

CBCS SCHEME

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18EC55

Fifth Semester B.E. Degree Examination, Jan./Feb. 2023 Electromagnetic Waves

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. The three vertices of a triangle are located at $A(6, -1, 2)$, $B(-2, 3, -4)$ and $C(-3, 1, 5)$. Find (i) $R_{AB} \times R_{AC}$ (ii) Area of triangle (04 Marks)
- b. Define Electric field intensity. Derive the expression for electric field intensity due to infinite line charge. (10 Marks)
- c. Given the electric flux density $\bar{D} = 0.3r^2 \bar{a}_m \text{C/m}^2$ in free space.
- (i) Find E at point $P(r = 2, \theta = 25^\circ, \phi = 90^\circ)$.
- (ii) Find total charge within the sphere $r = 3$.
- (iii) Find total electric flux leaving the sphere $r = 4$. (06 Marks)

OR

- 2 a. Four identical 3nC (nano Coulomb) charges are located at $P_1(1, 1, 0)$, $P_2(-1, 1, 0)$, $P_3(-1, -1, 0)$ and $P_4(1, -1, 0)$. Find the electric field intensity \bar{E} at $P(1, 1, 1)$. (10 Marks)
- b. Infinite uniform line charges of 5 nC/m lie along the (positive and negative) x and y axes in free space. Find \bar{E} at $P_A(0, 0, 4)$. (04 Marks)
- c. Define Coulomb's law. Make use of this to find the force on Q_1 . Given that the point charges $Q_1 = 50 \mu\text{C}$ and $Q_2 = 10 \mu\text{C}$ are located at $(-1, 1, -3)\text{m}$ and $(3, 1, 0)\text{m}$ respectively. (06 Marks)

Module-2

- 3 a. Explain Gauss law applicable to the case of infinite line charge and derive the relation used. (08 Marks)
- b. Evaluate both sides of the divergence theorem for the field $\bar{D} = 2xy\bar{a}_x + x^2\bar{a}_y \text{ C/m}^2$ and the rectangular parallelepiped formed by the planes $x = 0$ and 1 , $y = 0$ and 2 and $z = 0$ and 3 . (08 Marks)
- c. Given the potential field $V = 2x^2y - 5z$ and point $P(-4, 3, 6)$. (i) Find potential V at P . (ii) Field intensity \bar{E} , (iii) Volume charge density ρ_v . (04 Marks)

OR

- 4 a. Compute the numerical value for $\text{div} \bar{D}$ at the point specified below:
 $\bar{D} = (2xyz - y^2)\bar{a}_x + (x^2z - 2xy)\bar{a}_y + x^2y\bar{a}_z \text{ C/m}^2$ at $P_A(2, 3, -1)$ (04 Marks)
- b. Show that Electric field is a negative gradient of potential. (08 Marks)
- c. Let $E = y\bar{a}_x \text{ V/m}$ at a certain instant of time and calculate the work required to move a 3c charge from $(1, 3, 5)$ to $(2, 0, 3)$ along the straight line segment joining
- (i) $(1, 3, 5)$ to $(2, 3, 5)$ to $(2, 0, 5)$ to $(2, 0, 3)$
- (ii) $(1, 3, 5)$ to $(1, 3, 3)$ to $(1, 0, 3)$ to $(2, 0, 3)$ (08 Marks)

Module-3

- 5 a. Solve the Laplace's equation for the potential field in the homogenous region between the two concentric conducting spheres with radii 'a' and 'b' such that $b > a$, if potential $V = 0$ at $r = b$ and $V = V_0$ at $r = a$. Also find the capacitance between two concentric spheres. (10 Marks)
- b. State and explain Biot-Savart law applicable to magnetic field. (06 Marks)
- c. Calculate the value of vector current density in a rectangular coordinates at $P_A(2, 3, 4)$ if $\vec{H} = x^2 z \vec{a}_y - y^2 x \vec{a}_z$. (04 Marks)

OR

- 6 a. State and illustrate uniqueness theorem. (08 Marks)
- b. Define Stoke's theorem. Use this theorem to evaluate both sides of the theorem for the field $\vec{H} = 6xy \vec{a}_x - 3y^2 \vec{a}_y$ A/M and the rectangular path around the region, $2 \leq x \leq 5$, $-1 \leq y \leq 1$, $z = 0$. Let the positive direction of ds be \vec{a}_z . (12 Marks)

