

Fourth Semester B.E. Degree Examination, Jan./Feb. 2023

Control Systems

Time: 3 hrs.

Note: Answer any **FIVE** full questions, choosing **ONE** full question from each module.

Max. Marks: 100



Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
 2. Any revealing of identification, appeal to evaluator and /or equations written eg, $42+8 = 50$, will be treated as malpractice.

Module-1

1. a. Define Control System. Distinguish between open loop and closed loop control systems. (06 Marks)
- b. Write the differential equations of performance for the mechanical system shown in Fig.Q1(b). Draw its F – V analogous circuit.

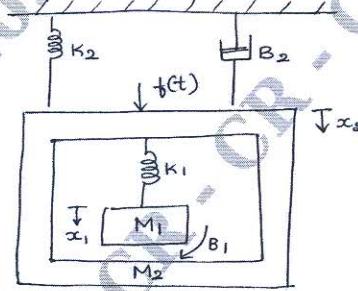


Fig.Q1(b)

(08 Marks)

- c. For the signal flow graph shown in Fig.Q1(c), determine the transfer function $\frac{C(s)}{R(s)}$ using Mason's gain formula.

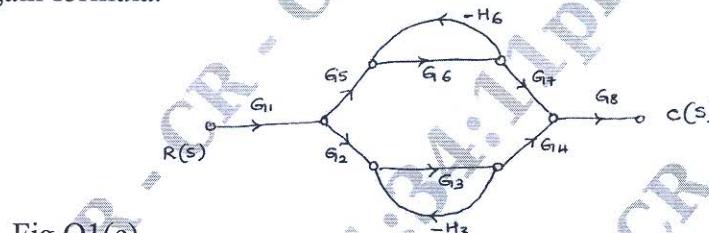


Fig.Q1(c)

(06 Marks)

OR

2. a. Illustrate how to perform the following in connection with block diagram reduction technique.
- Shifting – take – off point after a summing point
 - Shifting – take – off point before a summing point
 - Removing minor feedback loop.
- b. For the block diagram shown in Fig.Q2(b), determine the transfer function $C(s)/R(s)$ using block diagram reduction technique.

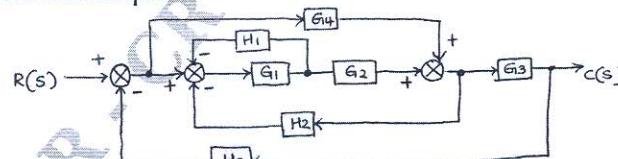


Fig.Q2(b)

(08 Marks)

- c. Obtain the transfer function $\frac{\theta_2(s)}{T(s)}$ for the system shown in Fig.Q2(c).

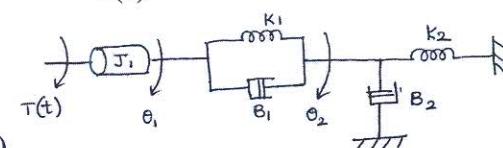


Fig.Q2(c)

(06 Marks)

Module-2

- 3 a. Define the following time response specifications for an underdamped second order system :
 i) Rise time (t_r)
 ii) Peak time (t_p)
 iii) Peak overshoot (M_p)
 iv) Settling time (t_s). (04 Marks)
- b. A system is given by differential equation :

$$\frac{d^2y(t)}{dt^2} + \frac{4dy(t)}{dt} + 8y(t) = 8x(t),$$

 where $y(t)$ is the output and $x(t)$ is the input. Determine all time domain specifications for unit step input assuming 2% criterion. (08 Marks)
- c. For a unity feedback system with $G(s) = \frac{s(s+1)}{s^2(s+3)(s+10)}$. Determine the type of the system, error co-efficient and steady state error for input $r(t) = 1 + 3t + \frac{t^2}{2}$. (08 Marks)

OR

- 4 a. Derive an expression for $c(t)$ of an underdamped second order system for a unit step input. (08 Marks)
- b. The unity negative feedback system with $G(s) = \frac{K(s+\alpha)}{(s+\beta)^2}$ is to be designed to meet the following specifications. Steady state error for a unit step input = 0.1, damping ratio = 0.5, natural frequency = $\sqrt{10}$ rad/sec. Find K , α and β . (08 Marks)
- c. Explain PID controller with the help of a block diagram. (04 Marks)

