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| CMR<br>INSTITUTE OF<br>TECHNOLOGY   | USN <span style="border: 1px solid black; display: inline-block; width: 100px; height: 15px;"></span> |                      |
| Internal Assessment Test II – Dec 2021  |   |                      |
| Sub:  | Signals and Systems   | Code: 18EE54         |
| Date: 16/12/2021  | Duration: 90 mins   | Max Marks: 50        |
|   | Sem: V  | Section: EEE (A & B) |
| Note: Answer any <b>five FULL</b> Questions<br>Sketch neat figures wherever necessary. Answer to the point. <b>Good luck!</b> |   |                      |

OBE  
Marks CO RBT

|       |   |        |     |    |
|-------|---|--------|-----|----|
| 1     | Determine Energy of the following signals<br>(i) $x(t) = \begin{cases} \frac{1}{2}[1 + \cos(\omega t)] & -\frac{\pi}{\omega} \leq t \leq \frac{\pi}{\omega} \\ 0 & \text{Otherwise} \end{cases}$<br>(ii) $x(t) = e^{-3t}u(t)$<br>(iii) $x[n] = n \quad 0 \leq n \leq 5$ | [10 M] | CO1 | L3 |
| 2 (a) | A certain signal is described by the following mathematical equation. What is the energy of the signal?<br>$x(t) = \begin{cases} 2t & 0 \leq t < 1 \\ 2 + \sin(2\pi t) & 1 \leq t < 2 \\ 4 - t & 2 \leq t < 4 \\ 0 & \text{Otherwise} \end{cases}$                      | [7 M]  | CO1 | L3 |
| 2 (b) | Distinguish between Power and Energy signals  | [3 M]  | CO1 | L1 |
| 3     | Determine whether the following systems represented by input-output relations is (i) Linear (ii) Time-invariant (iii) Causal (iv) Memoryless (v) Stable<br>(a) $y[n] = x[n] u[n + 1]$ (b) $y(t) = \int_{-\infty}^t x(\tau) d\tau$                                       | [10 M] | CO2 | L3 |
| 4(a)  | Given the impulse response $h[n]$ , of an LTI system, obtain the condition which needs to be satisfied by $h[n]$ , for the system to be (i) Causal (ii) Stable.   | [4 M]  | CO3 | L2 |
| 4(b)  | Verify whether the following impulse responses are stable and causal or not.<br>(i) $h(t) = e^{2t}u(t - 1)$<br>(ii) $h[n] = \left(\frac{1}{2}\right)^n u[n]$  | [6 M]  | CO3 | L3 |
| 5     | Find the output $y(t)$ of the system, for a continuous time LTI system with unit impulse response $h(t) = u(t)$ and input $x(t) = e^{-5t}u(t)$  | [10 M] | CO2 | L3 |
| 6     | Determine the output of the following discrete time system, whose impulse response is $h[n] = (0.2)^n u[n]$ and the excitation of $x[n] = (0.6)^n u[n]$   | [10 M] | CO2 | L3 |
| 7 (a) | Determine the natural response for the following differential/difference equation<br>(i) $3 \frac{dy(t)}{dt} + 2y(t) = 5 \frac{dx(t)}{dt}$<br>(ii) $y[n] - \frac{1}{3}y[n - 1] + \frac{1}{2}y[n - 2] = x[n] + x[n - 1]$   | [5 M]  | CO2 | L3 |
| 7(b)  | Determine the forced response for the given input, $x[n] = \left(\frac{1}{2}\right)^n u[n]$<br>$y[n] - \frac{1}{4}y[n - 1] - \frac{1}{8}y[n - 2] = x[n] + x[n - 1]$   | [5M]   | CO2 | L3 |
| 8 (a) | Explain the cascade and parallel connection of impulse responses and write the output equation.   | [5M]   | CO2 | L2 |
| 8 (b) | Find the output for the following sequences. $x[n] = \{1, 3, 0, -1, 2, 1\}$ and $h[n] = \{2, -1, 3\}$   | [5M]   | CO2 | L2 |

CCI

CCI

HOD

① Determine Energy of the following signals.

$$(i) x(t) = \begin{cases} \frac{1}{2} [1 + \cos(\omega t)] & -\frac{\pi}{\omega} \leq t \leq \frac{\pi}{\omega} \\ 0 & \text{otherwise.} \end{cases}$$

$$E = \lim_{T \rightarrow \infty} \int_{-T}^T |x(t)|^2 dt$$

$$E = \int_{-\pi/\omega}^{\pi/\omega} \left( \frac{1}{2} [1 + \cos(\omega t)] \right)^2 dt$$

$$= \frac{1}{4} \int_{-\pi/\omega}^{\pi/\omega} (1 + \cos \omega t)^2 dt = \frac{1}{4} \int_{-\pi/\omega}^{\pi/\omega} (1 + \cos^2 \omega t + 2 \cos \omega t) dt$$

$$= \frac{1}{4} \int_{-\pi/\omega}^{\pi/\omega} \left[ 1 + \left( \frac{1 + \cos 2\omega t}{2} \right) + 2 \cos \omega t \right] dt$$

$$= \frac{1}{4} \int_{-\pi/\omega}^{\pi/\omega} \left[ 1 + \frac{1}{2} + \frac{\cos 2\omega t}{2} + 2 \cos \omega t \right] dt$$

$$= \frac{1}{4} \int_{-\pi/\omega}^{\pi/\omega} \left[ \frac{3}{2} + \frac{\cos 2\omega t}{2} + 2 \cos \omega t \right] dt$$

$$= \frac{1}{4} \left[ \int_{-\pi/\omega}^{\pi/\omega} \frac{3}{2} dt + \int_{-\pi/\omega}^{\pi/\omega} \frac{\cos 2\omega t}{2} dt + 2 \int_{-\pi/\omega}^{\pi/\omega} \cos \omega t dt \right]$$

$$= \frac{1}{4} \left[ \frac{3}{2} \cdot t \Big|_{-\pi/\omega}^{\pi/\omega} + 0 + 0 \right]$$

$$= \frac{1}{4} \left( \frac{3}{2} \left( \frac{2\pi}{\omega} \right) \right) = \frac{3\pi}{4\omega}$$