Module-4

- 7 a. Obtain the expression for magnetic force between differential current elements. (06 Marks)
- b. Derive the boundary conditions to apply to \vec{B} and \vec{H} at the interface between two different magnetic materials. (08 Marks)
- c. The point charge $q = 18\text{nC}$ has a velocity of 5×10^6 m/s in the direction. $\vec{a}_v = 0.60 \vec{a}_x + 0.75 \vec{a}_y + 0.30 \vec{a}_z$
Calculate the magnitude of the force exerted on the charge by the field,
(i) $\vec{B} = -3 \vec{a}_x + 4 \vec{a}_y + 6 \vec{a}_z$ mT
(ii) $\vec{E} = -3 \vec{a}_x + 4 \vec{a}_y + 6 \vec{a}_z$ kV/m
(iii) \vec{B} and \vec{E} acting together (06 Marks)

OR

- 8 a. Find the magnetization in a magnetic material, where
(i) $\mu = 1.8 \times 10^{-5}$ H/m and $H = 120$ A/m
(ii) $\mu_r = 22$, there are 8.3×10^{28} atoms/m³, and each atom has a dipole moment of 4.5×10^{-27} A.m²
(iii) $B = 300 \mu\text{T}$ and $\chi_m = 15$. (06 Marks)
- b. Let permittivity be $5 \mu\text{H/m}$ in region A where $x < 0$ and $20 \mu\text{H/m}$ in region B, where $x > 0$. If there is a surface current density $\vec{K} = 150 \vec{a}_y - 200 \vec{a}_z$ A/m at $x = 0$, and if $\vec{H}_A = 300 \vec{a}_x - 400 \vec{a}_y + 500 \vec{a}_z$ A/m. Compute
(i) $|H_{tA}|$ (ii) $|H_{nA}|$ (iii) $|H_{tB}|$ (iv) $|H_{nB}|$ (08 Marks)
- c. State and explain Faraday's law of electromagnetic induction. (06 Marks)

Module-5

- 9 a. List and explain Maxwell's equations in point and integral form. (08 Marks)

- b. The time domain expression for the magnetic field of a uniform plane wave travelling in free space is given by,

$$H(z,t) = \bar{a}_y 2.5 \cos(1.257 \times 10^9 t - K_0 z) \text{ mA/m.}$$

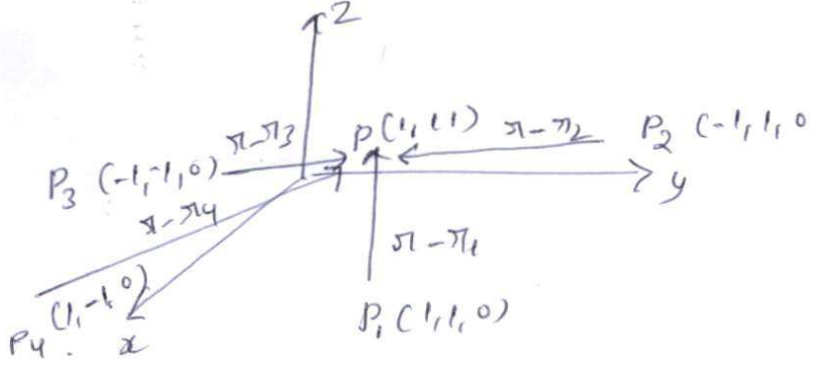
Compute

- (i) The direction of wave propagation.
 - (ii) Operating frequency
 - (iii) Phase constant.
 - (iv) The time domain expression for electric field $E(z,t)$ starting from the Maxwell's equations.
 - (v) The phasor form of both the electric and magnetic field. (10 Marks)
- c. For silver the conductivity is $\sigma = 3 \times 10^6 \text{ S/m}$. At what frequency will the depth of penetration be 1 mm. (02 Marks)

