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18EE61

Sixth Semester B.E. Degree Examination, July/August 2022 Control Systems

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Write the comparison between open loop and closed loop control system with example. (06 Marks)
- b. For the mechanical system shown in Fig. Q1 (b). Draw the electrical equivalent network based on torque-voltage analogy.

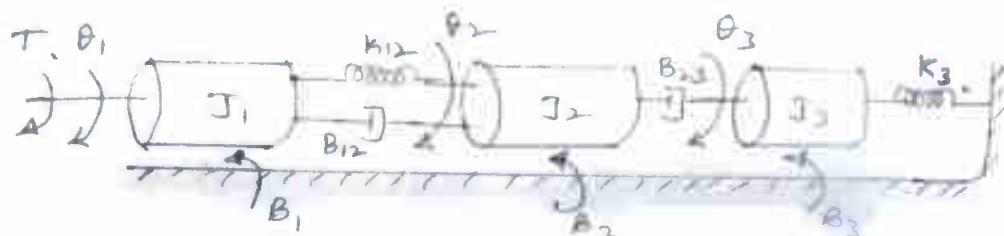


Fig. Q1 (b)

(08 Marks)

- c. For the electrical network shown in Fig. Q1 (c), obtain the transfer function $\frac{V_o(s)}{V_i(s)}$.

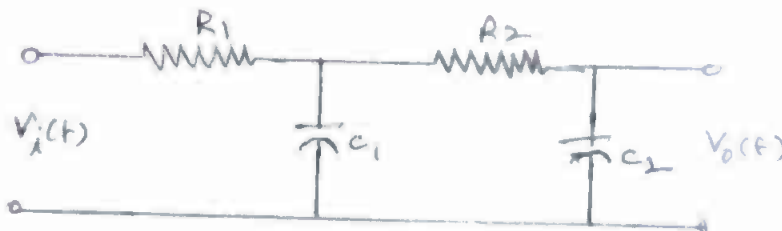


Fig. Q1 (c)

(06 Marks)

OR

- 2 a. Define Transfer function. Also derive the transfer function relating displacement and excitation voltage drop for the armature controlled D.C. motor. (06 Marks)
- b. Obtain the mathematical model for the mechanical system shown in Fig. Q2 (b). Draw the electrical equivalent based on F-I analogy.

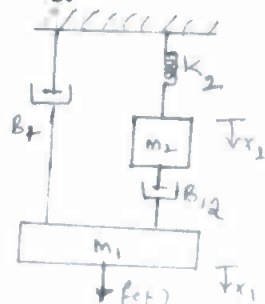


Fig. Q2 (b)

(08 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and /or equations written eg. 42+8 = 50, will be treated as malpractice.

c. Write the torque equation of the gear train shown in Fig. Q2 (c).

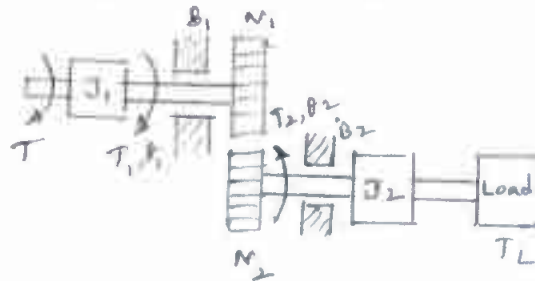


Fig. Q2 (c)

(06 Marks)

Module-2

3 a. Using block diagram, reduction technique obtain transfer function $\frac{C(s)}{R(s)}$, whose block diagram shown in Fig. Q3 (a).

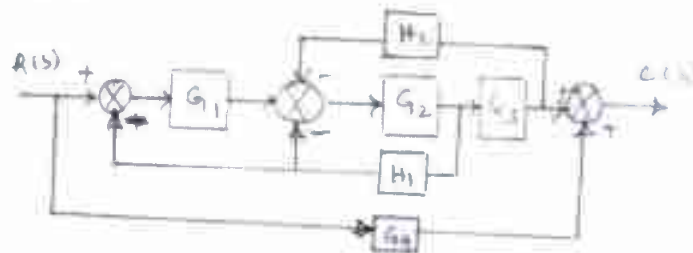
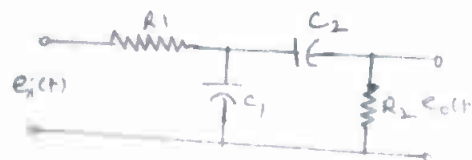


Fig. Q3 (a)

(10 Marks)

b. Draw a block diagram for the electric circuit shown in Fig. Q3 (b) and hence evaluates Transfer function, $\frac{E_o(s)}{E_i(s)}$ using block diagram reduction techniques.



- $R_1 = 100 \text{ K}\Omega$
- $R_2 = 1 \text{ M}\Omega$
- $C_1 = 10 \text{ }\mu\text{F}$
- $C_2 = 1 \text{ }\mu\text{F}$

Fig. Q3 (b)

(10 Marks)

OR

4 a. Using Mason's gain formula determine the Transfer function of the given signal flow graph shown in Fig. Q4 (a).

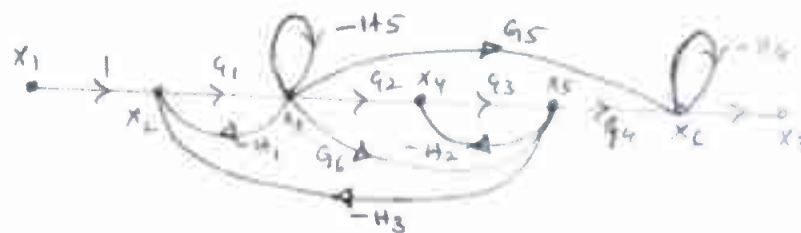


Fig. Q4 (a)

(10 Marks)

b. A system is described by the following set of linear equation. Draw the signal flow graph and obtain the Transfer function $\frac{X_5}{X_1}$.

$$X_2 = a_{12}X_1 + a_{22}X_2 + a_{32}X_3$$

$$X_3 = a_{23}X_2 + a_{43}X_4$$

$$X_4 = a_{24}X_2 + a_{34}X_3 + a_{44}X_4$$

$$X_5 = a_{25}X_2 + a_{45}X_4$$

(10 Marks)

Module-3

- 5 a. Define time domain specifications of the second order system with diagram. (05 Marks)
- b. A unity feedback system is characterized by an open loop Transfer Function $G(s) = \frac{K}{s(s+10)}$. Determine the gain 'K', so that system will have a damping ratio of 0.5. For the value of K determine the settling time, peak, overshoot, time to peak overshoot for a unit step input. (07 Marks)
- c. Open loop Transfer Function of a unity feedback system is given by $G(s) = \frac{K}{s(1+TS)}$, where K and T are positive constants. By what factor should the amplifier gain 'K' be reduced so that peak overshoot of a unit step response of the system is reduced from 75% to 25%. (08 Marks)

