





Fig. 2.1 Arrangement for study of a Townsend discharge

 $a$ , the average number of ionizing collisions made by an electron per centimetre travel in the direction of the field ( $\alpha$  depends on gas pressure  $p$ and EIp, ) and is called the Town send's first ionization coefficient).

The secondary ionization coefficient  $\gamma$  is defined in the same way as a, as the net number of secondary electrons produced per incident positive ion, photon, excited particle, or metastable particle, and the total value of  $\gamma$  is the sum of the individual coefficients due to the three different processes, i.e.,  $\gamma = \gamma 1 + \gamma 2 + \gamma 3 = \gamma$  is called the Townsend's secondary ionization coefficient and is a function of the gas pressure  $p$  and  $E/p$ .

## **CURRENT GROWTH IN THE PRESENCE OF SECONDARY PROCESSES**

The single avalanche process described in the previous section becomes complete when the initial set of electrons reaches the anode. However, since the amplification of electrons [exp(od)] is occurring in the field, the probability of additional new electrons being liberated in the gap by other mechanisms increases, and these new electrons create further avalanches. The other mechanisms are:

1. The positive ions liberated may have sufficient energy to cause liberation of electrons from the cathode when they impinge on it.

2. The excited atoms or molecules in avalanches may emit photons, and this will lead to the emission of electrons due to photo-emission.

3. The metastable particles may diffuse back causing electron emission.

Referring to Fig. 2.1 let us assume that  $n_0$  electrons are emitted from the cathode. When one electron collides with a neutral particle, a positive ion and an electron are formed. This is called an ionizing collision. Let  $\alpha$  be the average number of ionizing collisions made by an electron per centimetre travel in the direction of the field ( $\alpha$ iepends on gas pressure  $p$  and  $E/p$ , and is called the Townsend's first ionization coefficient). At any distance x from the cathode, let the number of electrons be  $n_x$ . When these  $n_x$  electrons travel a further distance of dx they give rise to  $(\alpha n_x dx)$ electrons.

$$
x = 0, n_x = n_0 \tag{2.6}
$$

Also,

At

$$
\frac{d n_x}{dx} = \alpha n_x; \text{ or } n_x = n_0 \exp{(\alpha x)} \tag{2.7}
$$

Then, the number of electrons reaching the anode  $(x = d)$  will be

 $\overline{1}$ 

$$
n_d = n_0 \exp(\alpha \, d) \tag{2.8}
$$

The number of new electrons created, on the average, by each electron is

$$
\exp\left(\alpha d\right) - 1 = \frac{nd - n_0}{n_0} \tag{2.9}
$$

Therefore, the average current in the gap, which is equal to the number of electrons travelling per second will be

$$
I = I_0 \exp{(\alpha \, d)} \tag{2.10}
$$

 $(2.11)$ 

 $(2.12)$ 

where  $I_0$  is the initial current at the cathode.

The electrons produced by these processes are called secondary electrons. The

Following Townsend's procedure for current growth, let us assume

Following Townsend's procedure for current growth, let us assume  $n_0'$  = number of secondary electrons produced due to secondary ( $\gamma$ )

processes.

 $n_0$ " = total number of electrons leaving the cathode. Let

Then 
$$
n_0'' = n_0 + n_0
$$

The total number of electrons  $n$  reaching the anode becomes,

 $n = n_0'' \exp(\alpha d) = (n_0 + n_0') \exp(\alpha d);$ 

and

or

$$
n_0' = \gamma [n - (n_0 + n_0')]
$$

Eliminating  $n_0'$ ,

minating 
$$
n_0'
$$
,  
\n
$$
n = \frac{n_0 \exp(\alpha d)}{1 - \gamma [\exp(\alpha d) - 1]}
$$
\n
$$
I = \frac{I_0 \exp(\alpha d)}{1 - \gamma [\exp(\alpha d) - 1]}
$$



#### i)Suspended Particle Theory

- In commercial liquids, the presence of solid impurities cannot be avoided.
- These impurities will be present as fibrous or as dispersed solid particles.
- The permittivity of these particles  $(\epsilon 1)$  will be different from the permittivity of the liquid  $(\epsilon 2)$ .
- If we consider these impurities to be spherical particles of radius r, and if the applied field is E, then the particles experience a force F, where

$$
F = r^3 \frac{\varepsilon_1 - \varepsilon_2}{\varepsilon_1 + 2\varepsilon_2} E \cdot \frac{dE}{dx}
$$