OR

- 10 a. State and explain Poynting theorem and write the equation both in point and integral form. (08 Marks)
- b. Simplify the value of K to satisfy the Maxwell's equations for region $\sigma = 0$ and $\rho_v = 0$ if $\bar{D} = 10x\bar{a}_x - 4y\bar{a}_y + kz\bar{a}_z \text{ } \mu\text{C/m}^2$ and $B = 2\bar{a}_y \text{ mT}$. (06 Marks)
- c. A plane wave of 16 GHz frequency and $E = 10 \text{ V/m}$ propagates through the body of salt water having constant $\epsilon_r = 100$, $\mu_r = 1$ and $\sigma = 100 \text{ s/m}$. Determine attenuation constant, phase constant, phase velocity and intrinsic impedance and depth and penetration. (06 Marks)

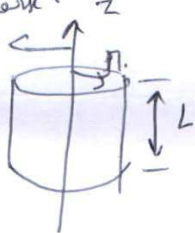
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Question Number	Solution	Marks Allocated
1 a)	$R_{AB} = R_B - R_A = -8ax + 4ay - 6az$ $R_{AC} = R_C - R_A = -9ax + 2ay + 3az$ $\phi R_{AB} \times R_{AC} = 24ax + 78ay + 20az.$ <p>(ii) Area of triangle = $\frac{1}{2} R_{AB} \times R_{AC} = 42 \text{ sq. unit}$</p> <p>b) The force exerted per unit charge is called electric field intensity $\vec{E} = \frac{F}{Q} \text{ V/m}$</p> <p><u>Expression for line charge</u> Fig - intermediate steps</p> <p>Final expression $\vec{E}_p = \frac{\rho_L}{2\pi\epsilon_0 r} \vec{a}_r \vec{a}_y \text{ V/m}$</p> <p>c) (i) $D = \epsilon E$, $E = D/\epsilon$ at $r=2$ we get $E = 135.2 \text{ V/m}$</p> <p>(ii) $D = \frac{Q}{4\pi r^2} \Rightarrow Q = 305.208 \text{ nC}$</p> <p>(iii) WKT $Q = \phi$ at $r=4$ $D = \frac{Q}{4\pi r^2} \Rightarrow Q = 964.608 \text{ nC}$, $\phi = 965 \text{ nC}$</p>	<p>1 } 1 } 1 } 04 1 }</p> <p>02</p> <p>02</p> <p>06</p> <p>02</p> <p>02</p> <p>02</p> <p>02</p>
2 a)	 <p>$\pi = ax + by + cz$, $\pi_1 = ax + by$, $\pi_2 = cz$</p>	<p>02</p>

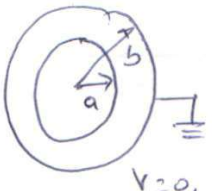
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Subject Title : Electromagnetics

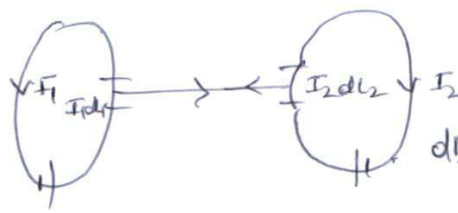
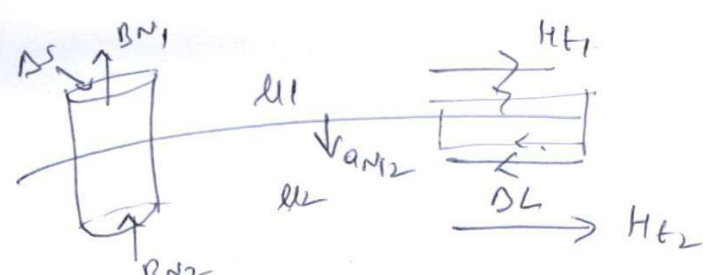
Subject Code : 18EC55