OR

- 6 a. A certain feedback control system is described by the following Transfer Function. $G(s) = \frac{K}{s^2(s+20)(s+30)}$, $H(s) = 1$. Determine order of system, Type number, Steady state error co-efficients and also determine the value of K to limit the steady state. Error 8 unit due to input $r(t) = 1 + 10t + 30t^2$. (05 Marks)
- b. For the characteristic equation given below. Determine the number of roots of the characteristics equation in the RHS of S-plane $s^6 + 3s^5 + 5s^4 + 9s^3 + 8s^2 + 6s + 4 = 0$ (07 Marks)
- c. A unity feedback control system is characterized by the open loop transfer function, $G(s) = \frac{K(s+13)}{s(s+3)(s+7)}$. Using R.H. criteria (i) Calculate the range of K for the system to be stable (ii) Determine the value of K which will cause sustained frequency of oscillations in the closed loop system. What are the corresponding oscillation frequencies? (08 Marks)

Module-4

- 7 a. Draw the complete root locus plot for the system $G(s)H(s) = \frac{K}{s(s+2)(s+4)}$. Find the range of K, so that damping ratio of the closed loop system is 0.5. (10 Marks)
- b. Draw the complete root locus for the system with $G(s)H(s) = \frac{K}{s(s+6)(s^2+4s+13)}$. Comment on stability. (10 Marks)

OR

- 8 a. The open loop transfer function of an unity feedback is $G(s) = \frac{K}{s(s+a)}$. (i) Find the value of 'K' and 'a'. So that resonant peak = 1.04 and resonant frequency = 11.5 rad/sec (ii) for the value of 'K' and 'a' found in part (i). Calculate the settling time and Bandwidth of the system. (06 Marks)
- b. Draw the Bode plot for the system having, $G(s) = \frac{10}{s(1+0.1s)(1+0.5s)}$, $H(s) = 1$
- Determine the (i) Gain cross over frequency (ii) Phase crossover frequency (iii) Gain margin (iv) Phase margin. (08 Marks)

- c. Find the open loop transfer function of a system whose approximate plot is as shown in Fig. Q8 (c).

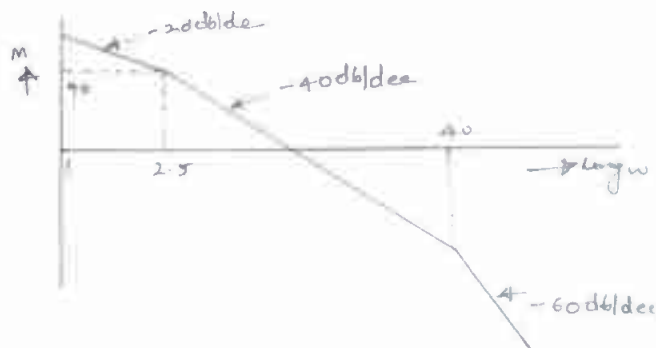


Fig. Q8 (c)

(06 Marks)

Module-5

- 9 a. The open loop transfer function of a control system is $G(s)H(s) = \frac{1}{s(s+2)(s+10)}$. Sketch the Nyquist plot and calculate the value of K. (10 Marks)
- b. What is controller? Explain the effect of P, I, PI and PID controller of a second order system. (10 Marks)

OR

- 10 a. Explain the step by step procedure of Lag compensating network. (10 Marks)
- b. Design a Lead Compensator for a unity feedback system with an open loop transfer function $G(s) = \frac{K}{s(s+1)}$ for the specification of velocity error constant $K_v = 12 \text{sec}^{-1}$ and phase margin as 40° . (10 Marks)

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Scheme & Solutions

Signature of Scrutinizer

Subject Title : CONTROL SYSTEM

Subject Code : 18EEG1

Question Number	Solution	Marks Allocated
1(a)	<p>OLCS <u>Module-1</u> CLCS</p> <p>(i) output Independent of control action (i) output somewhat depends on control action</p> <p>(ii) more stable 1x6=6 (ii) less stable</p> <p>(iii) feedback absent (iii) feedback present</p> <p>(iv) Simple in construction (iv) complicated in construction</p> <p>(v) operated in time basis (v) operated in accuracy basis</p> <p>(vi) Field control, Traffic signal (vi) Armature control, Heavily being</p>	06
(b)	<p> $T = J_1 \frac{d^2\theta_1}{dt^2} + B_1 \frac{d\theta_1}{dt} + B_{12} \frac{d(\theta_1 - \theta_2)}{dt} + K_{12}(\theta_1 - \theta_2)$ $J_2 \frac{d^2\theta_2}{dt^2} + B_2 \frac{d\theta_2}{dt} + B_{23} \frac{d(\theta_2 - \theta_3)}{dt} + B_{12} \frac{d(\theta_2 - \theta_1)}{dt} + K_{12}(\theta_2 - \theta_1) = 0$ $J_3 \frac{d^2\theta_3}{dt^2} + B_3 \frac{d\theta_3}{dt} + K_3 \theta_3 + B_{23} \frac{d(\theta_3 - \theta_2)}{dt}$ </p> <p> $L_1 \frac{di_1}{dt} + R_1 i_1 + R_{12} (i_1 - i_2) + \frac{1}{C_{12}} \int (i_1 - i_2) dt$ $L_2 \frac{di_2}{dt} + R_2 i_2 + R_{23} (i_2 - i_3) + R_{12} (i_2 - i_1) + \frac{1}{C_{12}} \int (i_2 - i_1) dt = 0$ $L_3 \frac{di_3}{dt} + R_3 i_3 + \frac{1}{C_3} \int i_3 dt + R_{23} (i_3 - i_2) = 0$ </p>	08
(c)	<p> $R_1 i_1 + \frac{1}{C_1} \int (i_1 - i_2) dt = V_1$ $R_2 i_2 + \frac{1}{C_2} \int i_2 dt + \frac{1}{C_1} \int (i_2 - i_1) dt = 0$ </p> <p> $\begin{bmatrix} (R_1 + \frac{1}{C_1 s}) & -\frac{1}{C_1 s} \\ -\frac{1}{C_1 s} & (R_2 + \frac{1}{C_1 s} + \frac{1}{C_2 s}) \end{bmatrix} \begin{bmatrix} I_1(s) \\ I_2(s) \end{bmatrix} = \begin{bmatrix} V_1(s) \\ 0 \end{bmatrix}$ </p> <p> $I_2(s) = \frac{\Delta F(s)}{\Delta} = \frac{V_1(s)}{C_1 s}$ </p> <p> $\frac{V_0(s)}{V_1(s)} = \frac{1}{s^2 R_1 R_2 C_1 C_2 + [R_1 C_1 + R_2 C_2 + R_1 C_2] s + 1}$ </p>	06

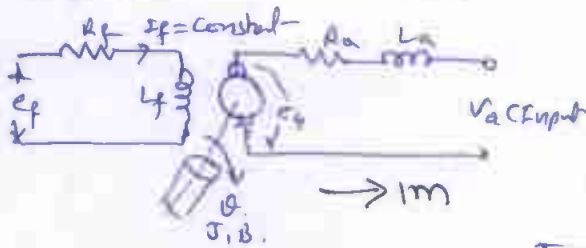
Question Number

Solution

Marks Allocated

2(a)

Definition — IM.