- this force is directed towards a place of higher stress if  $\epsilon$ 1 >  $\epsilon$ 2 and towards a place of lower stress if  $\epsilon$ 1 <  $\epsilon$ 2 when  $\epsilon$ 1 is the permittivity of gas bubbles.
- The force given above increases as the permittivity of the suspended particles ( $\varepsilon$ 1) increases. If  $\varepsilon$ 1  $\rightarrow$ co

$$
F=r^3\ \frac{1-\epsilon_2/\epsilon_1}{1+2\epsilon_2/\epsilon_1}\ E\ \frac{dE}{dx}
$$
 
$$
\text{Let}\ \epsilon_1\to\infty
$$
 
$$
F=r^3E\cdot\frac{dE}{dx}
$$

- · Force will tend the particle to move towards the strongest region of the field.
- In a uniform electric field which usually can be developed by a small sphere gap, the field is the strongest in the uniform field region. Here  $dE/dx \rightarrow 0$  so that the force on the particle is zero and the particle remains in equilibrium.
- Particles will be dragged into the uniform field region.
- Permittivity of the particles is higher than that of the liquid, the presence of particle in the uniform field region will cause flux concentration at its surface.
- Other particles if present will be attracted towards the higher flux concentration.
- · The movement of the particle under the influence of electric field is opposed by the viscous force posed by the liquid and since the particles are moving into the region of high stress, diffusion must also be taken into account.
- We know that the viscous force is given by (Stoke's relation)
- $\cdot$  Fy=6 $\pi$ nny
- where  $\eta$  is the viscosity of liquid, r the radius of the particle and y the velocity of the particle.
- Equating the electrical force with the viscous force we have

$$
6\pi\eta rv = r^3 E \frac{dE}{dx} \quad \text{or} \quad v = \frac{r^2 E}{6\pi\eta} \frac{dE}{dx}
$$

· However, if the diffusion process is included, the drift velocity due to diffusion will be given by

$$
v_d = -\frac{D}{N}\frac{dN}{dx} = -\frac{KI}{6\pi\eta r}\frac{dN}{Ndx}
$$

$$
E_0 = \frac{1}{(\epsilon_1 - \epsilon_2)} \left[ \frac{2\pi\sigma(2\epsilon_1 + \epsilon_2)}{r} \left\{ \frac{\pi}{4} \sqrt{\left(\frac{V_b}{2rE_0}\right)} - 1 \right\} \right]^{\frac{1}{2}}
$$

- Where 6 is the surface tension of the liquid.
- *εl* is the permittivity of the liquid,
- $\cdot$   $\varepsilon$ 2 is the permittivity of the gas bubble.
- r is the initial radius of the bubble assumed as a sphere  $\ddot{\phantom{1}}$
- · Vb is the voltage drop in the bubble (corresponding to minimum on the Paschen's curve).
- · From this equation, it can be seen that the breakdown strength depends on the initial size of the bubble which in turn is influenced by the hydrostatic pressure and temperature of the liquid.

### iii) Stressed Oil Volume Theory

- In commercial liquids where minute traces of impurities are present, breakdown strength is determined by the "largest possible impurity" or "weak link".
- On a statistical basis it was proposed that electrical breakdown strength of oil is defined by the weakest region in the oil, the region which is stressed to maximum and by the volume of oil included in that region.
- In non-uniform fields, the stressed oil volume is taken as the volume which is contained between the maximum stress (Emax) contour and 0.9 Emax contour.
- According to this theory the breakdown strength is inversely proportional to the stressed oil volume. . The breakdown voltage is highly influenced by the gas content in the oil, the viscosity of the oil. and the presence of other impurities.
- These being uniformly distributed, increase in the stressed oil volume consequently results in a reduction in the breakdown voltage.
- The variation of the breakdown voltage stress with the stressed oil volume is shown in Fig.

### iii) Cavitation and the Bubble Theory

experimentally observed that in many liquids, the breakdown strength depends strongly on the applied hydrostatic pressure.



