2 = 0$$

$$I_1(-8 + j4) + I_2(-5 - j10) = 0 \quad \text{--- (1)}$$

KCL at X

$$-I_1 - 6 + I_2 = 0$$

$$I_1 = I_2 - 6 \quad \text{--- (2)}$$

from (1) & (2)

$$(I_2 - 6)(-8 + j4) + I_2(-5 - j10) = 0$$

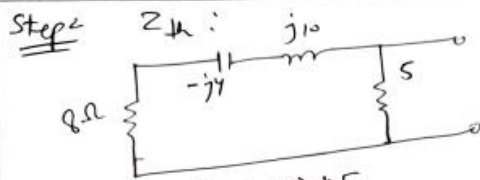
$$I_2(-8 + j4) - 6(-8 + j4) + I_2(-5 - j10) = 0$$

$$I_2(-13 - j6) = 6(-8 + j4)$$
~~$$I_2 = 0.29 = 0.29$$~~

$$I_2 = 2.34 - 2.92j \text{ A}$$

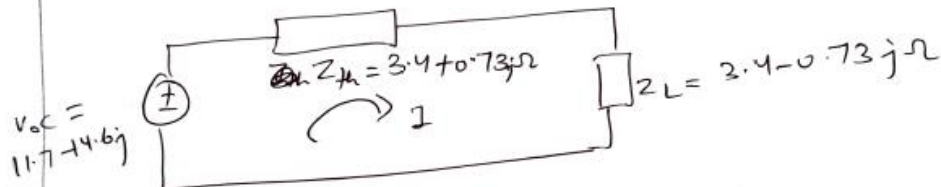
$$V_{oc} = 5I_2$$

$$= 11.7 - 14.6j \text{ Volts}$$



$$Z_{th} = \frac{(8+j6) \parallel 5}{8+j6+5} = \frac{40+30j}{13+j6} = 3.4+0.73j \Omega$$

$$Z_L = Z_{th}^* = 3.4 - 0.73j \Omega$$



$$I = \frac{V_{oc}}{Z_{th} + Z_L} = \frac{11.7 - 14.6j}{3.4 - 0.73j + 3.4 + 0.73j} = 1.72 - 2.15j \text{ A}$$

$$= 2.75 \angle -51.3^\circ \text{ A}$$

$$P_{max} = \frac{I^2 \cdot R_L}{2} = \frac{(2.75)^2 \cdot (3.4)}{2} = 12.86 \text{ Watts}$$

6 State Norton's theorem and explain its equivalent circuit. Find the Norton's equivalent circuit for the circuit in Fig. 7 with respect to terminals a-b.

[10]

CO2

L1,L3

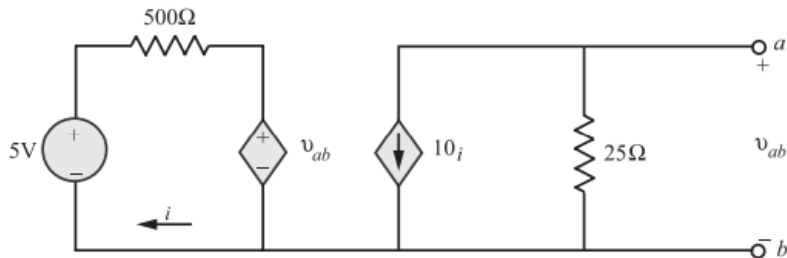


Fig.7

Solution:

*Norton's theorem states that a linear two-terminal network can be replaced by an equivalent circuit consisting of a current source  $i_N$  in parallel with resistor  $R_N$ , where  $i_N$  is the short-circuit current through the terminals and  $R_N$  is the input or equivalent resistance at the terminals when the independent sources are turned off. If one does not wish to turn off the independent sources, then  $R_N$  is the ratio of open circuit voltage to short-circuit current at the terminal pair.*

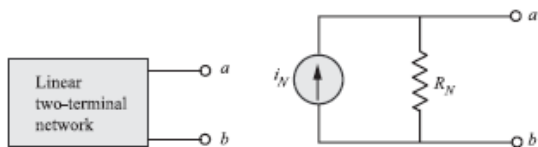


Figure 3.61(a) Original circuit

Figure 3.61(b) Norton's equivalent circuit

Figure 3.61(b) shows Norton's equivalent circuit as seen from the terminals  $a - b$  of the original circuit shown in Fig. 3.61(a). Since this is the dual of the Thevenin circuit, it is clear that  $R_N = R_t$  and  $i_N = \frac{v_{oc}}{R_t}$ . In fact, source transformation of Thevenin equivalent circuit leads to Norton's equivalent circuit.