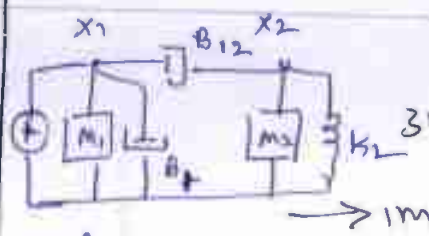


$$\begin{aligned} T_m &\propto I_a \\ T_m &= k_T I_a \\ e_b &= k_b \frac{d\theta}{dt} \\ L_a \frac{di_a}{dt} + R_a i_a + e_b &= V_{dc} \\ T_m &= J \frac{d^2\theta}{dt^2} + B \frac{d\theta}{dt} = k_T I_a \end{aligned}$$

$$\frac{\theta(s)}{V_{dc}(s)} = \frac{k_T}{s [R_a + sL_a] (Js + B) + k_T k_b} \rightarrow 2m$$

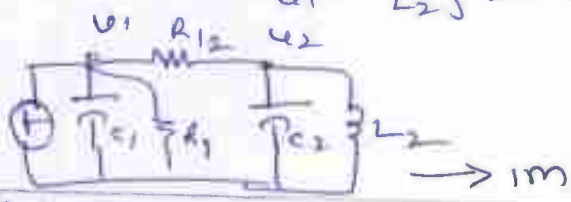
(06)

(b)



$$\begin{aligned} f(t) &= M_{12} \frac{dx_1}{dt} + B_1 \frac{dx_1}{dt} + B_{12} \frac{d(x_1+x_2)}{dt} \\ M_2 \frac{d^2x_2}{dt^2} + K_2 x_2 + B_{12} \frac{d}{dt}(x_2-x_1) &= 0 \end{aligned}$$

$$\begin{aligned} \hat{x}(t) &= c_1 \frac{dw_1}{dt} + \frac{w_1}{R_1} + \frac{w_1 - w_2}{R_{12}} \\ e_2 \frac{dw_2}{dt} + \frac{1}{L_2} \int w_2 dt + \frac{w_2 - w_1}{R_{12}} &= 0 \end{aligned}$$



(08)

(c)

Side-1
 $T = J_1 \frac{d^2\theta_1}{dt^2} + B_1 \frac{d\theta_1}{dt} + T_L(t) \rightarrow 1m$

Side-2
 $T_2 = J_2 \frac{d^2\theta_2}{dt^2} + B_2 \frac{d\theta_2}{dt} + T_L$
 $\frac{T_1}{T_2} = \frac{\theta_2}{\theta_1} = \frac{N_1}{N_2}$

$$\frac{\theta_2}{\theta_1} = \frac{N_1}{N_2} \Rightarrow \frac{N_2}{N_1} T_L = J_2 \frac{d^2\theta_2}{dt^2} + B_2 \frac{d\theta_2}{dt} + T_L$$

$$\therefore T_1 = \frac{N_1}{N_2} J_2 \frac{d^2\theta_2}{dt^2} + \frac{N_1}{N_2} B_2 \frac{d\theta_2}{dt} + \frac{N_1}{N_2} T_L \rightarrow 1m$$

$$\therefore T = J_1 \frac{d^2\theta_1}{dt^2} + B_1 \frac{d\theta_1}{dt} + \frac{N_1}{N_2} J_2 \frac{d^2\theta_2}{dt^2} + \frac{N_1}{N_2} B_2 \frac{d\theta_2}{dt} + \frac{N_1}{N_2} T_L$$

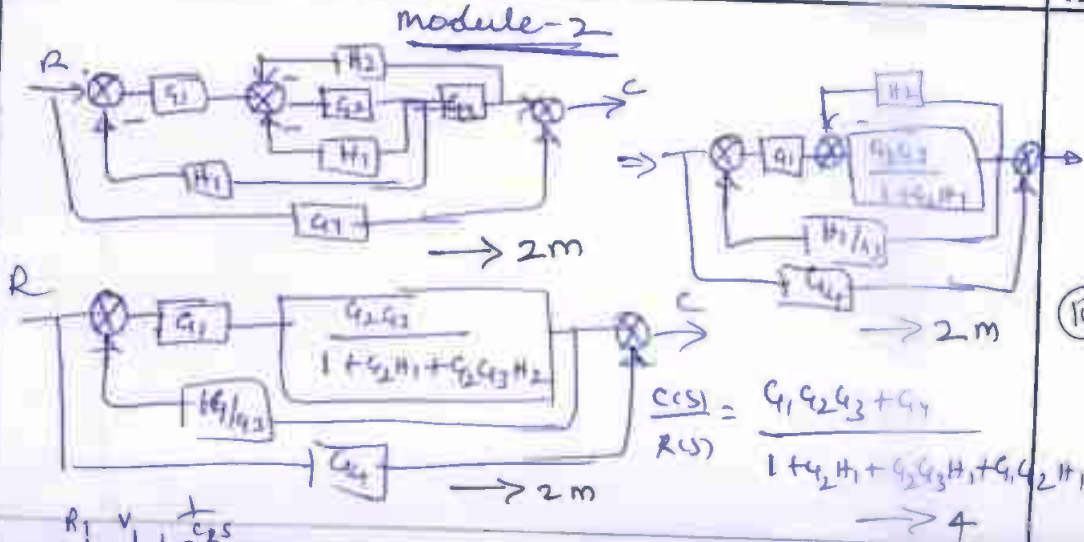
$$\theta_2 = \frac{N_1}{N_2} \theta_1 \rightarrow 1m$$

$$\therefore T = \left[J_1 + \left(\frac{N_1}{N_2} \right)^2 J_2 \right] \frac{d^2\theta_1}{dt^2} + \left[B_1 + \left(\frac{N_1}{N_2} \right)^2 B_2 \right] \frac{d\theta_1}{dt} + \frac{N_1}{N_2} T_L \rightarrow 1m$$

(06)

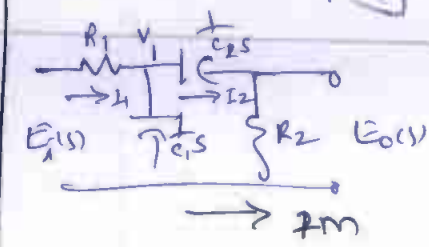
Question Number	Solution	Marks Allocated
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3 (a)



(10)

(b)

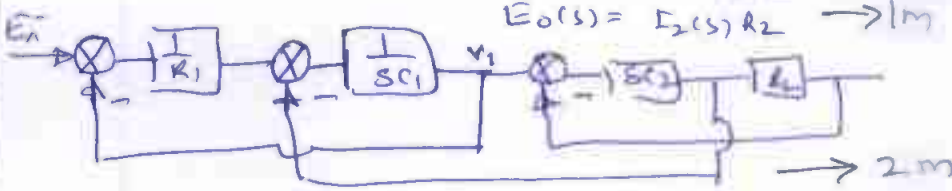


$$I_1(s) = \frac{E_1(s) - V_1(s)}{R_1} \rightarrow 1m$$

$$V_1(s) = I_1(s) - I_2(s) \times \frac{1}{C_1 s} \rightarrow 1m$$

$$I_2(s) = \frac{V_1(s) - E_2(s)}{1/s C_2} = \frac{(V_1 - E_2) C_2 s}{1/s C_2} \rightarrow 1m$$

$$E_2(s) = I_2(s) R_2 \rightarrow 1m$$



$$\frac{E_2(s)}{E_1(s)} = \frac{s C_2 R_2}{s^2 R_1 R_2 C_1 C_2 + s [R_1 C_1 + R_2 C_2 + R_1 C_2] + 1} \rightarrow 2m$$

$$\frac{E_2(s)}{E_1(s)} = \frac{s}{s^2 + 2.1s + 1} \rightarrow 1m$$

(10)

