

Internal Assessment Test 2 – February 2022

Sub:	Engineering Physics Theory				Sub Code:	21PHY12	Branch:	CS/IS/CIV/MECH		
Date:	28/02/2022	Duration:	90 min's	Max Marks:	50	Sem/Sec:	I Sem / A, B, C, D, E, F and G		OBE	
Answer any FIVE FULL Questions								MARKS	CO	RBT
Given: $c = 3 \times 10^8$ m/s; $h = 6.625 \times 10^{-34}$ Js; $k = 1.38 \times 10^{-23}$ J/K; $m_e = 9.1 \times 10^{-31}$ kg; $e = 1.6 \times 10^{-19}$ C										
1 (a)	Discuss the theory of forced oscillations and hence classify the conditions of variation of amplitude and phase with angular frequency.						[07]	CO2	L2	
(b)	Calculate the probability that an energy level at 0.2eV below Fermi level is occupied at temperature 500K.						[03]	CO3	L3	
2 (a)	Explain the Quantum Mechanical modifications to the classical free electron theory of metals to explain the electrical conductivity in solids and its success.						[07]	CO3	L3	
(b)	Find the resistivity in Intrinsic Germanium from the following data. $n = 2.4 \times 10^{10}/m^3$, $\mu_e = 0.39 m^2/Vs$, $\mu_h = 0.19 m^2/Vs$						[03]	CO2	L2	
3 (a)	Deduce the expression for electrical conductivity of a conductor using the quantum free electron theory of metals.						[06]	CO3	L2	
(b)	Show that occupation probability at an energy $E_F + \Delta E$ is equal to non-occupation probability at the energy $E_F - \Delta E$.						[04]	CO3	L4	
4 (a)	What is Hall effect? Obtain the expression for the Hall coefficient.						[07]	CO2	L3	
(b)	The Hall coefficient of certain silicon specimen was found to be $-7.35 \times 10^{-5} m^3 C^{-1}$. Determine the nature of the majority charge carriers and their number concentration.						[03]	CO2	L3	

PTO

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(b) A free particle is executing S.H.M in straight line with a period of 5 seconds. At the equilibrium point, the velocity is found to be 0.7m/s. Find the displacement at the end of 10 seconds, and also the amplitude of oscillation.	[3]	CO3	L3
6 (a) Define SHM and mention any two examples. Derive the differential equation using Hooke's law.	[6]	CO2	L3
(b) Given the damping constant of the medium 0.1 kg s^{-1} calculate the amplitude of the oscillations at resonance given the mass attached to the spring-mass oscillator $50 \times 10^{-3} \text{ kg}$, the amplitude of the applied periodic force 1N and the period of oscillations 1 second.	[4]	CO3	L4
7 (a) Define Fermi Energy. Find the electron density in Potassium if the Fermi energy is 3eV	[4]	CO3	L3
(b) Discuss the variation of Fermi factor with temperature.	[6]	CO3	L3
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IAT-2 PHYSICS SCHEME

1.a) Let $F = F_0 \sin \omega_f t$ be the oscillating applied force

The equation of motion is given by

$$F = ma = -kx - bv + F_0 \sin \omega_f t$$

$$m \frac{d^2 x}{dt^2} + b \frac{dx}{dt} + kx = F_0 \sin \omega_f t$$

$$\frac{d^2 x}{dt^2} + \frac{b}{m} \frac{dx}{dt} + \frac{k}{m} x = \frac{F_0}{m} \sin \omega_f t$$

$$\text{Let } \frac{b}{m} = 2R; \frac{k}{m} = \omega_o^2; \frac{F_0}{m} = F$$

$$\frac{d^2 x}{dt^2} + 2R \frac{dx}{dt} + \omega_o^2 x = F \sin \omega_f t \dots (1)$$

Let one particular solution be $x = A \sin(\omega_f t - \phi)$ (2 marks)

$$\frac{dx}{dt} = \omega_f A \cos(\omega_f t - \phi)$$

$$\frac{d^2 x}{dt^2} = -\omega_f^2 A \sin(\omega_f t - \phi)$$

Also

$$F \sin \omega_f t = F \sin(\omega_f t - \phi + \phi)$$

$$= F \sin(\omega_f t - \phi) \cos \phi + F \cos(\omega_f t - \phi) \sin \phi$$

Substituting in (1)

$$-\omega_f^2 A \sin(\omega_f t - \phi) + 2RA \omega_f \cos(\omega_f t - \phi) + \omega_o^2 A \sin(\omega_f t - \phi) = F \sin(\omega_f t - \phi) \cos \phi + F \cos(\omega_f t - \phi) \sin \phi$$