Question Number	Solution	Marks Allocated
	$ r_1 - r_1 = 1, \quad r_1 - r_2 = \sqrt{5}, \quad r_1 - r_3 = 3 \text{ and}$ $ r_1 - r_4 = \sqrt{5},$ $E = 26.96 \left[\frac{q_2}{r_1^2} \frac{1}{12} + \frac{2q_2x + q_2}{r_5^2} \frac{1}{(\sqrt{5})^2} + \frac{2q_2x + 2q_2y + q_2}{3} \frac{1}{32} + \frac{2q_2y + q_2}{r_5^2} \frac{1}{(\sqrt{5})^2} \right]$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $E = 6.829\bar{x} + 6.829\bar{y} + 32.89\bar{z} \text{ V/m}$ </div>	<p>04</p> <p>04</p>
2b)	$E = \frac{\rho L}{2\pi\epsilon_0} q_p = \frac{5 \times 10^{-9}}{2\pi\epsilon_0(4)^2} \frac{4q_2}{4} + \frac{5 \times 10^{-9}}{2\pi\epsilon_0(4)^2} \frac{4q_2}{4}$ $= 4592 \text{ V/m}$	<p>2</p> <p>2</p>
2c)	<p>Definition</p> $F = \frac{Q_1 Q_2}{4\pi\epsilon_0 r^2} \bar{r}_s, \quad \bar{r}_s = \frac{\bar{r}}{ \bar{r} } = \frac{-49\bar{x} - 39\bar{z}}{5}$ $\bar{F} = -0.1449\bar{x} - 0.1089\bar{z} \text{ N}$	<p>02</p> <p>02</p> <p>02</p>
3a)	<p>line charge</p>  <p>Consider line charge along z axis:</p> $Q = \oint \bar{D} \cdot d\bar{s}$ $0 = \oint_{\text{side}} \bar{D} \cdot d\bar{s} + \int_{\text{top}} \bar{D} \cdot d\bar{s} + \int_{\text{bottom}} \bar{D} \cdot d\bar{s}$ <p>\bar{D} has only radial component and no component along \bar{a}_z & $-\bar{a}_z$.</p> $0 = \oint_{\text{side}} \bar{D} \cdot d\bar{s} = \int \bar{D}_r \cdot \bar{a}_r \rho d\rho dz$ $D_r = \frac{Q}{2\pi r L} \bar{a}_r \quad \rho L = Q/L$ $\bar{D} = \frac{\rho L}{2\pi r} \bar{a}_r \text{ C/m}^2 \quad E = \frac{D}{\epsilon_0} = \frac{\rho L}{2\pi\epsilon_0 r} \bar{a}_r \text{ V/m}$	<p>04</p> <p>04</p>

Question Number	Solution	Marks Allocated
3b)	$\oint \vec{D} \cdot d\vec{s} = \int \nabla \cdot \vec{D} dv$ $\oint \vec{D} \cdot d\vec{s} = 12, \quad \int \nabla \cdot \vec{D} \cdot dv = 12.$	04 04 <u>08</u>
3c)	$V_p = 2(-4)^2(3) - 5(6) = 66V$ $E = -\nabla V = -4xy\hat{a}_x - 2x^2\hat{a}_y + 5\hat{a}_z \text{ V/m}$ $D = \epsilon_0 E = -35.4xy\hat{a}_x - 17.71x^2\hat{a}_y + 44.3\hat{a}_z \text{ pC/m}^3$ $P_v = \nabla \cdot D = -35.4y \text{ pC/m}^3$	01 04 02
4a)	$\nabla \cdot D = \frac{\partial D_x}{\partial x} + \frac{\partial D_y}{\partial y} + \frac{\partial D_z}{\partial z}$ $= 2y^2 - 2x = 2(3)(-1) - 2(3) = -10$	04
4b)	$E = -\nabla V$ $dV = \frac{\partial V}{\partial x} dx + \frac{\partial V}{\partial y} dy + \frac{\partial V}{\partial z} dz$ $dV = -E \cdot dL = -E_x dx - E_y dy - E_z dz$ $E = -\left(\frac{\partial V}{\partial x} \hat{a}_x + \frac{\partial V}{\partial y} \hat{a}_y + \frac{\partial V}{\partial z} \hat{a}_z\right)$ $E = -\nabla V$ $\text{Since } \nabla = \frac{\partial}{\partial x} \hat{a}_x + \frac{\partial}{\partial y} \hat{a}_y + \frac{\partial}{\partial z} \hat{a}_z$	01 01 03 03
4c)	$(i) W = -Q \int E \cdot dL$ $W = W_1 + W_2 + W_3$ $W_1 = -3 \int_1^2 (y\hat{a}_x + 0\hat{a}_y + 0\hat{a}_z) dz \hat{a}_z$ $W_2 = -9J$ $W_2 = -3 \int_0^1 (y\hat{a}_x + 0\hat{a}_y + 0\hat{a}_z) (dy \hat{a}_y)$ $= 0J$ $W_3 = -3 \int_5^3 (y\hat{a}_x + 0\hat{a}_y + 0\hat{a}_z) dz \hat{a}_z$ $= 0J$ $W = -9J$	04