— 5M

$$(ii) x(t) = e^{-3t} u(t)$$

$$E = \lim_{T \rightarrow \infty} \int_{-T}^T |x(t)|^2 dt$$

$$= \lim_{T \rightarrow \infty} \int_{-T}^T (e^{-3t} u(t))^2 dt$$

$$= \lim_{T \rightarrow \infty} \int_{-T}^T e^{-6t} u(t) dt$$

$$= \lim_{T \rightarrow \infty} \int_{-T}^0 e^{-6t} u(t) dt + \lim_{T \rightarrow \infty} \int_0^T e^{-6t} u(t) dt$$

$$= \lim_{T \rightarrow \infty} 0 + \lim_{T \rightarrow \infty} \int_0^T e^{-6t} dt$$

$$= \lim_{T \rightarrow \infty} \int_0^T e^{-6t} dt = \lim_{T \rightarrow \infty} \frac{e^{-6t}}{-6} \Big|_0^T = \lim_{T \rightarrow \infty} \frac{e^{-6T} - e^0}{-6}$$

$$= \frac{e^{-\infty} - e^0}{-6} = \frac{-1}{-6} = \frac{1}{6} \quad \underline{\underline{-3M}}$$

$$(iii) x[n] = n \quad 0 \leq n \leq 5$$

$$E = \lim_{N \rightarrow \infty} \sum_{n=-\infty}^{\infty} (x[n])^2$$

$$E = \sum_{n=0}^5 |x[n]|^2$$

$$= \sum_{n=0}^5 n^2 = 0 + 1^2 + 2^2 + 3^2 + 4^2 + 5^2 = 55$$

-2M

10M

$$\textcircled{2} \textcircled{a} x(t) = \begin{cases} 2t & 0 \leq t < 1 \\ 2 + \sin(2\pi t) & 1 \leq t < 2 \\ 4 - t & 2 \leq t < 4 \\ 0 & \text{otherwise} \end{cases}$$

$$E = \lim_{T \rightarrow \infty} \int_{-T}^T |x(t)|^2 dt$$

$$E = \int_0^1 (2t)^2 dt + \int_1^2 (2 + \sin(2\pi t))^2 dt + \int_2^4 (4-t)^2 dt \quad - 1M$$

$$= \int_0^1 4t^2 dt + \int_1^2 (4 + \sin^2 2\pi t + 4 \sin(2\pi t)) dt + \int_2^4 (16 + t^2 - 8t) dt$$

$$= 4 \frac{t^3}{3} \Big|_0^1 + 4t \Big|_1^2 + \int_1^2 \sin^2(2\pi t) dt + 4 \int_1^2 \sin(2\pi t) dt + \left[ 16t \Big|_2^4 + \frac{t^3}{3} \Big|_2^4 - \frac{8t^2}{2} \Big|_2^4 \right] \quad - 2M$$

$$= \frac{4}{3} + 4 + \int_1^2 \frac{1 - \cos 4\pi t}{2} dt + 4 \frac{(-\cos 2\pi t)}{2\pi} \Big|_1^2 + 16(2) + \frac{56}{3} - 4(12) \quad - 1M$$

$$= \frac{16}{3} + \frac{1}{2} t \Big|_1^2 - \frac{1}{2} \int_1^2 \cos 4\pi t dt + \frac{2}{\pi} (-\cos 4\pi + \cos 2\pi) + 32 + \frac{56}{3} - 48$$

$$= \frac{16}{3} + \frac{1}{2} - \frac{1}{2} \frac{(\sin 4\pi t)}{4\pi} \Big|_1^2 + \frac{2}{\pi} (-1+1) + \frac{8}{3} \quad - 1M$$

$$= 8 + \frac{1}{2} - \frac{1}{8\pi} (\sin 8\pi - \sin 4\pi) + 0 = \frac{17}{2} - 0$$

$$E_{x(t)} = \frac{17}{2}$$

— 2M

$$E_{x(t)} = 8.5$$

— 7M

②⑥

## Energy Signal

1. The total energy is obtained

$$\text{using } E = \lim_{T \rightarrow \infty} \int_{-T}^T |x(t)|^2 dt$$

for DTS

$$E = \lim_{N \rightarrow \infty} \sum_{n=-N}^{\infty} (x[n])^2$$

2. for the energy signal  
Energy is finite  $0 < E < \infty$

3. The average power  $P = 0$ .

4. Non-Periodic signals are  
energy signals.

5. Energy signals are not  
time limited.

## Power Signal

1. The average power is obtained

$$\text{using } P = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^T |x(t)|^2 dt$$

$$P = \lim_{N \rightarrow \infty} \frac{1}{2N+1} \sum_{n=-N}^N (x[n])^2$$

2. The power of a power signal  
is finite.  $0 < P < \infty$ .

3. The energy 'E' should be  
infinity  $E = \infty$ .

4. periodic signals are power  
signals. However all power  
signals not periodic.