Comparing coefficients of

$\sin(\omega_f t - \phi)$ and $\cos(\omega_f t - \phi)$ on both sides

$$A(\omega_o^2 - \omega_f^2) = F \cos \phi$$

$$2RA \omega_f = F \sin \phi$$

$$\therefore F^2 = A^2(\omega_o^2 - \omega_f^2)^2 + 4R^2 A^2 \omega_f^2$$

$$A = \frac{F}{\sqrt{(\omega_o^2 - \omega_f^2)^2 + 4R^2 \omega_f^2}}$$

$$\tan \phi = \frac{2R \omega_f}{\omega_o^2 - \omega_f^2} \quad (3 \text{ marks})$$

Case 1: amplitude is infinity when $\omega_0 = \omega_f$, damping is zero

Case 2: Amplitude is less when $\omega_0 \neq \omega_f$ (2 marks)

1B (Formula-1mark, Substitution- 1 mark, Answer- 1 mark)

$$f(E) = \frac{1}{e^{\frac{E-E_f}{kT}} + 1}$$

$$= \frac{1}{e^{\frac{-\Delta E}{1.38 \times 10^{-23} \times 500}} + 1} = \frac{1}{e^{\frac{-0.02 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \times 500}} + 1} = 0.99$$

2A

Success of quantum theory: Quantum theory modified the energy of free electrons in metal to be quantized as per Paulis exclusion Principle and their distribution is given by Fermi – Dirac theory as

$$n(E)dE = g(E) dE f(E)$$

Where n(E) is number of conduction electrons per unit energy range

$$n(E)dE = g(E)dE \cdot f(E)$$

$$g(E) \text{ is density of states} = \frac{8\pi\sqrt{2}m^{\frac{3}{2}}}{h^3} E^{\frac{1}{2}}$$

f(E) is the Fermi probability factor . (2 marks)

1. Specific heat: (1 mark)

Classical theory predicted high values of specific heat for metals on the basis of the assumption that all the conduction electrons are capable of absorbing the heat energy as per Maxwell - Boltzmann

$$\text{distribution i.e., } C_V = \frac{3}{2} R$$

But according to the quantum theory, only those electrons occupying energy levels close to Fermi energy (E_f) are capable of absorbing heat energy to get excited to higher energy levels. Thus only a small percentage of electrons are capable of receiving the

thermal energy and specific heat value becomes small

It can be shown that $C_V = 10^{-4} R$.

This is in conformity with the experimental values. (2 marks)

2. Temperature dependence of electrical conductivity.

According to classical free electron theory,

$$\text{Electrical conductivity} \propto \frac{1}{\sqrt{\text{Temperature}}}$$

Where as from quantum theory

$$\text{Electrical conductivity} \propto \frac{1}{\text{collisional area of crosssection of lattice atoms}} \propto \frac{1}{\text{vibrational energy}} \propto \frac{1}{\text{Temperature}}$$

This is in agreement with experimental values.

3. Dependence of electrical conductivity on electron concentration: (2 marks)

According to classical theory,

$$\sigma = \frac{ne^2 \tau}{m} \Rightarrow \sigma \propto n$$

But it has been experimentally found that Zinc which is having higher electron concentration

than copper has lower Electrical conductivity.

According to quantum free electron theory,

Electrical conductivity $\sigma = \frac{ne^2}{m} \left(\frac{\lambda}{V_F} \right)$ where V_F is the Fermi

velocity.

Zinc possesses lesser conductivity because it has higher Fermi velocity.

Metal	n	σ
Cu	$8.45 \times 10^{28} / \text{m}^3$	$6 \times 10^7 (\Omega \text{m})^{-1}$
Zn	$13 \times 10^{28} / \text{m}^3$	$1 \times 10^7 (\Omega \text{m})^{-1}$

2B (Formula-1 mark, Substitution- 1 mark, Answer- 1 mark)

$$\rho = \frac{1}{\sigma} = \frac{1}{ne(\mu_e + \mu_h)} = 4.4 \times 10^8 \Omega \text{m}$$

3A.

Expression for Electrical conductivity:

Imagine a conductor across which an electric field E is applied. The free electrons acquire drift velocity and the matter wave number change from k_1 to k_2 in time interval τ_F in the presence of electric field.