Question Number	Solution	Marks Allocated
	<p>ii) $W = -Q \int E \cdot dL$</p> <p>$W = W_1 + W_2 + W_3$</p> <p>$W_1 = -3 \int_1^2 y dx = -3x = 0J$</p> <p>$W_2 = 0J$</p> <p>$W_3 = 0J$</p> <p>$W = 0 + 0 + 0 = \underline{0J}$</p>	04.
59)	<div style="display: flex; align-items: center;">  <div> <p>$\nabla^2 v = 0$</p> <p>$\frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \frac{\partial v}{\partial r}) = 0$</p> <p>Solving v</p> <p>$v = -\frac{C_1}{r} + C_2$</p> <p>Apply boundary conditions</p> <p>$v = 0, r = b \quad v = v_0 \text{ at } r = a$</p> <p>$C_1 = \frac{v_0}{\frac{1}{b} - \frac{1}{a}} \quad C_2 = \frac{v_0}{b[\frac{1}{b} - \frac{1}{a}]}$</p> <p>$v = \frac{-v_0}{r[\frac{1}{b} - \frac{1}{a}]} + \frac{v_0}{b[\frac{1}{b} - \frac{1}{a}]}$</p> <p>$\vec{E} = -\nabla v \Rightarrow -\frac{v_0}{(\frac{1}{b} - \frac{1}{a}) r^2} \vec{a}_r \text{ v/m.}$</p> <p>$D = \frac{\epsilon v_0}{(\frac{1}{a} - \frac{1}{b}) r^2} \text{ C/m}^2.$</p> <p>$Q = D = D = \frac{\epsilon v_0}{(\frac{1}{a} - \frac{1}{b}) r^2} \text{ C/m}^2$</p> <p>$Q = \epsilon_s \times A.$</p> <p>$C = \frac{Q}{V} \quad V = v_0 = \frac{4\pi\epsilon_0 v_0}{\frac{1}{a} - \frac{1}{b}} = \frac{4\pi\epsilon}{\frac{1}{a} - \frac{1}{b}} F$</p> </div> </div>	03.
		03
		04

Question Number	Solution	Marks Allocated
5b)	<p>The magnetic field intensity $d\vec{H}$ produced at a point P due to a differential current element $I d\vec{L}$ is proportional to the product of current I and differential length dL, sine of the angle θ between the element and line joining point P to the element and inversely proportional to the square of the distance R between point P and the element.</p>	02
	$d\vec{H} = \frac{I dL \sin \theta}{4\pi R^2}$ <p style="text-align: right;">Explanation -</p>	04
5c)	<p>Given $\vec{H} = x^2 \vec{a}_y - y^2 \vec{a}_z$</p> $J = \nabla \times H = \begin{vmatrix} \vec{a}_x & \vec{a}_y & \vec{a}_z \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ 0 & x^2 & -y^2 \end{vmatrix}$ $J = -16\vec{a}_z + 9\vec{a}_y + 16\vec{a}_z \text{ A/m}^2$	03 01
6a)	<p><u>Statement</u> Under the given boundary condition the Laplace equation has a unique solution.</p>	02
	<p><u>$V_1 = V_2$</u>, Illustration —</p>	06
6b)	<p>Definition of Stokes theorem —</p> $\oint \vec{H} \cdot d\vec{L} = \int_S (\nabla \times \vec{H}) \cdot d\vec{S}$ <p>LHS, $\oint_{cb} \vec{H} \cdot d\vec{l} = \int_2^5 (6zy \vec{a}_z + 3y^2 \vec{a}_y) (dz \vec{a}_z)$</p> $= 63 \cdot 9 = 63 \cdot 10 = -63$ <p>$\int_{bc} \vec{H} \cdot d\vec{l} = -2$, $\int_{ca} \vec{H} \cdot d\vec{l} = -63$, $\int_{ab} \vec{H} \cdot d\vec{l} = 2$</p>	02 04