5. Power signals exist over  
infinite time.

--- 3M  
-----  
1QM

3) (a)  $y[n] = x[n] u[n+1]$

(i) Linearity: The given system is similar to  $y[n] = m x[n]$

form. So the system is Linear — 1M

$$T[\alpha x_1[n] + \beta x_2[n]] \rightarrow \alpha y_1[n] + \beta y_2[n]$$

(ii) Time-invariant: In the given system, "n" exist in

$x[n]$  and  $u[n+1]$  terms. The system is Time-variant — 1M

$$y[n] \neq y[n-n_0]$$

(iii) Causality: The <sup>present</sup> o/p of the system depends only on the

present i/p system. So, the given system is Causal — 1M

(iv) Memoryless: The present o/p of the given system only depends on the present i/p. So the given system is static (or) Memoryless. — 1M

(v) Stable: The given system is stable.

$$y[n] = x[n] u[n+1]$$

$x[n] \rightarrow$  Bounded i/p

$u[n+1] \rightarrow$  Bounded signal (step).

$y[n] \rightarrow$  Bounded o/p.

$\therefore$  The system is stable. — 1M

SM

$$(b) y(t) = \int_{-\infty}^t x(\tau) d\tau.$$

(i) Linearity :- The given system consists the integrator, which is linear operator. So, the given system is linear — 1M

$$T [\alpha x_1(t) + \beta x_2(t)] = \alpha y_1(t) + \beta y_2(t).$$

(ii) Time-invariant :- In the given system, the integral

limits  $-\infty$  to  $t$ .

$$y_1(t) = \int_{-\infty}^t x(\tau) d\tau = \int_{-\infty}^{t-t_0} x(\tau) d\tau$$

$$y(t-t_0) = \int_{-\infty}^{t-t_0} x(\tau) d\tau =$$

$$y_1(t) = y(t-t_0) \quad \text{--- 1M}$$

$\therefore$  The given system is time-invariant.

(iii) Causality :- The given system has integral term with limits  $-\infty$  to  $t$ .

The present o/p depends on past and present i/p, then the system is Causal. — 1M

(iv) Memoryless :- The present o/p depends on past and present i/p, the system is dynamic system (or) Memory — 1M

(v) Stable :- The given system is ~~stable~~ unstable. — 1M

$$y(t) = \int_{-\infty}^t x(\tau) d\tau.$$

$$\text{let } x(\tau) = u(\tau), \quad y(t) = \int_{-\infty}^t u(\tau) d\tau = r(t).$$

$x(t) \rightarrow$  bounded signal,

$y(t) =$  unbounded signal.

$\therefore$  The given system unstable system. — 1M

#### ④ (a) Condition for causality of an Impulse response of an LTI System

Sol:

If a system is said to be causal, if the present o/p depends on past and present i/p.

from the definition of convolution,  $y[n] = x[n] * h[n]$

$$y[n] = \sum_{k=-\infty}^{\infty} h[k] x[n-k] \quad \text{--- 1M}$$

for a LTI system to be causal,

$$h[k] = 0 \quad k < 0 \quad \text{Discrete time signal.}$$

$$h(t) = 0 \quad t < 0, \quad \text{Continuous time signal.}$$

--- 1M

#### Condition for stability of an impulse response of an LTI System

If a system is said to be stable, if it produces bounded output for every bounded input.

$$y[n] = \sum_{k=-\infty}^{\infty} h[k] x[n-k] \quad \text{--- 1M}$$

~~$y[n]$~~  s.t.  $x[n-k]$  is bounded input,

to make,  $y[n]$  to be bounded,

$$\sum_{k=-\infty}^{\infty} |h[k]| < \infty \quad \text{--- 1M}$$

$$\int_{-\infty}^{\infty} |h(t)| dt < \infty \quad \text{--- 4M}$$

(4) (b) Given impulse responses,

(i)  $h(t) = e^{2t} u(t-1)$ .

The given system is Causal,

$h(t) = 0, t < 0.$



$$u(t-1) = \begin{cases} 1 & t > 1 \\ 0 & t < 1 \end{cases}$$

(ii) To evaluate stability,

$$\int_{-\infty}^{\infty} h(t) dt = \int_{-\infty}^{\infty} e^{2t} u(t-1) dt$$

$$= \int_1^{\infty} e^{2t} dt$$

$$= \left. \frac{e^{2t}}{2} \right|_1^{\infty} = \frac{1}{2} (e^{\infty} - e^2) = e^{\infty} = \infty.$$

$$u(t-1) = \begin{cases} 1 & t > 1 \\ 0 & t < 1 \end{cases}$$

$\therefore$  The given system is unstable

← 2M

(or)  
 $h(t) = e^{2t} u(t-1)$

$$u(t-1) = \begin{cases} 1 & t > 1 \\ 0 & t < 1 \end{cases}$$

$$h(t) = e^{2t} u(t-1) = \begin{cases} e^{2t} & t > 1 \\ 0 & t < 1 \end{cases}$$

$\therefore$  The given system is Causal

3M.

$$(ii) h[n] = \left(\frac{1}{2}\right)^n u[n]$$

$$u[n] = \begin{cases} 1 & n \geq 0 \\ 0 & n < 0. \end{cases}$$

$$\therefore h[n] = \left(\frac{1}{2}\right)^n u[n] = \begin{cases} \left(\frac{1}{2}\right)^n & n \geq 0 \\ 0 & n < 0 \end{cases}$$

$\therefore$  The given system is causal.

