



Second Semester B.E. Degree Examination, July/August 2022 Engineering Mathematics – II

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Solve : $(4D^4 - 4D^3 - 23D^2 + 12D + 36)y = 0$, where $D = \frac{d}{dx}$. (06 Marks)
- b. Solve $\frac{d^3y}{dx^3} + y = 65\cos(2x+1)$. (07 Marks)
- c. Solve : $y'' + 4y = x^2 + e^{-x}$ by the method of undetermined co-efficients. (07 Marks)

OR

- 2 a. Solve $\frac{d^2y}{dx^2} - 4y = \cosh(2x-1) + 3^x$. (06 Marks)
- b. Solve $(D^2 + D + 1)y = 1 - x + x^2$. (07 Marks)
- c. Solve $\frac{d^2y}{dx^2} + y = \frac{1}{1 + \sin x}$ by the method of variation of parameters. (07 Marks)

Module-2

- 3 a. Solve $x^3 \frac{d^3y}{dx^3} + 3x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} = x^3$. (06 Marks)
- b. Solve $p^2 + 2p \cot x = y^2$. (07 Marks)
- c. Modify the following equations into Clairaut's form and hence obtain its general and singular solution. $xp^2 - py + Kp + a = 0$. (07 Marks)

OR

- 4 a. Solve $(3x+2)^2 y'' + 3(3x+2)y' - 36y = 8x^2 + 4x + 1$. (06 Marks)
- b. Solve $p(p+y) = x(x+y)$. (07 Marks)
- c. Solve $(px-y)(py+x) = 2p$ by reducing it to Clairaut's form, by taking the substitution $X = x^2, Y = y^2$. (07 Marks)

Module-3

- 5 a. Form a PDE by eliminating arbitrary functions $\phi(x+y+z, x^2+y^2-z^2) = 0$. (06 Marks)
- b. Solve $\frac{\partial^2 z}{\partial x \partial y} = \sin x \sin y$ for which $\frac{\partial z}{\partial y} = -2 \sin y$ where $x = 0$ and $z = 0$ if y is an odd multiple of $\frac{\pi}{2}$. (07 Marks)
- c. Derive one dimensional wave equation in the form $\frac{\partial^2 u}{\partial t^2} = C^2 \frac{\partial^2 u}{\partial x^2}$. (07 Marks)

OR

- 6 a. Form a PDE by eliminating arbitrary functions, $z = yf(x) + x\phi(y)$. (06 Marks)
- b. Solve the equation $\frac{\partial^2 z}{\partial x^2} + z = 0$ given that $z = e^y$ and $\frac{\partial z}{\partial x} = 1$ when $x = 0$. (07 Marks)
- c. Find various possible solution of one dimensional heat equation, by the method of separation of variables. (07 Marks)

Module-4

- 7 a. Evaluate $\int_0^a \int_0^{x+y} \int_0^x e^{x+y+z} dz dy dx$. (06 Marks)
- b. Evaluate $\int_1^2 \int_1^{x^2} (x^2 + y^2) dy dx$ by changing the order of integration. (07 Marks)
- c. Derive the relation between Beta and Gamma function as $\beta(m, n) = \frac{\Gamma m \Gamma n}{\Gamma m+n}$. (07 Marks)

OR

- 8 a. Evaluate $\iint_R x^2 y dx dy$, where R is the region bounded by the lines $y = x$, $y + x = 2$ and $y = 0$. (06 Marks)
- b. Evaluate $\int_0^a \int_0^{\sqrt{a^2-y^2}} y \sqrt{x^2 + y^2} dx dy$ by changing into polars. (07 Marks)
- c. Show that $\int_0^\infty x e^{-x^8} \times \int_0^\infty x^2 e^{-x^4} dx = \frac{\pi}{16\sqrt{2}}$. (07 Marks)

Module-5

- 9 a. Find the Laplace transform of $2^t + \frac{\cos 2t - \cos 3t}{t}$. (06 Marks)
- b. If $f(t) = \begin{cases} t, & 0 \leq t \leq a \\ 2a - t, & a \leq t \leq 2a \end{cases}$, $f(t+2a) = f(t)$
Sketch the graph of $f(t)$ as a periodic function and show $L[f(t)] = \frac{1}{s^2} \tanh\left(\frac{as}{2}\right)$. (07 Marks)
- c. Find the inverse Laplace transform of $\frac{s^2}{(s^2 + a^2)^2}$, using convolution theorem. (07 Marks)

OR

- 10 a. Express $f(t) = \begin{cases} \cos t: & 0 < t \leq \pi \\ 1: & \pi < t \leq 2\pi \\ \sin t: & t > 2\pi \end{cases}$ in terms of unit step function and hence find its Laplace transform. (06 Marks)
- b. Find the inverse Laplace transform of $\frac{5s + 3}{(s-1)(s+1)^2}$. (07 Marks)
- c. Solve the differential equation $\frac{d^2 y}{dx^2} + 5 \frac{dy}{dx} + 6y = e^{2x}$, $y(0) = 2$, $y'(0) = 1$ using Laplace transform method. (07 Marks)

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