Townsend's Criteria  $\rightarrow$ enables the evaluation.  $\gamma$  $exp(d) -1$  $\checkmark$ breakdrun voltage of the gap by.<br>apprepriate values of  $\alpha/\beta$  and ay the use of  $\sigma$  $\gamma$   $\approx$ ewountin corresponding to E/P when the the cathode and also  $\frac{1}{10}$   $\frac{1}{10}$ damage disfortions are minimum Space charge. and experimental values matches Calculated gaps are short high on Long pressure 1/2 when Sulations lous. for uniform field  $\int_{0}^{\pi/2}$  $v_0$  / type Breakdown and purchion length tig  $\alpha$  $\sigma$  $a<sub>o</sub>$ defined Jum prisoner  $\frac{9a}{1}$  $0.85$ threshold exprime gquation **kand** the whompshird toreftland off and worth open the  $\sqrt{4}$ E  $f(\epsilon|e)$  pd  $\epsilon$  . e both sides:  $ln$ taking  $\mathsf{K}$ . E  $ln$  $\mathbf{1}$ pd  $\overline{a}$ ←  $\gamma$  $V_{\mathbf{b}}$  $E =$ uniform  $\frac{1}{2}$  $=$   $K$  $(bd)$  $\mathbf b$ pd pd pd  $P<sub>d</sub>$  $=$  F  $V_{\ell}$ the breakdron vo tone  $\sigma_{\rm c}$ Shows  $\alpha$ This Jild functi is unique  $\frac{g}{g}$  $\sigma$ form and clerko de  $H^0$ pressive product g matous. Parcher's  $\rightarrow$  $au.$ mean that breakin this rulation dos not propontional ł٥ product voltage is  $p$ d of the product pd the some region of the

6 Paschen's Law Curve  $\overline{\phantom{a}}$  $V_{L}$  $\bullet$ c  $\overrightarrow{pd}$ hat Experimentally obtained relation between<br>ionization coeff  $\alpha/p$  and field strangth for  $E_b(r)$ resperants 宁 con onset of conseation  $\epsilon$ 4  $\alpha$ 3 r  $\overline{2}$  $F$ The Townsend's outerise  $dd = k$ .  $\frac{\alpha}{\beta}$  $-\gamma \frac{V}{E}$  $\frac{\kappa}{\mathbf{P}}$  $\frac{\alpha}{\Gamma}$  $\overline{\mathbf{k}}$  $\frac{E}{P}$  $0r$  $\overline{\vee}$ 



fact that there exists o explain the  $\alpha$ in the potential rulat sparking minimum gap leng potential and . sparking between  $|c_{\alpha}|$ confirm Can M  $he'$  $h h$ 4 one eation  $ol<sub>k</sub>$  $H_{\text{c}}$  $\circ\downarrow$  $m$ compromised different c the gap with thavermind energics. 0 second that the lownsund's Assuming small.  $A$ ot conjaction U icient of  $i\alpha$ coc (pd) ming electrons Crossing values  $(\mathbf{r}^d)$  $\frac{1}{2}$ frequent collision the gab make morrie but the with gas moleculestan at  $ped)$ mm ketween the gained SUCCOSIVE collection 18 small that at (pd) min. Hence unless the Twor probability of loniesting  $\sqrt{a}$ V  $pd)$ In case of Pd onin clerkon Imaking arthout any collect Oross the gab and thus I the spacking G pd) mean point to righer Corresponding Form parim efficiency hence miorionum and Sporking potential.

upartile In pader to obtain minimum potential  $\sqrt{P}$  $V_{b} =$  $\mathbf{I}$ Legerithm in both n'des. Jaking  $\theta$  $ln$  $Apo$  $Bpo$  $V_{k}$  $Bpg$  $V_{b}$ .  $ln \frac{Apd}{K}$ and equating differentiating Vb with pd J derivally to ever Ш 代。 在长  $\underbrace{\mathsf{L}_{\mathsf{A}} \frac{\mathsf{A}_{\mathsf{P}} \mathsf{d}}{\mathsf{K}} * \mathsf{B} - \mathsf{B}_{\mathsf{P}} \mathsf{d} \cdot \frac{\mathsf{K}}{\mathsf{A}_{\mathsf{P}} \mathsf{d}}}{\mathsf{L}_{\mathsf{P}} \mathsf{d}}$  $dV_{b}$  $\overline{\omega}$  $\frac{d(\rho d)}{d}$  $\frac{1}{\sqrt{4}}$  $ln($  $2.$  $TLn$ In Apd  $\frac{A_{pd}}{A}$  $\mathfrak{b}$ K.  $2n$  Apd