1M

To evaluate the stability,

$$\sum_{k=-\infty}^{\infty} |h(k)| < \infty.$$

$$\sum_{k=-\infty}^{\infty} h(k) = \sum_{k=-\infty}^{\infty} \left(\frac{1}{2}\right)^k u(k)$$

$$= \sum_{k=0}^{\infty} \left(\frac{1}{2}\right)^k = \frac{1}{1 - \left(\frac{1}{2}\right)}$$

$$= \frac{1}{\left(\frac{1}{2}\right)} = 2 < \infty.$$

$\therefore$  The given system is stable.

2M

3M.

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$$\sum_{k=0}^n \alpha^k = \frac{1 - \alpha^{n+1}}{1 - \alpha}$$
$$\sum_{k=0}^{\infty} \alpha^k = \frac{1}{1 - \alpha}$$

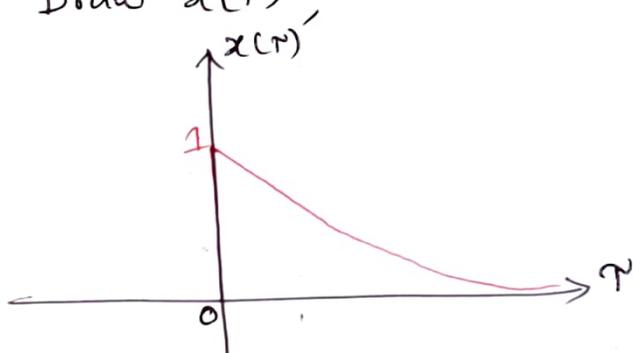
⑤ input  $x(t) = e^{-5t} u(t)$

impulse response  $h(t) = u(t)$ .

output  $y(t) = ?$

$$y(t) = x(t) * h(t) = \int_{-\infty}^{\infty} x(\tau) h(t-\tau) d\tau. \quad - 1M$$

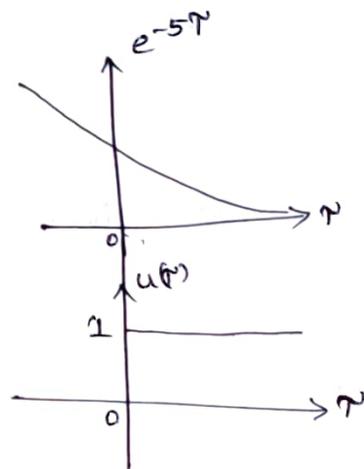
step 1:- Draw  $x(\tau)$



$$x(\tau) = e^{-5\tau} u(\tau)$$

$$= e^{-5\tau} \begin{cases} 1 & \tau > 0 \\ 0 & \tau < 0 \end{cases}$$

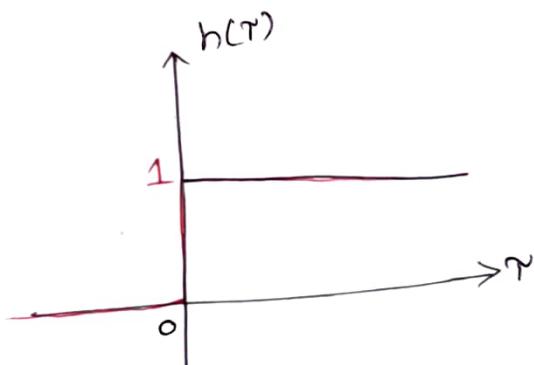
$$x(\tau) = \begin{cases} e^{-5\tau} & \tau > 0 \\ 0 & \tau < 0 \end{cases}$$



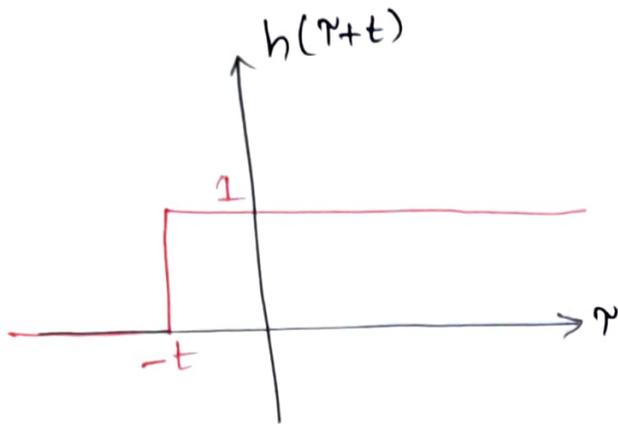
step 2:-

$$h(t-\tau) = h(-\tau+t)$$

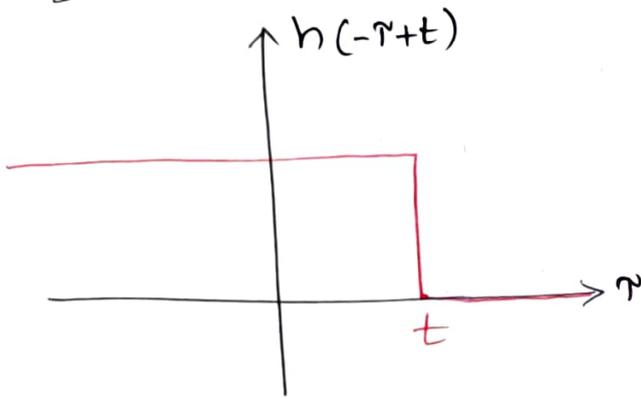
$$\text{Draw } h(\tau) = u(\tau) = \begin{cases} 1 & \tau > 0 \\ 0 & \tau < 0 \end{cases}$$