Question Number	Solution	Marks Allocated
	$\oint H \cdot dL = 63 - 2 - 63 + 2 = \underline{\underline{-126A}}$ <p>RHS: $\nabla \times H = -6x^2 \hat{z}$</p> $\int (\nabla \times H) \cdot dS = \int_{-1}^1 \int_{-2}^2 -6x^2 \hat{z} \cdot (dx dy \hat{z})$ $= \underline{\underline{-126A}}$ <p><u>RHS = LHS</u> <u>-126 = -126A</u></p>	<p>01</p> <p>01</p> <p>04</p>
7a)	<p>Force b/w differential current elements</p>  <p>$d(dF_1) = I_1 dL_1 \times dB_2$</p> <p>$dB_2 = \mu_0 dI_2 = \mu_0 \left[\frac{I_2 dL_2 \times \hat{a}_{R21}}{4\pi R_{21}^2} \right]$</p> $d(dF_1) = \frac{\mu_0 I_1 dL_1 \times (I_2 dL_2 \times \hat{a}_{R21})}{4\pi R_{21}^2}$ $F_1 = \frac{\mu_0 I_1 I_2}{4\pi} \int_{L_1} \int_{L_2} \frac{dL_1 \times (dL_2 \times \hat{a}_{R21})}{R_{21}^2}$ $F_2 = \frac{\mu_0 I_2 I_1}{4\pi} \int_{L_2} \int_{L_1} \frac{dL_2 \times (dL_1 \times \hat{a}_{R12})}{R_{12}^2}$	<p>03</p> <p>03</p>
7b)	<p>Magnetic boundary condition.</p>  <p>$\oint B \cdot dS = 0$ We set $B_1 \cdot dS - B_2 \cdot dS = 0$</p> <p>$B_1 = B_2$</p>	<p>04</p>

Question Number	Solution	Marks Allocated
	$H_{M2} = \frac{\mu_1}{\mu_2} H_{M1}$ $\oint H \cdot dL = I$ $H_{L1} \Delta L - H_{L2} \Delta L = K \Delta L$ $H_{L1} - H_{L2} = K$ $(H_1 - H_2) \times a_{M12} = K$ $H_{L1} - H_{L2} = a_{M12} \times K$ $\frac{B_{L1}}{\mu_1} = \frac{B_{L2}}{\mu_2} = K$	<p style="text-align: center;">04.</p>
70	<p>(i) $F = q \times B$</p> $= (297a_2 - 405a_3 + 418a_2) \times 10^{-6} N$ $ F_M = \underline{660 \mu N}$	<p style="text-align: center;">02</p>
	<p>(ii) $F = qE = 1.8 \times 10^{-9} (-3a_2 + 4a_3 + 6a_2) \times 10^{-3}$</p> $= (-54a_2 + 72a_3 + 108a_2) \mu N$ $ F = 140.6 \mu N$	<p style="text-align: center;">02</p>
	<p>(iii) $F = q(E \times v \times B)$</p> $((-54a_2 + 72a_3 + 108a_2) + (297a_2 - 405a_3 + 418a_2)) \times 10^{-6}$ $ F = \underline{668.7 \mu N}$	<p style="text-align: center;">02</p>
7a)	<p>(i) $\mu = \mu_r \mu_0$</p> $\mu_r = 14.32 \text{ H/m} \quad \mu_r = \mu_r - 1 = 14.3 - 1 = 13.3$ $M = \chi_m \times H = 13.3 \times 120 = 1599 \text{ A/m}$	<p style="text-align: center;">02</p>
	<p>(ii) $M = \sigma \cdot m \Rightarrow 8.3 \times 10^{28} \times 4.5 \times 10^{-27}$</p> $= 374 \text{ A/m}$ <p>(iii) $\mu_r = \chi_m + 1 = 16, \quad \mu = \frac{\mu_0}{\mu_r} = 14.92$</p>	<p style="text-align: center;">02</p>

Q.No.

$$M = \mu_r \mu_0 k = 1.5 \times 14.92 = 224 \text{ A/m}$$

Marks

02

8b)

State $x=0$ plane

(ii) H_{NA} has only x component.

$$H_{NA} = 300 \bar{a}_x \text{ A/m}$$

To find H_{NB} , $\frac{H_{NA}}{H_{NB}} = \frac{\mu_2}{\mu_1}$

$$\frac{300 \bar{a}_x}{H_{NB}} = \frac{20}{5} \Rightarrow H_{NB} = 75 \bar{a}_x \text{ A/m}$$

