MATDIP401

Fourth Semester B.E. Degree Examination, July/August 2022

Advanced Mathematics – II

Max. Marks: 100

Note: Answer any FIVE full questions.

- 1 a. Find the distance between the points A(1, 1, 1) and B(2, 3, 5). (06 Marks)
 - b. Find the angle between the lines whose direction cosines are proportional to 1, 2, 4 and -2, 15. (06 Marks)
 - c. If ℓ , m, n are the direction of cosines of a line then prove that $\ell^2 + m^2 + n^2 = 1$. (08 Marks)
- 2 a. Find the equation of the plane passing through the points (3, -3, 1) and parallel to the plane 2x + 3y + 5z + 6 = 0. (06 Marks)
 - b. Find the equation of the plane which passes through the points A(0, 1, 1), B(1, 1, 2) and C(-1, 2, -2). (06 Marks)
 - c. Show that points (2, 2, 0), (4, 5, 1), (3, 9, 4) and (0, -1, -1) are coplanar. (08 Marks)
- 3 a. If $\vec{a} = 2\hat{i} + 3\hat{j} \hat{k}$, $\vec{b} = \hat{i} 2\hat{j} + \hat{k}$ and $\vec{c} = 3\hat{i} \hat{j} + 2\hat{k}$. Find $2\vec{a} + 3\vec{b} 2\vec{c}$. (06 Marks)
 - b. If $\vec{a} = (3, -1, 4)$, $\vec{b} = (1, 2, 3)$ and $\vec{c} = (4, 2, -1)$ find $\vec{a} \times (\vec{b} \times \vec{c})$ (06 Marks)
 - c. Prove that $\begin{bmatrix} \vec{a} + \vec{b}, \vec{b} + \vec{c}, \vec{c} + \vec{a} \end{bmatrix} = 2 \begin{bmatrix} \vec{a}, \vec{b}, \vec{c} \end{bmatrix}$ (08 Marks)
- 4 a. A particle moves along the curve $\vec{r} = (1-t^3)\hat{i} + (1+t^2)\hat{j} + (2t-5)\hat{k}$. Determine its velocity and acceleration. (06 Marks)
 - b. If $\vec{F} = (3xz 3yz)\hat{i} + (3y^2 3xz)\hat{j} + (3z^3 3xy)\hat{k}$, find div \vec{F} . (06 Marks)
 - c. Find Curl \vec{F} , whose $\vec{F} = (x + y + 1) \hat{i} + \hat{j} (x + y) \hat{k}$. (08 Marks)
- 5 a. A particle moves along the curve $\vec{r} = \cos 2t \hat{i} + \sin 2t \hat{j} + t \hat{k}$. Find its velocity and acceleration. (06 Marks)
 - b. Find the divergence of the rector $\vec{V} = xyz \hat{i} + 3x^2y \hat{j} + (xz^2 y^2z) \hat{k}$ (06 Marks)
 - c. If $\vec{r} = x \hat{i} + y \hat{j} + z \hat{k}$, show that Curl $\vec{r} = 0$. (08 Marks)
- a. Find the Laplace transform of 5Sin 2t + 3 Cos4t. (06 Marks)
 - b. Find the Laplace transform of Cos² 2t. (06 Marks)
 - c. Find the Laplace transform of
 i) Sin4t + e^{-3t}
 ii) Cosh2t + 2. (08 Marks)

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(06 Marks)

(06 Marks)

Find Laplace transform of t Cosat. Find the Laplace transform of $e^{-2t}[2 \text{ Cos } 5t - \text{Sin}5t]$. Find the inverse Laplace transform of $\frac{1}{s+2} + \frac{3}{2s+5}$

(08 Marks)

a. Solve $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 3y = e^{-x}$ with y(0) = y'(0) = 1, by using Laplace transform method.

(06 Marks)

b. Find $L^{-1} \left[\frac{1}{s(s^2 + a^2)} \right]$ by using convolution theorem.

(06 Marks)

Find the inverse Laplace transform of $\frac{1}{(s+1)(s-1)}$

(08 Marks)