Step 3:-  $h(\tau+t)$

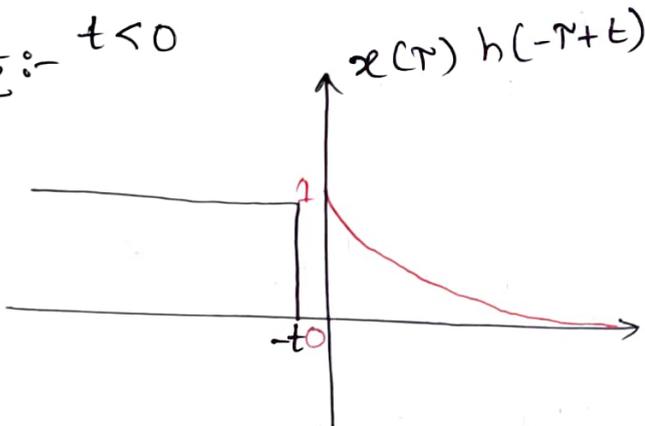


Step 4:- Draw  $h(-\tau+t)$



— 1M

Step 5:-  $t < 0$

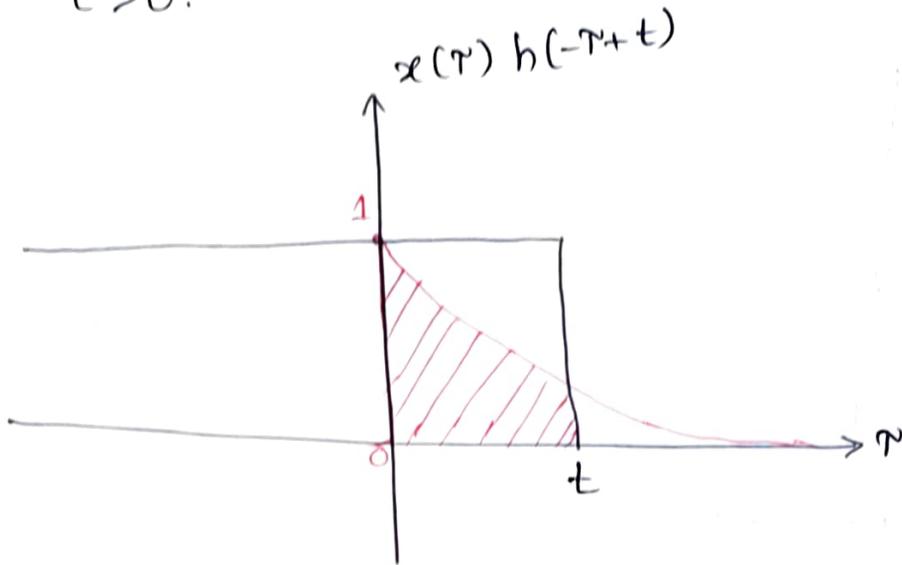


$$y(t) = x(t) * h(t) = \int_{-\infty}^{\infty} x(\tau) h(t-\tau) d\tau$$

— 1M

$$= 0 \quad (\text{No common Area}).$$

Step 6:-  $t > 0$ .



$$y(t) = x(t) * h(t) = \int_0^t x(\tau) h(t-\tau) d\tau$$

$$= \int_0^t e^{-5\tau} d\tau$$

$$= \frac{e^{-5\tau}}{-5} \Big|_0^t$$

$$= \frac{(e^{-5t} - e^0)}{-5}$$

$$= \frac{1}{5} (1 - e^{-5t}), \quad t > 0.$$

$$\therefore y(t) = \begin{cases} \frac{1}{5} (1 - e^{-5t}) & t > 0 \\ 0 & t < 0. \end{cases}$$

— 5M

$$\therefore y(t) = \frac{1}{5} (1 - e^{-5t}) u(t)$$

— 1M  
— 10M

⑥ Given data,

input  $x[n] = (0.6)^n u[n]$

impulse response  $h[n] = (0.2)^n u[n]$

output  $y[n] = ?$

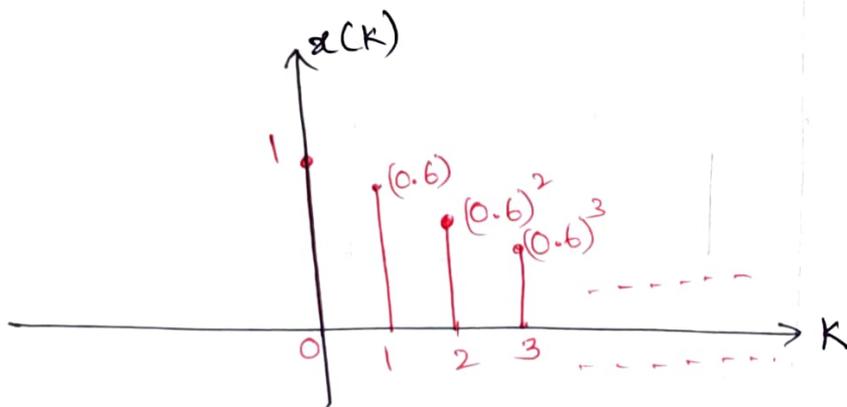
$$y[n] = x[n] * h[n] = \sum_{k=-\infty}^{\infty} x[k] h[n-k]$$

— IM

Step 1 :- Draw  $x(k) = (0.6)^k u(k)$ .