Module-3

- 5 a. State and explain Routh's stability criterion for determining the stability of the system. (04 Marks)
- b. Determine the number of roots that are :
 i) In the right half of s-plane
 ii) On the imaginary axis
 iii) In the left half of s-plane.
 For the system with the characteristic equation : $s^6 + 4s^5 + 3s^4 - 16s^2 - 64s - 48 = 0$. (08 Marks)
- c. The system shown in Fig.Q5(c) oscillates with a frequency of 2 rad/sec. Find the value of ' K_{mar} ' and ' P '. No poles are in RHS.

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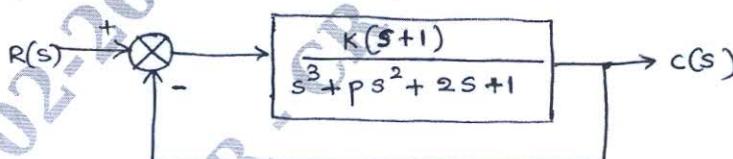


Fig.Q5(c)

(08 Marks)**OR**

- 6 a. Explain the following rules with respect to root locus technique :
 i) Angle of asymptotes
 ii) Point of intersection with imaginary axis
 iii) Angle of departure. (06 Marks)
- b. The open loop transfer function of a control system is given by

$$G(s)H(s) = \frac{K}{s(s+2)(s^2 + 6s + 25)}$$

Draw the complete root locus of the system.

(14 Marks)

Module-4

- 7 a. Find the gain margin and phase margin for the negative feedback control system with an open loop transfer function :

$$G(s)H(s) = \frac{200}{s(s^2 + 12s + 100)}.$$

(08 Marks)

- b. Construct the Bode plot for a unity feedback control system with

$$G(s)H(s) = \frac{10(s+10)}{s(s+2)(s+5)}$$

Find its gain margin and phase margin comment on the stability.

(12 Marks)

OR

- 8 a. Explain the procedure for investigating the stability using Nyquist criterion.
b. For the system with open loop transfer function :

$$G(s)H(s) = \frac{10}{s^2(1+0.25s)(1+0.5s)}$$

Sketch the Nyquist plot and determine whether the system is stable or not?

(14 Marks)

Module-5

- 9 a. Draw the block diagram of a typical system with digital controller and explain.
b. Obtain the state model of an electrical system shown in Fig.Q9(b).

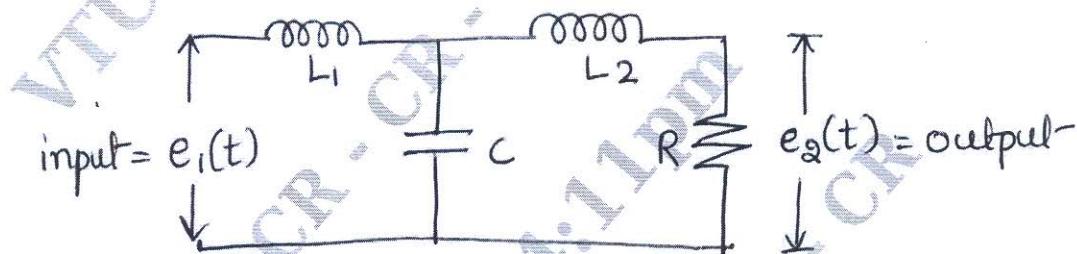


Fig.Q9(b)

(06 Marks)

- c. Find the transfer function of the system with a state model.

$$\begin{bmatrix} \dot{X}_1 \\ \dot{X}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} U \text{ and } y = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \end{bmatrix}$$

(08 Marks)

OR

- 10 a. State the properties of state transition matrix.
b. Obtain the state model for the system represented by the differential equation :

$$\frac{d^3y(t)}{dt^3} + \frac{9d^2y(t)}{dt^2} + \frac{26dy(t)}{dt} + 24y(t) = 6u(t)$$

(06 Marks)

- c. Find the state transition matrix for :

$$A = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}.$$

(08 Marks)