4 (a)

$P_1 = G_1 G_2 G_3 G_4$	$L_1 = -G_1 H_1$	$L_{11} = L_1 L_3 = G_1 G_3 H_1 H_2$
$P_2 = G_1 G_5$	$L_2 = -H_5$	$L_{12} = L_1 L_5 = G_1 H_1 H_4$
$P_3 = G_1 G_4 G_6$	$L_3 = -G_3 H_2$	$L_{13} = L_2 L_5 = G_3 H_2 H_5$
	$L_4 = -H_4$	$L_{14} = L_5 L_6$
	$L_5 = -G_1 G_2 G_3 H_3$	$L_{15} = L_3 L_5$
	$L_6 = -G_1 G_4 H_3$	$L_{16} =$

→ 1m

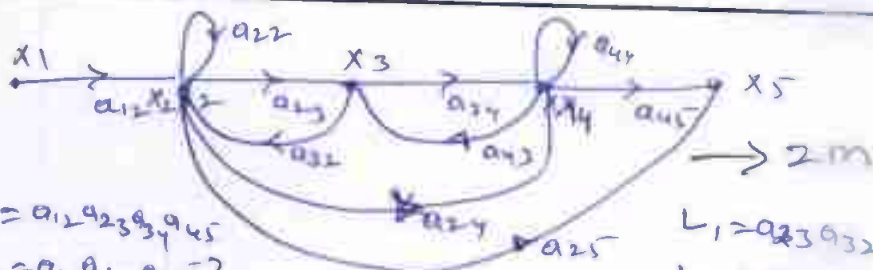
$$\Delta = 1 - [L_1 + L_2 + L_3 + L_4 + L_5 + L_6] + [L_{11} + L_{12} + L_{13} + L_{14} + L_{15} + L_{16}] \rightarrow 2m$$

$$T = \frac{\sum P_k \Delta_k}{\Delta} = \frac{P_1 \Delta_1 + P_2 \Delta_2 + P_3 \Delta_3 + P_4 \Delta_4}{\Delta}$$

$\Delta_1 = 1$
 $\Delta_2 = 1 + G_2 H_2$
 $\Delta_3 = 1$

$$T = \frac{G_1 G_2 G_3 G_4 + G_1 G_5 (1 + G_2 H_2) + G_1 G_4 G_6}{\Delta} \rightarrow 2m$$

(10)

Question Number	Solution	Marks Allocated
4 (5)	 <p> $P_1 = a_{12}a_{23}a_{34}a_{45}$ $P_2 = a_{12}a_{24}a_{45}$ $P_3 = a_{12}a_{25}$ </p> <p> $L_{11} = L_1 L_4$ $L_{12} = L_3 L_4$ $L_{13} = L_2 L_3$ </p> <p> $\Delta_1 = 1$ $\Delta_2 = 1$ $\Delta_3 = 1 - (L_2 + L_3)$ </p> <p> $\Delta = 1 - [L_1 + L_2 + L_3 + L_4 + L_5] + [L_{11} + L_{12} + L_{13}]$ </p> <p> $\frac{X_5}{X_1} = \frac{\sum P_k \Delta_k}{\Delta} = \frac{P_1 \Delta_1 + P_2 \Delta_2 + P_3 \Delta_3}{\Delta}$ </p> <p> $= \frac{a_{12}a_{23}a_{34}a_{45} + a_{12}a_{24}a_{45} + a_{12}a_{25} [1 - a_{24} + a_{23} + a_{24}]}{1 - [L_1 + L_2 + L_3 + L_4 + L_5] + [L_{11} + L_{12} + L_{13}]}$ </p> <p> $L_1 = a_{23}a_{32}$ $L_2 = a_{34}a_{43}$ $L_3 = a_{22}$ $L_4 = a_{44}$ $L_5 = a_{24}a_{43}a_{32}$ </p>	10
5 (a)	<p>Definition: Delay time, rise time, peak time, peak overshoot, settling time</p> <p>MODULE-3</p> <p>1 x 5 = 5 m</p> <p>(b) $\frac{C(s)}{R(s)} = \frac{K}{s^2 + 10s + 16} = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$</p> <p>$\omega_n = \sqrt{K}$, $2\zeta\omega_n = 10$</p> <p>$K = \omega_n^2 = 100$, $\omega_n = 10$</p> <p>$t_s = \frac{4}{\zeta\omega_n} = 0.8 \text{ sec}$</p> <p>$\%M_p = e^{-\frac{\zeta\omega_n}{\sqrt{1-\zeta^2}}} \times 100 = 0.163\%$</p> <p>$t_p = \frac{\pi}{\omega_n \sqrt{1-\zeta^2}} = 0.363 \text{ sec}$</p>	05
5 (c)	<p>$\frac{C(s)}{R(s)} = \frac{K}{s^2 + \frac{1}{T}s + \frac{K}{T}} = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \rightarrow 2 \text{ m}$</p> <p>$\omega_n = \sqrt{\frac{K}{T}}$, $\zeta = \frac{1}{2\sqrt{KT}} \rightarrow 1 \text{ m}$</p> <p>$M_p = 0.75$, $\zeta = \zeta_1$, $K > K_1$</p> <p>$M_p = 0.25$, $\zeta = \zeta_2$, $K > K_2$</p> <p>$0.75 = e^{-\frac{\zeta_1 \omega_{n1}}{\sqrt{1-\zeta_1^2}}}$, $0.25 = e^{-\frac{\zeta_2 \omega_{n2}}{\sqrt{1-\zeta_2^2}}}$</p> <p>$\zeta_1 = 0.09116 \rightarrow 1 \text{ m}$, $\zeta_2 = 0.40371 \rightarrow 1 \text{ m}$</p> <p>$\frac{\zeta_1}{\zeta_2} = \sqrt{\frac{K_2}{K_1}}$, $\therefore \frac{K_2}{K_1} = 0.05098$</p> <p>$K_2 = 0.05098 K_1 \rightarrow 0.2 \text{ m}$</p>	07