$$= (0.6)^k \begin{cases} 1 & k \geq 0 \\ 0 & k < 0 \end{cases}$$

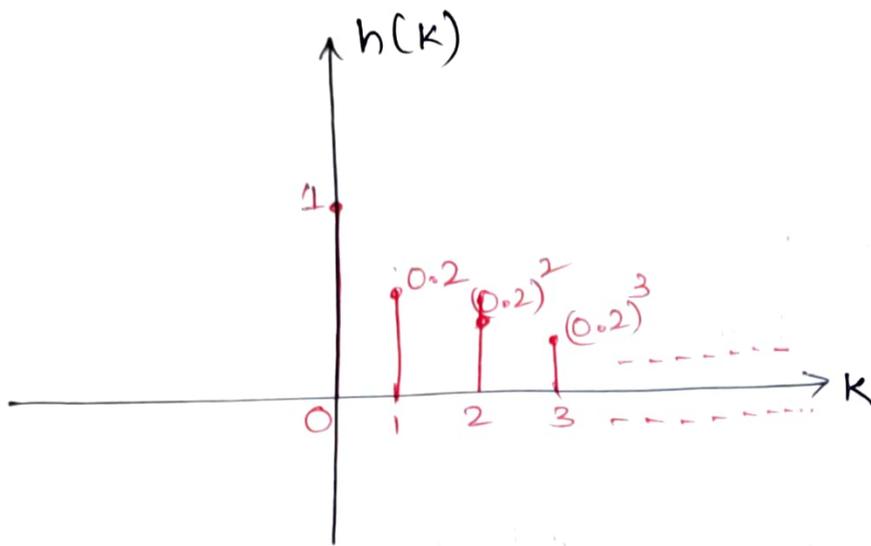
$$x(k) = \begin{cases} (0.6)^k & k \geq 0 \\ 0 & k < 0 \end{cases}$$



Step 2 :-  $h(n-k) = h(-k+n)$

Draw  $h(k) = (0.2)^k u(k)$

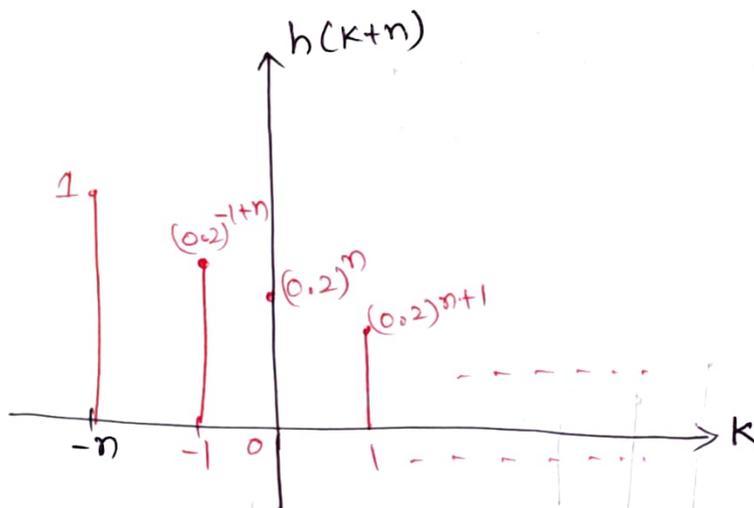
$$h(k) = \begin{cases} (0.2)^k & k \geq 0 \\ 0 & k < 0 \end{cases}$$



Step 3:- Draw  $h(k+n)$

$$h(k+n) = (0.2)^{k+n} u(k+n)$$

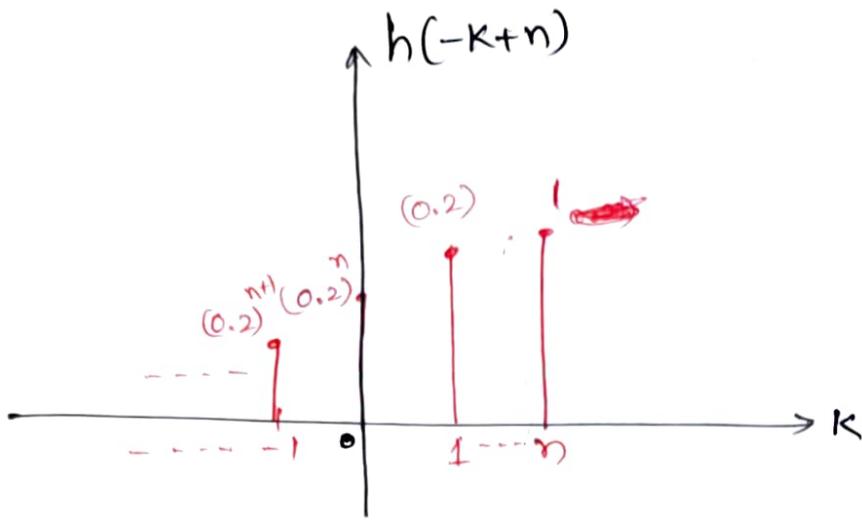
$$= \begin{cases} (0.2)^{k+n} & k \geq -n \\ 0 & k < -n \end{cases}$$