The force on the free electron is

$$F = \frac{dp}{dt} = eE$$

$$k = \frac{2\pi}{\lambda} = \frac{2\pi}{h/p} = \frac{2\pi p}{h}$$

$$p = \frac{hk}{2\pi}$$

$$\frac{dp}{dt} = \frac{h}{2\pi} \left(\frac{dk}{dt} \right)$$

$$dk = \frac{2\pi}{h} eE dt$$

On integration $k_2 - k_1 = \Delta k = \frac{2\pi \cdot eE \cdot \tau_F}{h} \dots\dots(1)$ **(4 marks)**

From quantum theory, conductivity $J = \Delta k \cdot ne \cdot \frac{h}{2\pi \cdot m^*} \dots\dots\dots(2)$

Substituting (1) in (2)

We get $J = \frac{ne^2 \tau_F}{m^*} E \dots(3)$

Since from Ohm's, $J = \sigma E$, conductivity σ can be written as

$$\sigma = \frac{ne^2 \tau_F}{m^*} = \frac{ne^2}{m^*} \frac{\lambda}{v_F} \text{ (2 marks)}$$

3B For an energy level E above Fermi level by ΔE , Probability of occupation is

$$f(E) = \frac{1}{e^{\frac{E-E_F}{kT}} + 1} = \frac{1}{e^{\frac{+\Delta E}{kT}} + 1} \text{ (1 mark)}$$

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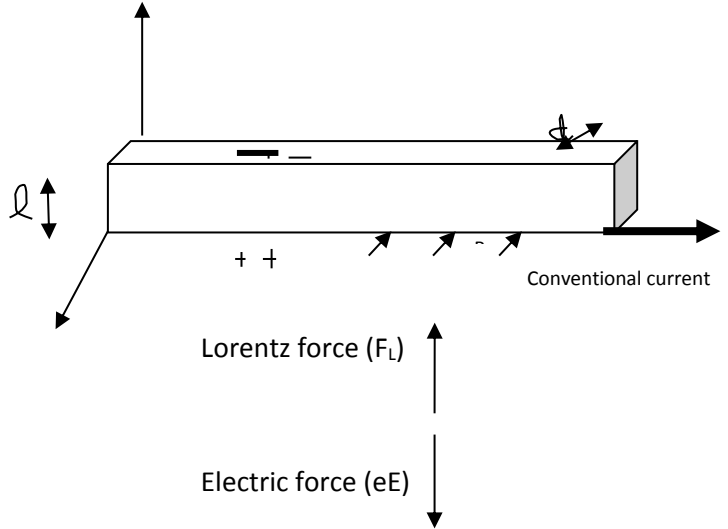
$$f(E) = \frac{1}{e^{\frac{E-E_F}{kT}} + 1} = \frac{1}{e^{\frac{-\Delta E}{kT}} + 1} \text{ (1 mark)}$$

Non occupation probability = $1 - f(E)$

$$= 1 - \frac{1}{e^{\frac{-\Delta E}{kT}} + 1} = \frac{e^{\frac{-\Delta E}{kT}} + 1 - 1}{e^{\frac{-\Delta E}{kT}} + 1} = \frac{1}{e^{\frac{-\Delta E}{kT}} + 1} = \frac{1}{1 + e^{\frac{+\Delta E}{kT}}}$$

(2 marks)

4A



Hall effect: When a conductor carrying current is placed in transverse magnetic field, an electric field is produced inside the conductor in a direction normal to both current and the magnetic field. **(1 mark)**

Here B is along $-X$, V is along $-Y$ axis
 Lorentz force = $-e(-\hat{j} \times X - \hat{i}) = +\hat{k}$
 So the electron is deflected along $+Z$ axis

Consider a rectangular slab of an n type semiconductor carrying a current I along $+X$ axis. Magnetic field B is applied along $-Z$ direction. Now according to Fleming's left hand rule, the Lorentz force on the electrons is along $+Y$ axis. As a result the density of electrons

increases on the upper side of the material and the lower side becomes relatively positive. This develops a potential V_H -Hall voltage between the two surfaces. Ultimately, a stationary state is obtained in which the current along the X axis vanishes and a field E_y is set up.
Expression for Hall Coefficient: (4 marks)

At equilibrium, Lorentz force is equal to force due to applied electric field

$$Bev_d = eE_H$$

$$\text{Hall Field } E_H = BV_d$$

$$\text{Current density } J = n_e ev_d$$

$$v_d = \frac{J}{n_e e}$$

$$E_H = B \frac{J}{n_e e}$$

Hence

$$\frac{E_H}{JB} = \frac{1}{n_e e} = R_H$$

Case 1: For P type semiconductor, the bottom surface will be at positive potential. (1 mark)

Case 2: For n type semiconductor, the bottom surface will be at positive potential (1 mark)