Question Number	Solution	Marks Allocated
<p>6(a)</p>	<p> $G(s) = \frac{15}{s^2(s+20)(s+30)}$ order of system = 4 \rightarrow 1M Type no: 2 \rightarrow 1M $\tau(t) = 1 + 10t + 60\frac{t^2}{2}$ $e_{ss} = \frac{A}{1+K_p} + \frac{B}{K_u} + \frac{C}{K_a}$ $B = \frac{1}{1+60} + \frac{10}{60} + \frac{60}{K/600}$ $K = 450$ </p> <p> $K_p = \lim_{s \rightarrow 0} G(s)(s+1) = 60$ $K_u = \lim_{s \rightarrow 0} sG(s)(s+1) = 60$ $K_a = \lim_{s \rightarrow 0} s^2 G(s)(s+1) = \frac{K}{600}$ </p>	<p>05</p>
<p>6(b)</p>	<p> s^6 1 5 8 4 s^5 3 9 6 s^4 2 6 4 s^3 0 0 4 s^2 \rightarrow 2M s^1 Difficulty no: 2 s^0 </p> <p> $A(s) = 2s^4 + 6s^2 + 4$ $\frac{dA(s)}{ds} = 8s^3 + 12s$ </p> <p> s^6 1 5 8 4 s^5 3 9 6 s^4 2 6 4 s^3 8 12 s^2 3 4 s^1 1 3 s^0 4 </p> <p> $A(s) = s^4 + 3s^2 + 2 = (s^2+2)(s^2+1)$ $LHS = 2$ $RHS = 0$ $\text{Im}g = 4$ $s = \pm j\sqrt{2}, s = \pm j$ </p>	<p>07</p>
<p>6(c)</p>	<p> $1 + G(s)H(s) = 0$ $1 + \frac{K(s+13)}{s(s+3)(s+7)} = 0$ $s^3 + 10s^2 + (21+K)s + 13K = 0$ s^3 1 21+K s^2 10 13 s^1 $\frac{210-3K}{10}$ - s^0 13K </p> <p> $13K > 0 \Rightarrow K > 0$ $\frac{210-3K}{10} > 0 \Rightarrow K < 70$ </p> <p> range of K: $0 < K < 70$ </p> <p> $10s^2 + 13K = 0$ $s = \pm j 9.53$ Sustained frequency of oscillation $\omega = 9.53 \text{ rad/sec}$ </p>	<p>08</p>

Question Number	Solution	Marks Allocated
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7(a)

Module-4
 $G(s)H(s) = \frac{k}{s(s+2)(s+4)}$

step 1:- There are 3 poles $s=0, -2, -4, n=3$
 There is no zero $m=0$. $\rightarrow 1M$

no of root loci $= n-m = 3$
 no of Asymptotes $= n-m = 3$

$\theta_q = \frac{(2q+1)180}{n-m} = 60^\circ, 180^\circ, 300^\circ$
 $\sigma_a = \frac{\sum p - \sum z}{n-m} = \frac{-2-4}{3} = -2$ } 2M $\xi = 0.5$

value of $k = \frac{L_p L_p L_p}{\text{Length zero}}$

step 2 Breakaway point-

$\frac{dk}{ds} = 0 \quad 1 + G(s)H(s) = 0$
 $1 + \frac{k}{s(s+2)(s+4)} = 0$
 $k = -[s^3 + 6s^2 + 8s]$ } 2M
 $\frac{dk}{ds} = -[3s^2 + 12s + 8] = 0$

$= \frac{1 \cdot 3 \times 1 \cdot 8 \times 3}{3}$
 $= 8.19$
 $\rightarrow 1M$

$s = -3.15, -0.85$
 Breakaway point $= s = -0.85$

step 3:- no need angles of departure & arrival.

step 4 crossing point on imaginary axis

s^3	1	8	$k > 0$	$6s^2 + k = 0$	} 2M
s^2	6	k	$\frac{48-k}{6} > 0$	$s^2 = -8$	
s^1	$\frac{48-k}{6}$	0	$k < 48$	$s = \pm j2.8$	
s^0	k				

step 5

There are 4 poles $s=0, s=-6, s=-2 \pm j3, n=4$
 There is no zero $m=0$ } 1M
 no of root loci $= n-m = 4$

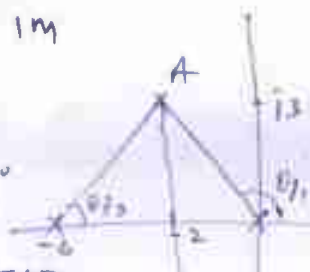
no of Asymptotes $= n-m = 4$
 $q = 0, 1, 2, 3$
 $\theta_q = \frac{(2q+1)180}{n-m} = 45^\circ, 135^\circ, 225^\circ, 315^\circ$ } 2M

step 2 $\sigma_a = \frac{\sum p - \sum z}{n-m} = -2.5$

step 3 $\frac{dk}{ds} = 0 \quad 1 + G(s)H(s) = 0$
 $k = [s^4 + 10s^3 + 37s^2 + 78s]$
 $\frac{dk}{ds} = 4s^3 + 30s^2 + 74s + 78 = 0$
 $s = -4.201, -1.64 \pm 1.386j$
 Breakaway point $= -4.201$

step 4

$\theta_{p1} = 180 - \tan^{-1} \frac{3}{2} = 122^\circ$
 $\theta_{p2} = 90^\circ$
 $\theta_{p3} = \tan^{-1} \frac{3}{4} = 38^\circ$ } 0.2
 $\phi_d > 180 - (122 + 90 + 38)$
 $= -70^\circ$
 ϕ_d at A*
 $\phi_d = 70^\circ$



7(b)

