

OR

- 6 a. Solve : $(xy^3 + y)dx + 2(x^2y^2 + x + y^4)dy = 0$. (06 Marks)
- b. Water at temperature 10°C takes 5 minutes to warm up to 20°C at a room temperature of 40°C . Find the temperature of the water after 20 minutes. (07 Marks)
- c. Find the general solution of the equation $(px - y)(py + x) = a^2p$ by reducing into Clairaut's form by taking the substitution $X = x^2, Y = y^2$. (07 Marks)

Module-4

- 7 a. Solve : $(4D^4 - 4D^3 - 23D^2 + 12D + 36)y = 0$. (06 Marks)
- b. Solve : $\frac{d^2y}{dx^2} + \frac{dy}{dx} = x^2 + 2x + 4$. (07 Marks)
- c. Solve by using method of variation of parameters $y'' - 2y' + y = \frac{e^x}{x}$. (07 Marks)

OR

- 8 a. Solve : $y'' + 2y' + y = e^{3x}$. (06 Marks)
- b. Solve : $x^3 \frac{d^3y}{dx^3} + 3x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + 8y = 65 \cos(\log x)$. (07 Marks)
- c. Solve : $(D^2 + 4)y = x^2$. (07 Marks)

Module-5

- 9 a. Find the rank of a matrix by reducing in to echelon form
- $$\begin{bmatrix} 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 3 & 1 & 0 & 2 \\ 1 & 1 & -2 & 0 \end{bmatrix}$$
- (06 Marks)
- b. Solve the system of equations by Gauss-Jordan method: $2x + 5y + 7z = 52, 2x + y - z = 0, x + y + z = 9$. (07 Marks)
- c. Solve the system of equations by Gauss-Seidel iterative method : $x + y + 54z = 110, 27x + 6y - z = 85, 6x + 15y + 2z = 72$. Perform 3 iterations by choosing $(0, 0, 0)$ as initial approximation. (07 Marks)

OR

- 10 a. For what values of λ and μ , the system of equations $x + y + z = 6, x + 2y + 3z = 10, x + 2y + \lambda z = \mu$ has (i) no solution (ii) Unique solution (iii) Infinitely many solutions. (06 Marks)
- b. Solve the system of equations by Gauss elimination method: $x + y + z = 9, x - 2y + 3z = 8, 2x + y - z = 3$. (07 Marks)
- c. Using Rayleigh's power method, find the largest eigen value and the corresponding eigen vector of the matrix $\begin{bmatrix} 4 & 1 & -1 \\ 2 & 3 & -1 \\ -2 & 1 & 5 \end{bmatrix}$ by taking $[1 \ 0 \ 0]^T$ as initial eigen vector. Carry out 5 iterations. (07 Marks)