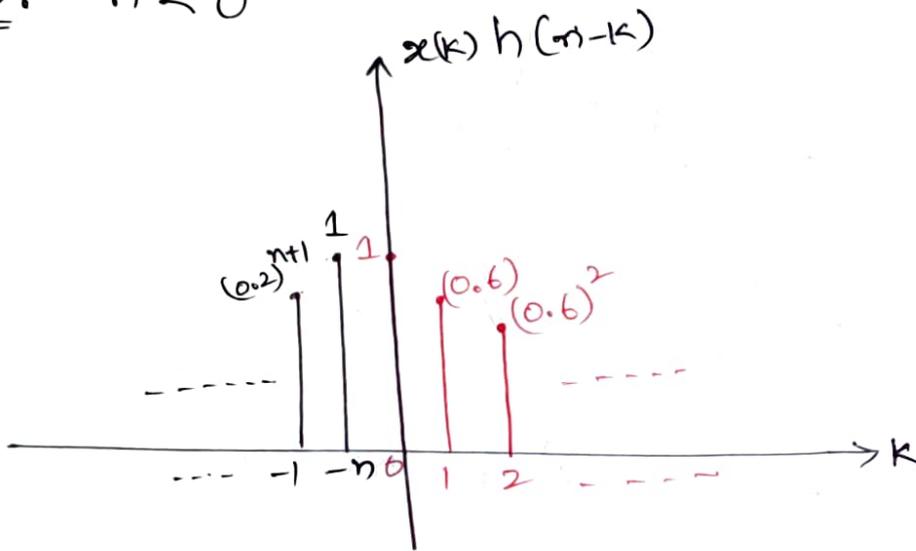
Step 4:- Draw  $h(-k+n)$

$$h(-k+n) = (0.2)^{-k+n} u(-k+n)$$

$$= \begin{cases} (0.2)^{-k+n} & k \leq n \\ 0 & k > n \end{cases}$$

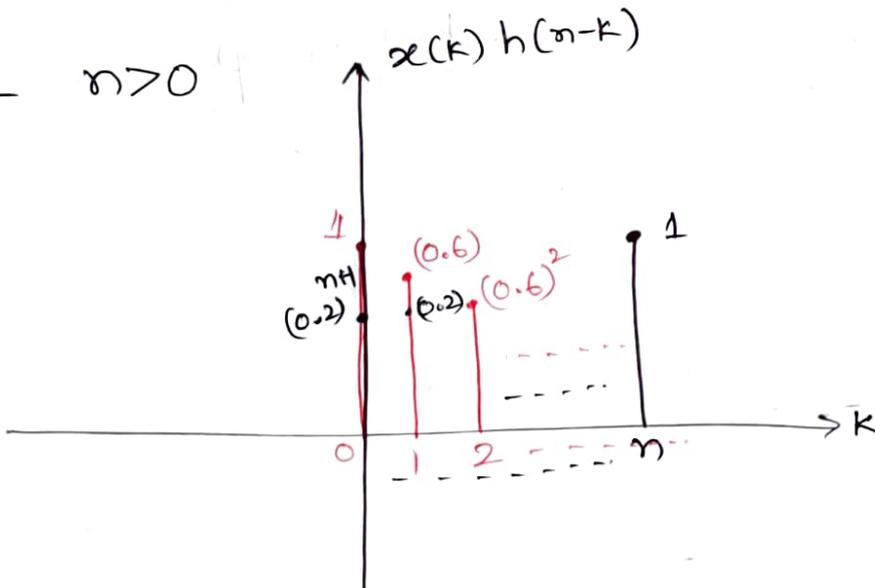


Step 5:-  $n < 0$



$$y[n] = 0 \quad n < 0.$$

Step 6:-  $n > 0$



$$y[n] = \sum_{k=0}^n (0.6)^k (0.2)^{n-k}$$

$$= \sum_{k=0}^n (0.6)^k \frac{(0.2)^n}{(0.2)^k}$$

$$= (0.2)^n \sum_{k=0}^n \left(\frac{0.6}{0.2}\right)^k$$

$$= (0.2)^n \sum_{k=0}^n 3^k$$

$$= (0.2)^n \left( \frac{1-3^{n+1}}{1-3} \right)$$

$$= (0.2)^n \left( \frac{1-3^{n+1}}{-2} \right)$$

$$= (0.2)^n \left( \frac{3^{n+1}-1}{2} \right)$$

$n > 0$ . — SM

$$\therefore y[n] = \begin{cases} (0.2)^n \left( \frac{3^{n+1}-1}{2} \right), & n > 0 \\ 0, & n < 0 \end{cases}$$

$$y[n] = (0.2)^n \left( \frac{3^{n+1}-1}{2} \right)$$

$u[n]$ . — 1M  
~~10M~~

7) (a) (i)  $3 \frac{dy(t)}{dt} + 2y(t) = 5 \frac{dx(t)}{dt}$

Step 1 :- To find natural response,  $x(t) = 0$ .

$$3 \frac{dy(t)}{dt} + 2y(t) = 0.$$

Step 2 :- find the characteristic equation,  ~~$\frac{d^k y(t)}{dt^k}$~~   $\frac{d^k y(t)}{dt^k} = r^k$

$$3r + 2 = 0$$

$$r = -2/3.$$

— 1M

Step 3 :- natural response (or) homogeneous solution.

$$y^{(h)}(t) = C_1 e^{rt}$$

$$y^{(h)}(t) = C e^{-2t/3}$$

— 1M  
— 2M

$$(ii) \quad y[n] - \frac{1}{3}y[n-1] + \frac{1}{2}y[n-2] = x[n] + x[n-1].$$

step 1:- To find natural response,  $x[n] = 0$ ,  $x[n-1] = 0$ .