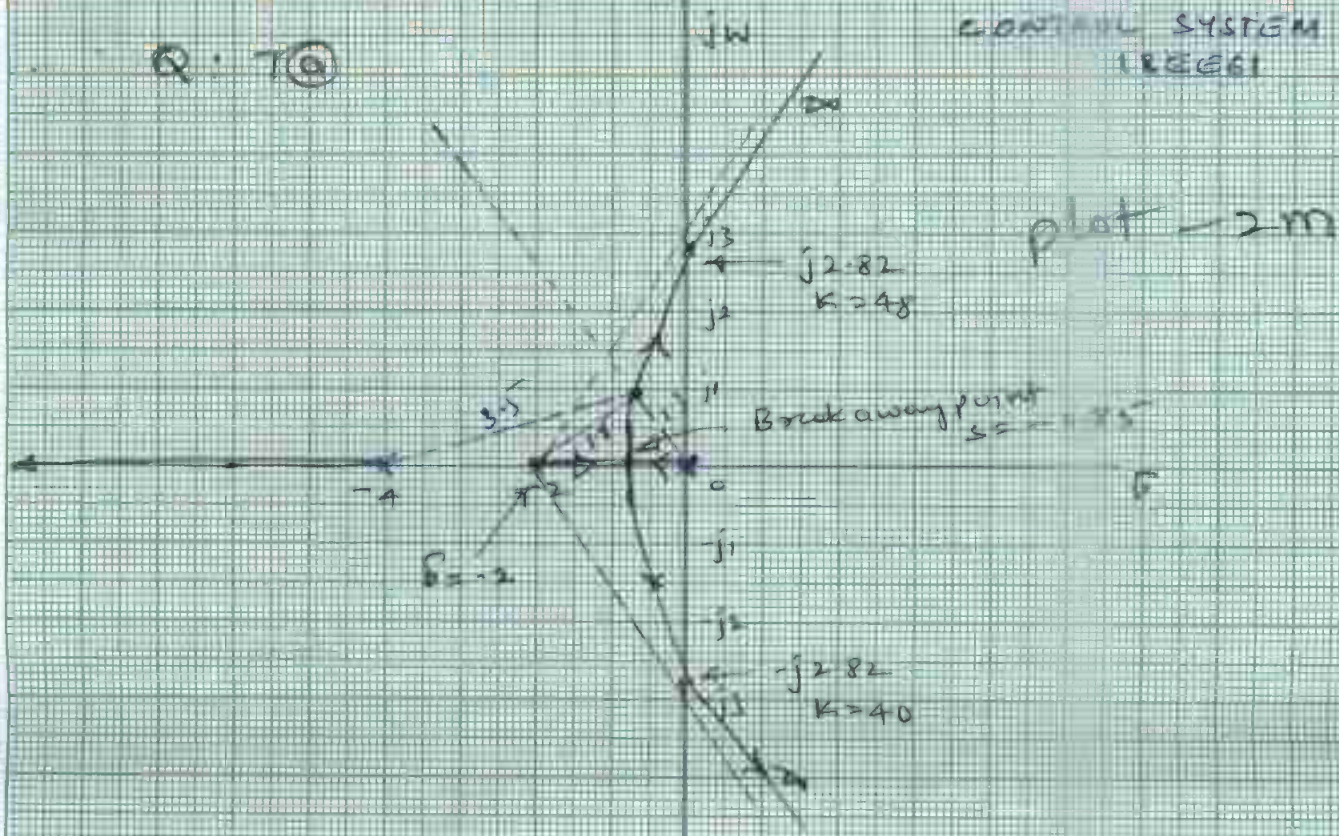
step 5 crossing point on imaginary axis

s^4	1	37	k	$k > 0$	$29.25^2 + k = 0$
s^3	10	78		$\frac{2277.6 - k}{29.2} > 0$	$s = \pm j2.8$
s^2	29.2	k		$k < 2277.6$	$\omega = 2.8 \text{ rad/sec}$
s^1	$\frac{2277.6 - k}{29.2}$				
s^0	k				

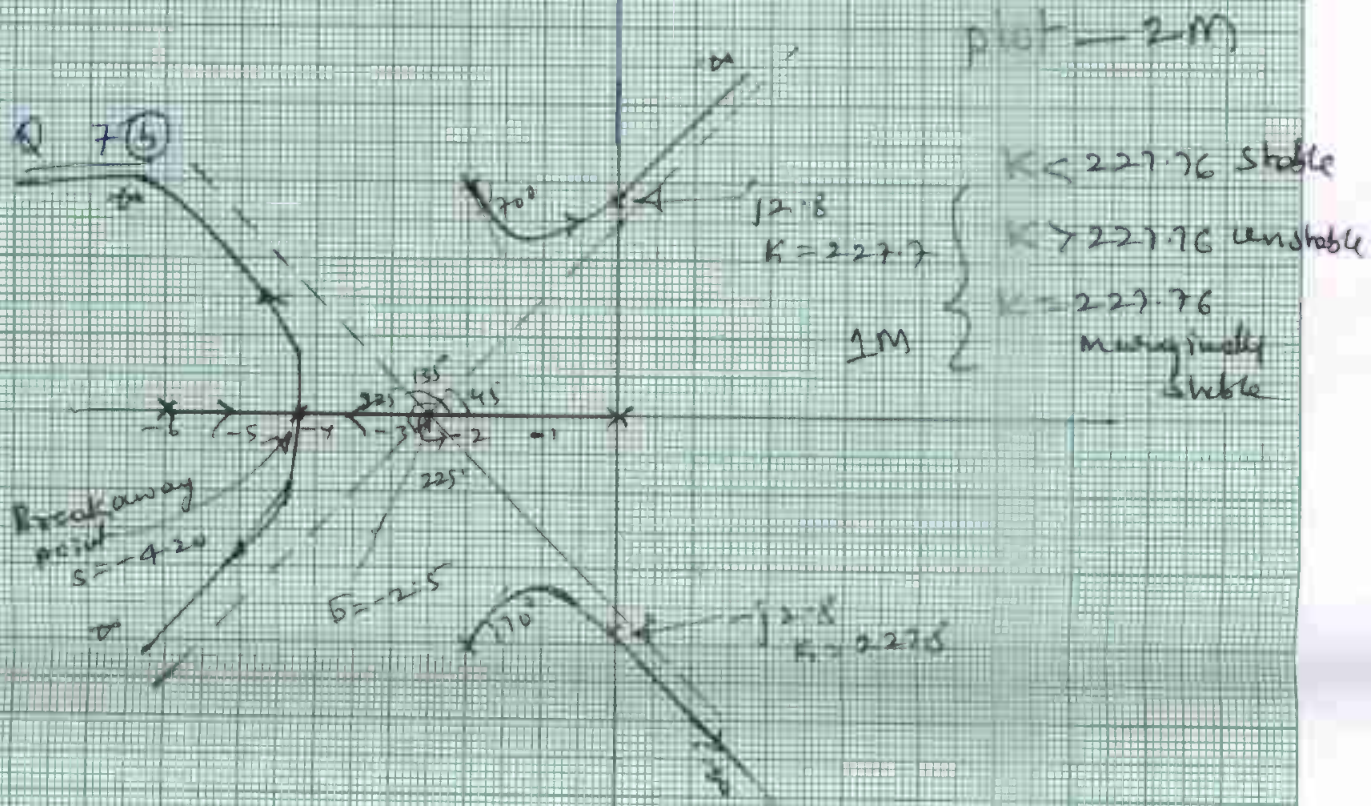
10

Q. 7 (a)

CONTROL SYSTEM (REGG)



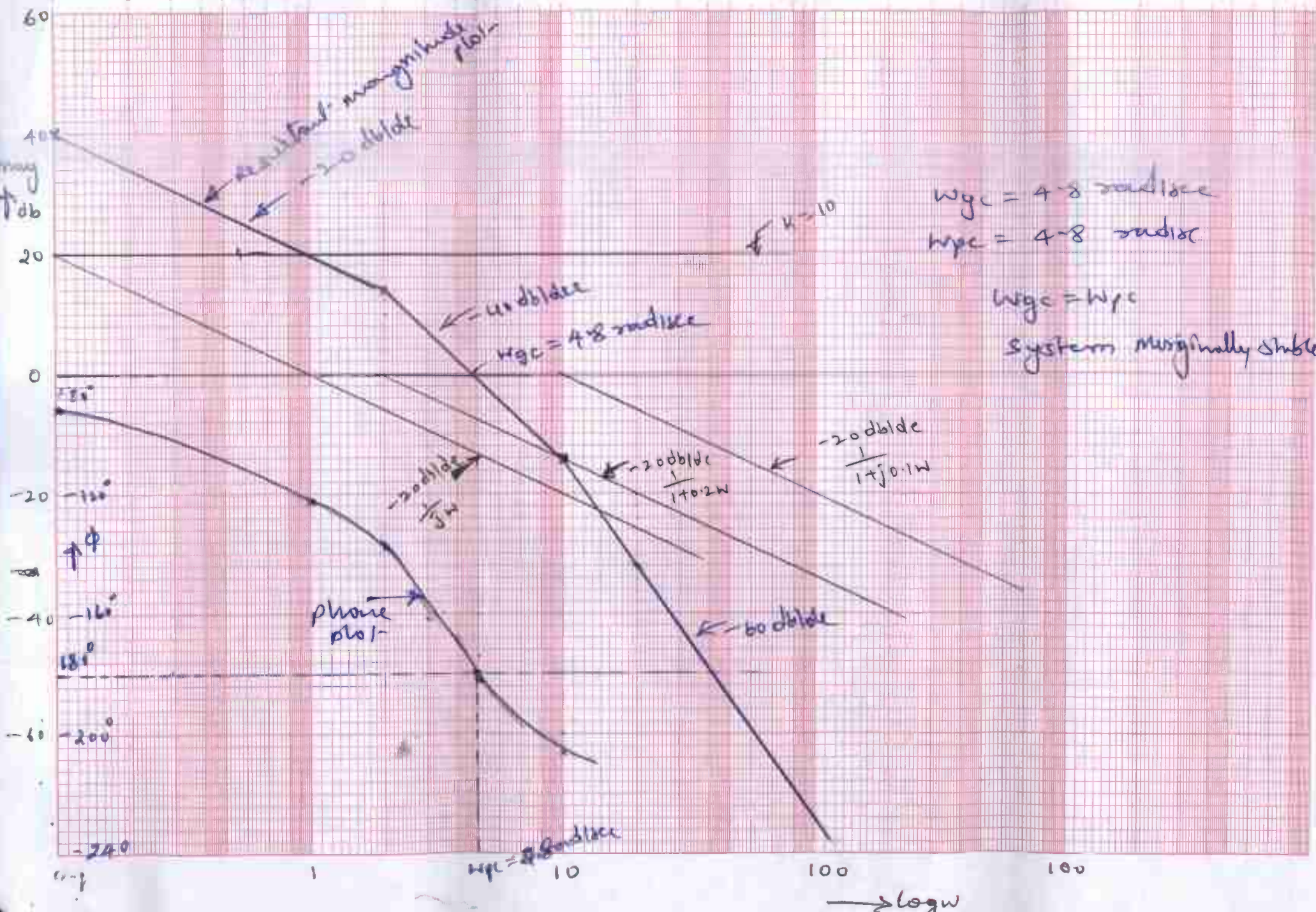
Q. 7 (b)