4B (Formula-1 mark, Substitution- 1 mark, Answer- 1 mark)

$$R_H = -7.35 \times 10^{-5} = \frac{1}{ne}$$

$$n = 8.5 \times 10^{22} / m^3$$

N type

5A In damped oscillations, the oscillator loses energy due to frictional forces causing the decrease in amplitude. (1 mark)

Let us assume that in addition to the elastic force $F = -kx$, there is a force that is opposed to the velocity, $F = b v$ where b is damping coefficient

For the oscillating mass in a medium with resistive coefficient b , the equation of motion is given by

$$m \frac{d^2 x}{dt^2} + kx + b \frac{dx}{dt} = 0$$

This is a homogeneous, linear differential equation of second order.

$$\text{The auxiliary equation is } D^2 + \frac{b}{m} D + \frac{k}{m} = 0$$

$$\text{The roots are } D_1 = -\frac{b}{2m} + \frac{1}{2m} \sqrt{b^2 - 4mk} \quad \text{and}$$

$$D_2 = -\frac{b}{2m} - \frac{1}{2m} \sqrt{b^2 - 4mk}$$

The solution can be derived as

$$x(t) = Ce^{-\left(\frac{b}{2m} - \frac{1}{2m} \sqrt{b^2 - 4mk}\right)t} + De^{-\left(\frac{b}{2m} + \frac{1}{2m} \sqrt{b^2 - 4mk}\right)t}$$

.....(1)

$$\text{Note: This can be expressed as } x(t) = Ae^{-\frac{b}{2m}t} \cos(\omega t - \phi)$$

$$\text{where } \omega = \sqrt{\frac{k}{m} - \left(\frac{b}{2m}\right)^2}$$

$$A = \sqrt{C^2 + D^2} \quad \phi = \tan^{-1}(D/C) \quad (4 \text{ marks})$$

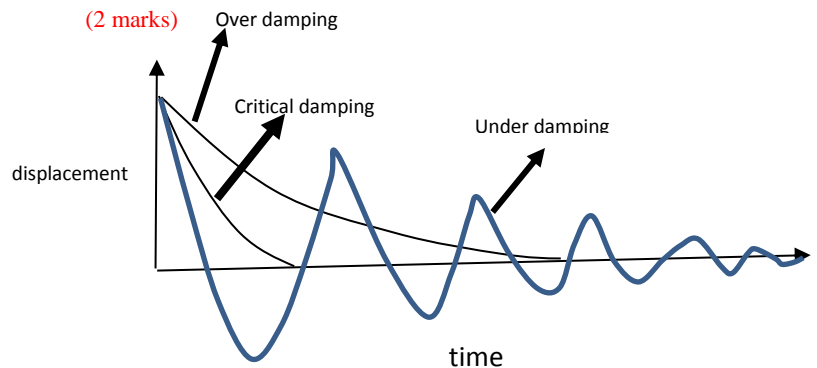
Here, the term $Ae^{-\frac{b}{2m}t}$ represents the decreasing amplitude and $(\omega t - \phi)$ represents phase

Case 1: $b^2 > 4mk$ OVER DAMPING

Case 2: $b^2 < 4mk$ UNDER DAMPING

Case 3: $b^2 = 4mk$ CRITICAL DAMPING

(2 marks)



5B (Formula-1 mark, Substitution- 1 mark, Answer- 1 mark)

$$\omega = \frac{2\pi}{T} = 1.25 \text{ rad/s}$$

$$V_{\text{max}} = 0.7 \text{ m/s} = \omega A$$

$$A = 0.56 \text{ m}$$

$$x = A \sin(\omega t) = -0.037 \text{ m}$$

6A

SIMPLE HARMONIC MOTION

It is the periodic oscillations of an object caused when the restoring force on the object is proportional to the displacement. The restoring force is directed opposite to displacement.

- Ex: 1. Oscillation of mass connected to spring
 2. Oscillations of prongs of Tuning fork
 3. Simple pendulum (2 marks)

Restoring force \propto - displacement

$$F = -kx$$

Here k is the proportionality constant known as spring constant. It represents the amount of restoring force produced per unit elongation and is a relative measure of stiffness of the material.

$$F_{\text{Restoring}} = -kx$$

$$m \frac{d^2x}{dt^2} = -kx$$

$$\text{Let } \omega_o^2 = \frac{k}{m}$$

$$\frac{d^2x}{dt^2} + \omega_o^2 x = 0$$

Here ω_o is angular velocity = $2\pi.f$

f is the natural frequency $f = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$

The Solution is of the form $x(t) = A \cos \omega_o t + B \sin \omega_o t$. (4 marks)

