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15EC36

Third Semester B.E. Degree Examination, July/August 2022 Engineering Electromagnetics

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. State and prove Coulomb's law. (05 Marks)
- b. Three equal charges of $1 \mu\text{C}$ each are located at the three corners of a square of 10 cm side. Find the electric field intensity at the fourth vacant corner of the square. (06 Marks)
- c. A charge $Q_1 = -20 \mu\text{C}$ is located at $P(-6, 4, 6)$ and a charge $Q_2 = 50 \mu\text{C}$ is located at $R(5, 8, -2)$ in a free space. Find the force exerted on Q_2 by Q_1 in vector form. The distance given in meter. (05 Marks)

OR

- 2 a. Derive the expression of electric field intensity for infinite line charge. (08 Marks)
- b. Find the electric field \vec{E} at the origin, if the following charge distributions are present in free space:
 - (i) Point charge 12 nC at $P(2, 0, 6)$
 - (ii) Uniform line charge of linear 3 nC at $x = 2, y = 3$. (08 Marks)

Module-2

- 3 a. State and prove Gauss's law. (05 Marks)
- b. State and prove Divergence theorem. (05 Marks)
- c. If $\vec{D} = xy^2z^2\hat{a}_x + x^2yz^2\hat{a}_y + x^2y^2z\hat{a}_z \text{ C/m}^2$.
Find :
 - (i) An expression for ρ_v
 - (ii) The total charge within the cube defined by $0 \leq x \leq 2, 0 \leq y \leq 2, 0 \leq z \leq 2$. (06 Marks)

OR

- 4 a. Derive the expression for work done in terms of line integral. (06 Marks)
- b. Given $V = \frac{\cos 2\phi}{r}$ in the free space, in cylindrical system:
 - (i) Find \vec{E} at $B(2, 30^\circ, 1)$.
 - (ii) Find the volume charge density at point $A(0.5, 60^\circ, 1)$. (10 Marks)

Module-3

- 5 a. Derive the expression for Poisson's and Laplace's equation. (04 Marks)
- b. Determine whether or not the following potential field satisfy the Laplace's equation:
 - (i) $V = x^2 - y^2 + z^2$
 - (ii) $V = r \cos \phi + z$ (04 Marks)
- c. Use Laplace's equation to find the capacitance per unit length of a co-axial cable of inner radius 'a' in and outer radius 'b' m. Assume $V = V_0$ at $r = a, V = 0$ at $r = b$. (08 Marks)

OR

- 6 a. State and explain Biot-Savart law. (05 Marks)
 b. State and prove the Stoke's theorem. (06 Marks)
 c. Given $\vec{A} = (\sin 2\phi)\hat{a}_\phi$ in cylindrical coordinates. Find curl of \vec{A} at $\left(2, \frac{\pi}{4}, 0\right)$. (05 Marks)

Module-4

- 7 a. Derive the expression for the force on a differential current element. (06 Marks)
 b. A point charge of $Q = 1.2C$ has velocity $\vec{v} = (5\hat{a}_x + 2\hat{a}_y - 3\hat{a}_z)$ m/s. Find the magnitude of the force exerted on the charge if,
 (i) $\vec{E} = -18\hat{a}_x + 5\hat{a}_y - 10\hat{a}_z$ V/m
 (ii) $\vec{B} = -4\hat{a}_x + 4\hat{a}_y + 3\hat{a}_z$ T. (10 Marks)

OR

- 8 a. Write short notes on Magnetization and Permeability. (06 Marks)
 b. Derive the boundary condition for tangential component in magnetic field. (05 Marks)
 c. A coil of 500 turns is wound on a closed iron ring of mean radius 10 cm and cross section area of 3 cm^2 . Find the self inductance of the winding if the relative permeability of iron is 800. (05 Marks)

Module-5

- 9 a. Write the Maxwell equations in point form and integral form. (06 Marks)
 b. Given $\vec{E} = E_m \sin(\omega t - \beta z)\hat{a}_y$ in free space. Find \vec{D} , \vec{B} and \vec{H} . (06 Marks)
 c. Prove that $\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$. (04 Marks)

OR

- 10 a. Derive the general expression for uniform plane in free space. (05 Marks)
 b. State and prove Poynting theorem. (07 Marks)
 c. Calculate the attenuation constant and phase constant for a uniform plane wave with frequency of 10 GHz in polythelene for which $\mu = \mu_0$, $\epsilon_r = 2.3$ and $\sigma = 256 \times 10^{-4} \text{ } \Omega/\text{m}$. (04 Marks)