$K < 227.76$ Stable
 $K > 227.76$ unstable
 $K = 227.76$ marginally stable

Q 8(b)

$$G(s) = \frac{10}{s(s+0.1s)(1+0.5s)}$$



$\omega_{gc} = 4.8 \text{ rad/sec}$
 $\omega_{pc} = 4.8 \text{ rad/sec}$

$\omega_{gc} = \omega_{pc}$
 System marginally stable.

Question Number

Solution

Marks Allocated

8(a)

$$\frac{C(s)}{R(s)} = \frac{K}{s^2 + as + K} = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \rightarrow 1M$$

$$\left. \begin{aligned} \omega_n &= \sqrt{K} \\ \zeta &= \frac{a}{2\sqrt{K}} \end{aligned} \right\} 1M$$

$$m_r = \frac{1}{2\zeta\sqrt{1-\zeta^2}} = 1.04$$

$$\zeta = 0.6021$$

$$\omega_r = \omega_n \sqrt{1-2\zeta^2} = 11.45$$

$$\omega_n = 21.027$$

→ 1M

$$\therefore K = \omega_n^2 = 485.1 \rightarrow 1M$$

$$a = \zeta 2\sqrt{K} = 26.52$$

$$BW = \omega_n \sqrt{1-2\zeta^2 + \sqrt{2-4\zeta^2 + 4\zeta^4}} = 25.23 \text{ rad/sec} \rightarrow 1M$$

$$T_s = \frac{4}{\zeta\omega_n} = 0.3016 \text{ sec} \rightarrow 1M$$

06

(b)

$$G(j\omega) = \frac{10 \angle 0}{\omega \angle 90 \times \sqrt{1^2 + (0.1\omega)^2} \angle \tan^{-1} 0.1\omega \times \sqrt{2^2 + (0.5\omega)^2} \angle \tan^{-1} 0.5\omega}$$

$$\phi = -90 - \tan^{-1} 0.1\omega - \tan^{-1} 0.5\omega \rightarrow 2M$$

corner frequency $\omega_{c1} = \frac{1}{0.5} = 2 \text{ rad/sec}$ $\omega_{c2} = \frac{1}{0.1} = 10 \text{ rad/sec}$

term	C/F	slope	change in slope
$K=10$	-		
$\frac{1}{j\omega}$	-	-20db/dec	-20db/dec
$\frac{1}{1+j0.5\omega}$	2	-20	-40
$\frac{1}{1+j0.1\omega}$	10	-2	-60

→ 2M

ω	ϕ
0	-90
0.1	-93.43
1	-122.3
2	-146.31
5	-184.76
10	-213
15	-238

→ 2M

02

$$\left. \begin{aligned} \omega_{gc} &= 4.8 \text{ rad/sec} \\ \omega_{pc} &= 4.8 \text{ rad/sec} \\ G_m &= 0 \text{ db} \\ P_m &= 180 + \phi_{gc} = 180 - 180 = 0^\circ \end{aligned} \right\}$$

plot → 03 M

$\omega_{gc} \approx \omega_{pc} \therefore$ System marginally stable

08

(c)

$$\omega = 2.5 \text{ rad/sec}$$

mag at $\omega_{c2} = A$ at $\omega_{c1} +$ change in slope from ω_{c1} to ω_{c2} $\log \frac{\omega_{c2}}{\omega_{c1}}$

$$40 = A \text{ at } \omega_{c1} + (-20 \times \log \frac{2.5}{1})$$

$$A = 47.95 \text{ db}$$

$$20 \log K = 47.95$$

$$K = 10$$

$$K = 250$$

→ 2M

first line have slope -20db/dec due to $\frac{1}{s} \rightarrow 1M$

$\omega = 2.5 \text{ rad/sec}$ slope change from -20 to -40 db due

1st order factor in denominator $= \frac{1}{1+s/2.5} \rightarrow 1M$

$\omega = 40$ slope changes from -40 to -60

due to $\frac{1}{1+s/40} \rightarrow 1M$

$$G(s) = \frac{250}{s(s + \frac{s}{2.5})(s + \frac{s}{40})} = \frac{250}{s(1+0.4s)(1+0.025s)}$$

06

Q NO

Solution
module-5

Marks

9(a)

$$G(s) = \frac{K}{s(s+2)(s+10)}$$

Step 1: $p=0$

Step 2: $N = -P \Rightarrow 0$

Step 3:



Step 4: put $s=j\omega$

$$G(j\omega) = \frac{K}{j\omega(j\omega+2)(j\omega+10)}$$

$$M = \frac{K}{\omega \sqrt{4+\omega^2} \sqrt{100+\omega^2}}$$

$$\phi = -90 - \tan^{-1} \frac{\omega}{2} - \tan^{-1} \frac{\omega}{10}$$

$$S = j\omega \quad K \quad S = -j\omega$$

$$\omega \rightarrow \infty \quad K \quad \omega \rightarrow 0$$

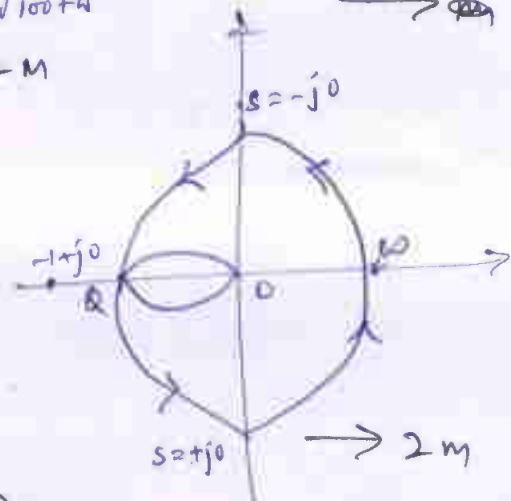
Section-I

$\omega \rightarrow \infty$	$\angle = 270^\circ$	$-90 - (-270)$
$\omega = 0$	$\angle = 90^\circ$	$= 180^\circ$