This can also be expressed as $x(t) = C \cos(\omega_o t - \theta)$ where

$$C = \sqrt{A^2 + B^2} \quad \tan \theta = B/A$$

6B (Formula-2marks, Substitution- 1 mark, Answer- 1 mark)

Amplitude of forced oscillations at resonance ($\omega_f = \omega_o$)

$$A = \frac{\frac{F_o}{m}}{\sqrt{(\omega_o^2 - \omega_f^2)^2 + \frac{b^2}{m^2} \omega_f^2}} = \frac{\frac{1}{0.05}}{\sqrt{0 + \frac{0.1^2}{0.05^2} \times 6.28^2}} = 1.59m$$

7A

It is the highest energy possessed by an electron at zero Kelvin. (1 mark)

(Formula-1mark, Substitution- 1 mark, Answer- 1 mark)

$$E_F = \frac{h^2}{8m} \left(\frac{3n}{\pi} \right)^{\frac{2}{3}}$$

$$\frac{3n}{\pi} = \left[\frac{8mxE_F}{h^2} \right]^{\frac{3}{2}}$$

$$n = 2.33 \times 10^{28} / m^3$$

7B.

To show that energy levels below Fermi energy are completely occupied:

For $E < E_F$, at $T = 0$,

$$f(E) = \frac{1}{e^{\frac{(E-E_F)}{kT}} + 1} \quad . (1 \text{ mark})$$

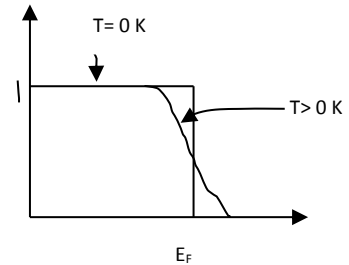
To show that energy levels above Fermi energy are empty:

For $E > E_F$, at $T=0$

$$f(E) = \frac{1}{e^{\frac{(E-E_F)}{kT}} + 1} = 0$$

At ordinary temperatures, for $E = E_F$,

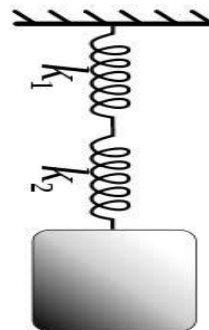
$$f(E) = \frac{1}{2} \quad . (4 \text{ marks})$$



Graph (1 mark)

8A

Expression for Spring Constant for Series Combination (3 marks)



Consider a load suspended through two springs with spring constants k_1 and k_2 in series combination. Both the springs experience same stretching force. Let Δx_1 and Δx_2 be their elongation.

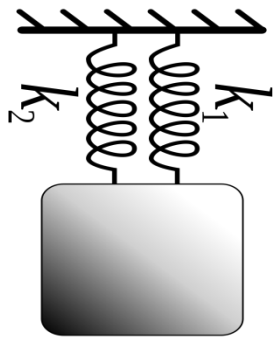
Total elongation is given by

$$\Delta X = \Delta X_1 + \Delta X_2 = \frac{F}{k_1} + \frac{F}{k_2}$$

$$\frac{F}{k_{eqv}} = \frac{F}{k_1} + \frac{F}{k_2}$$

$$\frac{1}{k_{eqv}} = \frac{1}{k_1} + \frac{1}{k_2}$$

Expression for Spring Constant for Parallel Combination (3 marks)



Consider a load suspended through two springs with spring constants k_1 and k_2 in parallel combination. The two individual springs both elongate by x but experience the load non uniformly.

Total load across the two springs is given by

$$F = F_1 + F_2$$

$$k_{eqv} \cdot \Delta X = k_1 \cdot \Delta X + k_2 \cdot \Delta X$$

$$k_{eqv} = k_1 + k_2$$

8B

$$\text{Electron current } I_e = n_e e A v_d(e)$$

$$\text{Hole current } I_h = n_h e A v_d(h)$$

current density

$$J = \frac{I}{A} = \frac{I_e + I_h}{A} = n_h e v_d(h) + n_e e v_d(e) = \sigma E \dots (1) \quad (2 \text{ marks})$$

(2 marks)

$$\text{But drift velocity } V_d = \mu E = \mu J / \sigma \quad \mu = V_d / E$$

$$\text{Using (1), } \sigma = n_e e \mu_e + n_h e \mu_h$$

In an intrinsic semiconductor, number of holes is equal to number of electrons.

$$\sigma_{int} = n_e e [\mu_e + \mu_{hole}] \quad (2 \text{ marks})$$

n_e is the electron concentration

n_p is the hole concentration

μ_e is the mobility of electrons

μ_h is the mobility of holes