To find $H_A = H_{NA} + H_{NB}$

$$= 300 \bar{a}_x - 400 \bar{a}_y + 500 \bar{a}_z + 300 \bar{a}_x$$

$$H_A = \sqrt{(400)^2 + (500)^2}$$

$$H_A = \underline{\underline{640 \text{ A/m}}}$$

$$H_B = H_{NB} + H_{NB}$$

$$H_B = \underline{\underline{695 \text{ A/m}}}$$

24=8

$$|H_A| = 640 \text{ A/m}, |H_{NA}| = 300 \text{ A/m}, |H_B| = 695 \text{ A/m}$$

$$|H_{NB}| = 75 \text{ A/m}$$

8c)

The electromotive force (e.m.f) induced in a closed path is proportional to rate of change of magnetic flux enclosed by the closed path. $e = -n \frac{d\phi}{dt}$ volts.

02

$$\text{emf} = \oint E \cdot dl = - \frac{d}{dt} \int B \cdot ds$$

$$= - \int \frac{\partial B}{\partial t} \cdot ds$$

$$\int \nabla \times E \cdot ds = - \int \frac{\partial B}{\partial t} \cdot ds$$

04

Electromagnetics

(8 ECE 55)

Q.No.		Marks	
9a)	<p>Point form</p> $\nabla \times E = -\frac{\partial B}{\partial t}$ $\nabla \times H = J + \frac{\partial D}{\partial t}$ $\nabla \cdot D = \rho_v$ $\nabla \cdot B = 0$	<p>integral form</p> $\oint E \cdot dl = -\int \frac{\partial B}{\partial t} \cdot dS$ $\oint H \cdot dl = I + \int \frac{\partial D}{\partial t} \cdot dS$ $\oint B \cdot ds = \int \rho_v dv$ $\oint B \cdot ds = 0$	<p>4+4 = 8</p>
9b)	<p>(i) They wave propagate along +z direction (ii) operating frequency = 200 MHz (iii) phase constant = 4.19 rad/m (iv) $E(z,t) = a_x 0.94 \cos(1.257 \times 10^9 t - 4.19 z)$ V/m (v) $E_s(z) = a_x 0.94 e^{-j4.19 z}$ V/m $H_s(z) = a_y 2.5 e^{-j4.19 z}$ mA/m</p>	<p>2x5 = 10</p>	
9c)	$\delta = \frac{1}{\pi f \mu_0} \Rightarrow f = 84.4 \text{ kHz}$	2	
10a)	<p>Poynting theorem definition — explanation — point form + integral form</p> $\oint (E \times H) \cdot ds = \int_{vol} J \cdot E dv + \frac{d}{dt} \int_{vol} \frac{1}{2} D \cdot E dv + \frac{d}{dt} \int_{vol} \frac{1}{2} B \cdot H dv$ $-\nabla \cdot (E \times H) = J \cdot E + \frac{\partial}{\partial t} \left(\frac{1}{2} D \cdot E \right) + \frac{\partial}{\partial t} \left(\frac{1}{2} B \cdot H \right)$	<p>02 04 02</p>	
10b)	$\nabla \cdot D = \rho_v, \rho_v = 0$ $\frac{\partial}{\partial x} D_x + \frac{\partial}{\partial y} D_y + \frac{\partial}{\partial z} D_z = 0$ $10 - 4 + k = 0 \Rightarrow k = -6 \text{ kC/m}^2$	<p>02 04</p>	
10c)	<p>$\frac{\sigma}{\omega \epsilon} > 1$ hence it is a good conductor</p> $\alpha = \beta = \sqrt{\frac{\omega \mu \sigma}{2}} = \underline{\underline{2513}}$ $\eta = \sqrt{\frac{\omega \mu}{\sigma}} \angle 45^\circ = 35.5 \angle 45^\circ$ $u = \frac{\omega}{\beta} = 4 \times 10^7 \text{ m/s}, \quad \delta = \frac{1}{\sqrt{\pi f \mu_0 \mu_0 \sigma}} = \underline{\underline{2513 \text{ m}}}$	<p>01 02 01 01+01</p>	