$$y[n] - \frac{1}{3}y[n-1] + \frac{1}{2}y[n-2] = 0. \quad \text{--- 1M}$$

step 2:- characteristic equation,  $y[n-k] = \frac{1}{r^k}$

$$1 - \frac{1}{3r} + \frac{1}{2r^2} = 0$$

$$\frac{6r^2 - 2r + 3}{6r^2} = 0$$

$$6r^2 - 2r + 3 = 0.$$

$$\text{roots, } r = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{2 \pm \sqrt{4 - 72}}{12}$$

$$= \frac{2 \pm \sqrt{-68}}{12} = \frac{2 \pm \sqrt{68}j}{12}$$

$$= \frac{2 \pm j2\sqrt{17}}{12} \quad \text{--- 1M}$$

$$= \frac{1 \pm j\sqrt{17}}{6} = \frac{1+j\sqrt{17}}{6}, \frac{1-j\sqrt{17}}{6}$$

step 3:- homogeneous solution,

$$y^{(h)}(t) = c_1 e^{\left(\frac{1+j\sqrt{17}}{6}\right)t} + c_2 e^{\left(\frac{1-j\sqrt{17}}{6}\right)t} \quad \text{--- 1M}$$

3M

(7) (b)

$$y[n] - \frac{1}{4} y[n-1] - \frac{1}{8} y[n-2] = x[n] + x[n-1]$$

Step 1 :- To find forced response, Given input

$$x[n] = \left(\frac{1}{2}\right)^n u[n]$$

$$y^{(p)}[n] = K \left(\frac{1}{2}\right)^n u[n]$$

— 1M

Step 2 :-  $y[n] = K \left(\frac{1}{2}\right)^n$

$$y[n-1] = K \left(\frac{1}{2}\right)^{n-1} = 2K \left(\frac{1}{2}\right)^n$$

$$y[n-2] = K \left(\frac{1}{2}\right)^{n-2} = 4K \left(\frac{1}{2}\right)^n$$

— 1M

$$y[n] - \frac{1}{4} y[n-1] - \frac{1}{8} y[n-2] = x[n] + x[n-1]$$

$$K \left(\frac{1}{2}\right)^n - \frac{1}{4} 2K \left(\frac{1}{2}\right)^n - \frac{1}{8} 4K \left(\frac{1}{2}\right)^n = \left(\frac{1}{2}\right)^n + \left(\frac{1}{2}\right)^{n-1}$$
$$= \left(\frac{1}{2}\right)^n + 2 \left(\frac{1}{2}\right)^n$$

$$K \left(\frac{1}{2}\right)^n \left[ 1 - \frac{1}{2} - \frac{1}{2} \right] = 3 \left(\frac{1}{2}\right)^n$$

— 1M

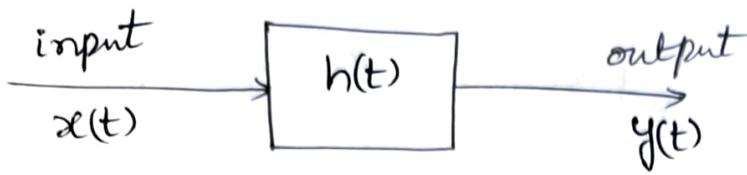
$$K = \text{undefined (or)} K = \infty$$

∴ The given system is unstable system.

forced response is not determined (or) Not exist  
for given input.

— 2M  
— 5M

8) a) Cascade connection of impulse responses.



$$y(t) = x(t) * h(t)$$



$$y_1(t) = x(t) * h_1(t)$$

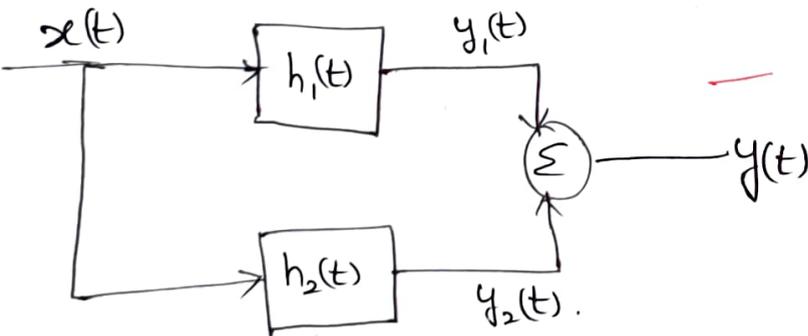
$$y(t) = y_1(t) * h_2(t)$$

$$y(t) = (x(t) * h_1(t)) * h_2(t)$$

$$y(t) = x(t) * (h_1(t) * h_2(t))$$

IM

Parallel connection of impulse responses.



$$y_1(t) = x(t) * h_1(t)$$

$$y_2(t) = x(t) * h_2(t)$$

$$y(t) = y_1(t) + y_2(t)$$

$$y(t) = x(t) * h_1(t) + x(t) * h_2(t)$$

$$y(t) = x(t) * (h_1(t) + h_2(t))$$

IM

SM

8(b)

$$x[n] = \{1, 3, 0, -1, 2, 1\}$$

$$h[n] = \{2, -1, 3\}$$

$$y[n] = x[n] * h[n] =$$

$$= \begin{array}{r} \begin{array}{cccccc} & 1 & 3 & 0 & -1 & 2 & 1 \\ 2 & 2 & 6 & 0 & -2 & 4 & 2 \\ -1 & -1 & -3 & 0 & 1 & -2 & -1 \\ 3 & 3 & 9 & 0 & -3 & 6 & 3 \end{array} \end{array} \quad \text{--- 4M}$$

$$y[n] = \{2, 5, 0, 7, 5, -3, 5, 3\} \quad \text{--- 1M}$$

5M.