**Procedure for finding Norton's equivalent circuit:**

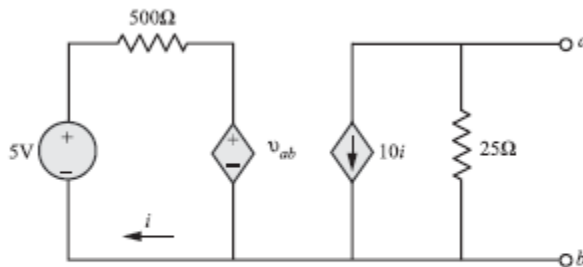
- (1) If the network contains resistors and independent sources, follow the instructions below:
  - (a) Deactivate the sources and find  $R_N$  by circuit reduction techniques.
  - (b) Find  $i_N$  with sources activated.
- (2) If the network contains resistors, independent and dependent sources, follow the steps given below:
  - (a) Determine the short-circuit current  $i_N$  with all sources activated.
  - (b) Find the open-circuit voltage  $v_{oc}$ .
  - (c)  $R_t = R_N = \frac{v_{oc}}{i_N}$
- (3) If the network contains only resistors and dependent sources, follow the procedure described below:
  - (a) Note that  $i_N = 0$ .
  - (b) Connect 1A current source to the terminals  $a - b$  and find  $v_{ab}$ .
  - (c)  $R_t = \frac{v_{ab}}{1}$

Note: Also, since  $v_t = v_{oc}$  and  $i_N = i_{sc}$

$$R_t = \frac{v_{oc}}{i_{sc}} = R_N$$

The open-circuit and short-circuit test are sufficient to find any Thevenin or Norton equivalent.

To find  $R_N$  or  $R_t$ :



Writing the KVL equations for the left-hand mesh, we get

$$-5 + 500i + v_{ab} = 0 \tag{3.15}$$

Also for the right-hand mesh, we get

$$v_{ab} = -25(10i) = -250i$$

Therefore

$$i = \frac{-v_{ab}}{250}$$

Substituting  $i$  into the mesh equation (3.15), we get

$$\begin{aligned} -5 + 500 \left( \frac{-v_{ab}}{250} \right) + v_{ab} &= 0 \\ \Rightarrow v_{ab} &= -5 \text{ V} \\ R_N = R_t \triangleq \frac{v_{oc}}{i_{sc}} = \frac{v_{ab}}{i_{sc}} &= \frac{-5}{-0.1} = 50 \Omega \end{aligned}$$

The Norton equivalent circuit is shown in Fig 3.77 (a).

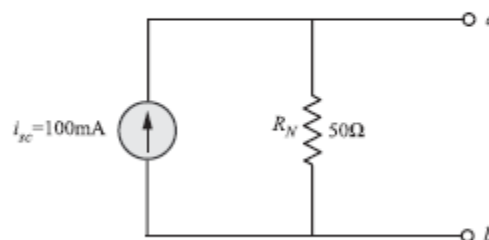
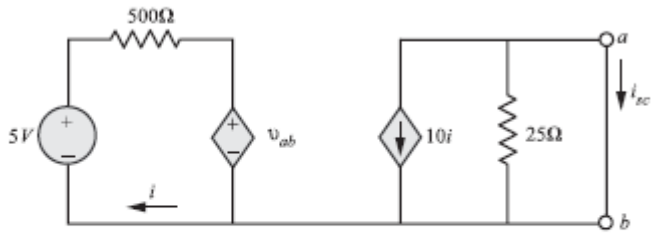


Figure 3.77 (a)



To find  $i_{sc}$ :



Note that  $v_{ab} = 0$  when the terminals  $a - b$  are short-circuited.

Then 
$$i = \frac{5}{500} = 10 \text{ mA}$$

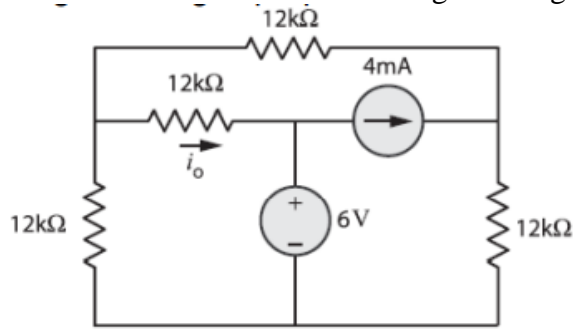
Therefore, for the right-hand portion of the circuit,  $i_{sc} = -10i = -100 \text{ mA}$ .

7 Find  $i_o$  in the network shown in figure using superposition

[10]

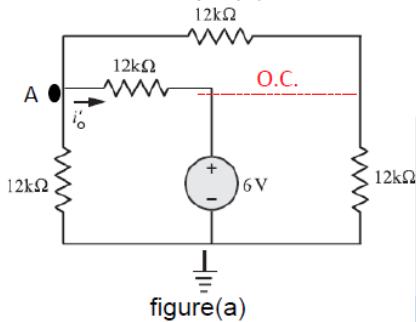
CO2

L3

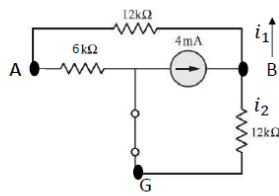


Solution:

**Sol:** As a first step, set the current source to zero. That is, the current source appears as an open circuit as shown in figure(a)



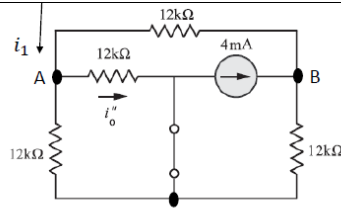




Using current division principle

$$i_1 = (4m) \left( \frac{12k}{12k + 12k + 6k} \right)$$

$$i_1 = 1.6mA$$



Using current division principle

$$i_0'' = 0.8mA$$

According to superposition theorem

$$i_0 = i_0' + i_0''$$

$$i_0 = -0.3m + 0.8m = 0.5mA$$