Section-II

$\omega = +10$	$\angle = 90^\circ$	$90 - (-90)$
$\omega = -0$	$\angle = 90^\circ$	$= 180^\circ$

Section-III mirror image of section about real axis



Step 5: $G(j\omega) = \frac{K(-j\omega)(10-j\omega)(2-j\omega)}{(j\omega)(-j\omega)(10+j\omega)(10-j\omega)(2+j\omega)(2-j\omega)}$

$$= \frac{-12K\omega^2}{D} - \frac{Kj\omega(20-\omega^2)}{D}$$

$$D = \omega^2(4+\omega^2)(100+\omega^2)$$

Equation in ω : $\omega(20-\omega^2) = 0$

Subreal part $\omega_{pc} = \sqrt{20}$

$$\omega = \frac{-12 \times K \times 20}{20 \times 20 + \omega^2 (100 + 20)} = -\frac{K}{240}$$

$$0 < K < 1$$

$$1 < K < 240$$

$$0 < K < 240$$

(b)

Controller — 2 m

P-controller — 2

I-controller — 2

PI-controller — 2

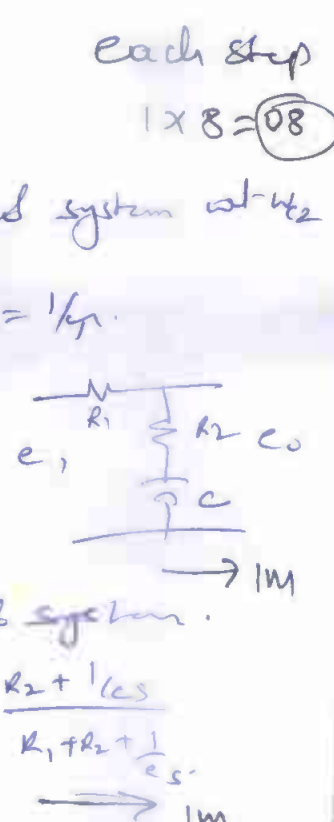
PID-controller — 2

10

10

Q. No	solution	marks
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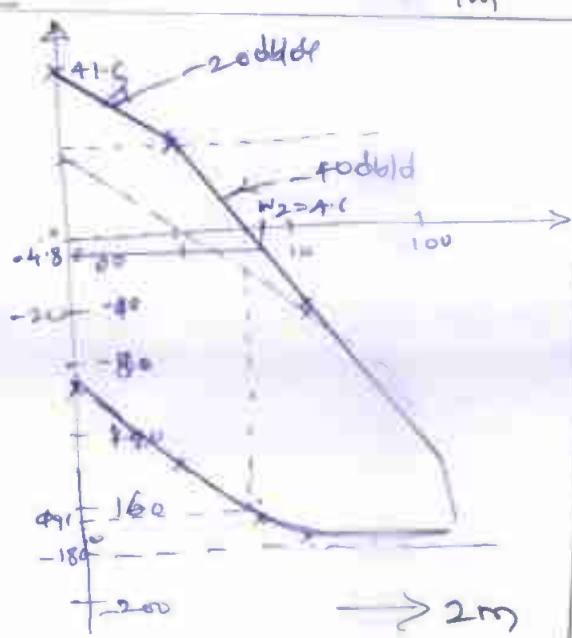
- 10a) Procedure for lag compensation
- Step 1 Determine the value of K to satisfy the specified error
 - For this value of K Draw Bodeplot, Find PM
 - If $\phi_s = \text{specified PM}$
 $e = \text{margin suffy } 5 \text{ to } 15^\circ$
 $\phi_2 = \phi_s + e$
 - Find frequency ω_{c2}
 - measure gain of an compensated system at ω_{c2}
 $\omega_{c2} = 20 \log B$
 - choose upper corner frequency $\omega_2 = 1/\beta$
 - Thus β & ω_2 are defined
 $G_c(s) = \frac{1}{\beta} \left[\frac{s + \frac{1}{\beta}}{s + \frac{1}{\beta\beta}} \right]$
 - Draw the Bode plot of the compensated system.



$$G_c(s) = \frac{(s+z_c)}{s+p_c} = \frac{s+1/\beta}{s+1/\beta\beta}, \quad \frac{e_0}{e_1} = \frac{R_2 + 1/s}{R_1 + R_2 + 1/s}$$

b) $G(s) = \frac{K}{s(s+1)}$
 $K=12$
 $G(s) = \frac{12}{s(s+1)}$
 $G(j\omega) = \frac{12}{j\omega(j\omega+1)} = \frac{12 \angle 0}{\omega \sqrt{1^2 + \omega^2} \angle \tan^{-1} \omega}$
 $\phi = -90 - \tan^{-1} \omega \rightarrow 2M$
magnitude
 $\omega=0.1 \quad A = 20 \log \frac{12}{0.1} = 41.5$
 $\omega=1 \quad A = 20 \log 12 = 21.5$
 $\omega=10 \quad A = A_{at \omega_c} + \text{slope from } \omega_c \text{ to } \omega \text{ with } \log \frac{\omega}{\omega_c}$
 $\quad \quad \quad = +20 \cdot 0.5 + (-20) \log \frac{10}{1}$
 $\quad \quad \quad = 1.5 \rightarrow 2M$

ω	ϕ
0.1	-95
1	-135
2	-153.4
5	-168.6
10	-174
500	179.80



$PM = 180 + \phi_{gc}$
 $= 180 - 165 = 15^\circ$
 $PM \text{ specified} = 4^\circ$
 $\text{phase lead} = 40 - 15 + 5 = 3^\circ$
 $\alpha = \frac{1 - \sin \theta}{1 + \sin \theta} = 0.33$
 $\rightarrow 0.2 m$

Gain = $-10 \log$

From plot 4.6 read.

$$W_{c2} = W_M = 4.6$$

$$\begin{aligned} \text{Corner freq.} &= \frac{1}{\tau_1} = W_M \sqrt{\alpha} \\ &= 4.6 \sqrt{0.33} \\ &= 2.64 \end{aligned}$$

$$W_2 = \frac{1}{\alpha \tau_1} = \frac{W_M}{\sqrt{\alpha}} = \frac{4.6}{0.33} = 8.20 \text{ rad/sec}$$

$$G_c = \frac{s + \frac{1}{\tau_1}}{s + \frac{1}{\alpha \tau_1}} = \frac{s + 2.64}{s + 8} \quad \left. \vphantom{\frac{s + \frac{1}{\tau_1}}{s + \frac{1}{\alpha \tau_1}}} \right\} 0.2$$

$$G_c(s) = \frac{0.33(1 + 0.378s)}{1 + 0.125s}$$

(10)