÷ Analytical expression ton onencomeen sparking  $\Rightarrow$ embild can be obtained wring general potential  $-6t$ Έ ×  $A_{c}$ f  $= P A e^{-B P / \epsilon}$  $i.d$  $-8p\frac{1}{4}$  $d = pAe$  $\vee_{b}$  $rac{PA}{Z}$  $e^{Brd/V_b}$ e BAYVE  $\cdot$  1 =  $\alpha$  $PA$ e Bpd/Vi  $\frac{d}{d}$  $PA.$  $\alpha_0 \propto d = ln(1 + \frac{1}{2})$  $Brd/v_b$  $\alpha$ e  $\frac{1}{a}$ PA  $R_{\text{max}}$  $\frac{1}{2}$  $\Xi$ ln  $e$ PA  $v' =$ Comfant  $a/r$  $(1 + \frac{1}{2})$ tn K  $\overline{z}$  $\lambda \rightarrow \infty$ Bpd  $\vee$  $\vec{r}$  d= x K  $\rho$  $P A$ 









## $Find 6.25 T$ • Triggering of the spark gaps by focused laser beams is also adopted since the

# B) Breakdown In Electronegative gases

- It has been recognized that one process that gives high breakdown strength to a gas is the electron attachment in which free electrons get attached to neutral atoms or molecules to form negative ions.
- Since negative ions like positive ions are too massive to produce ionization due to collisions, attachment represents an effective way of removing electrons which otherwise would have led to current growth and breakdown at low voltages.
- The gases in which attachment plays an active role are called **electronegative gases.**

The most common attachment processes encountered in gases are

- In the case of impulse current generators using three electrode gaps for tripping and control, a certain special design is needed.
- The electrodes have to carry high current from the capacitor bank.
- Secondly, the electrode has to switch large currents in a small duration of time (in about a microsecond).
- Therefore, the switch should have very low inductance.
- The erosion rate of the electrodes should be low.
- For high current capacitor banks, a number of spark gap switches connected in parallel asshown in Fig. 6.25 are often used to meet the requirement.
- Recently, trigatron gaps are being replaced by triggered vacuum gaps,
- the advantage of the latter being fast switching at high currents  $(>100 \text{ kA})$  in a few nanoseconds.
- Triggering of the spark gaps by focused laser beams is also adopted since the performance is better than the conventional triggering methods.

(b) the **dissociative attachment** in which the gas molecules split into their constituent atoms and the electronegative atom forms a negative ion. These processes may be symbolically represented as:

*(a) Direct attachment*

*(b) Dissociative attachment*

- A simple gas of this type is oxygen. Other gases are sulphur hexafluoride, freon, carbon dioxide, and fluorocarbons.
- In these gases, 'A" is usual y sulphur or carbon atom, and 'B<sup>\*</sup> is oxygen atom or one of the halogen atoms or molecules.
- With such gases, the Townsend current growth equation is modified to include ionization and attachment
- **An attachment coefficient (η) is defined, as the number of attaching collisions made by one electron drifting one centimetre in the direction of the field.**

The Townsend breakdown criterion for **attaching gases** canalso be deduced by equating the denominator to zero:

<sup>(</sup>a) *the direct* **attachment** in which an electron directly attaches to form a negative ion,





$$
i_m = \frac{V}{\omega L} \left[ \exp(-\alpha t) \right] \sin(\omega t)
$$
  
where  

$$
\alpha = \frac{R}{2L} \text{ and } \omega = \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}
$$
  
The time taken for the current  $i_m$  to rise from zero to the first peak value is  

$$
t_1 = t_f = \frac{1}{\omega} \sin^{-1} \frac{\omega}{\sqrt{LC}} = \frac{1}{\omega} \tan^{-1} \frac{\omega}{\alpha}
$$
  
The duration for one half cycle of the damped oscillatory wave  $t_2$  is,  

$$
t_2 = \frac{\pi}{\sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}}
$$