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**Internal Assessment Test 1 – March 2023 (QP-1)**

Sub:	<b>RADAR ENGINEERING</b>				Sub Code:	<b>18EC823</b>	Branch:	<b>ECE</b>		
Date:	<b>11-03-2023</b>	Duration:	<b>90 minutes</b>	Max Marks:	<b>50</b>	Sem/Sec:	<b>8<sup>th</sup> (A,B,C,D)</b>		<b>OBE</b>	
<u>ANSWER ANY 5 FULL QUESTIONS</u>								MARKS	CO	PET
1	Derive an expression for simple form of the RADAR range equation in three different forms starting from the power density of isotropic antenna.					10	CO1	L2		
2	With a neat block diagram, explain the conventional pulse radar with a super heterodyne receiver.					10	CO1	L2		
3	Write a note on (i) Origin of RADAR (ii) Applications of RADAR.					4 + 6	CO1	L1		
4	What do you understand by the term RADAR? Explain the importance of Radar. With a neat diagram, explain the basic principle of Radar.					1+2+7	CO1	L2		
5	What is meant by Minimum detectable signal power of receiver? Write a brief note on maximum unambiguous range. Tabulate the IEEE standard radar frequency range and their letter band nomenclature.					2+3+5	CO1	L2		
6	a) A ground based RADAR operates at 3cm. The RADAR transmitter using an antenna of gain 50dB produces 100kW. The receiver minimum detectable signal is $S_{min} = 10^{-13}W$ . The maximum RADAR range is given as 259km. Find the cross section of the target the radar can detect. $\rightarrow$ b) A 10 GHZ radar has the following characteristics $P_t = 250 kW$ , p.r.f = 1500 pps, pulse width = $0.8\mu s$ , power gain of antenna = 2500, $S_{min} = 10^{-14} W$ , $A_e = 10 m^2$ , $\sigma = 2 m^2$ . Find (i) R unambiguous (ii) Maximum possible range (iii) Duty cycle (iv) Average power. $\rightarrow$					4 + 6	CO1	L3		

~~100km~~  
100km

$\sigma = 0.9992 m^2$   
 $R_{max} = \left[ \frac{P_t G^2 \lambda^2 \sigma}{(4\pi)^3 S_{min}} \right]^{1/4}$

M.S. Ananth Kumar =  $\downarrow R_{max} = 298 km$   
 Course Instructor

$\rightarrow$   $\tau_{fp} = 0.12\%$   
 Chief Course Instructor

P. E. Lal.  
 HOD

IAT-1

(Q1) A radar eqn relates the radar range to the characteristics of Transmitter, Receiver, Antenna, Target and Environment.

Let ' $P_t$ ' be the transmitted power  
The Power Density of isotropic antenna is given by.

$$PD_{iso} = \frac{P_t}{4\pi R^2}$$

Where  $R$  is the radar range of the target.  
Radars employ directive antennas  
Gain of an antenna is defined by

$$G = \frac{\text{Max value of Power Density of directivity antenna}}{\text{Power Density of isotropic antenna supplied with the same i/p power.}}$$

The Power Density of directive antenna is given by.

$$PD = \frac{P_t G}{4\pi R^2}$$

Let ' $\sigma$ ' be radar cross section.

The Rereflected power density is given by

$$PD = \frac{P_t G}{4\pi R^2} \times \frac{\sigma}{4\pi R^2}$$

For maximum range Subs  $P_r = S_{min}$   
 When  $S_{min}$  is the minimum detectable signal

~~$$S_{min} = \frac{P_t G \sigma}{(4\pi)^2 R^4}$$~~

The received power is given by

$$P_r = \text{incident PD} \times \text{Aperture efficiency}$$

$$A_e = P_a A$$

where  $P_a = \text{effective capture area}$   
 $A = \text{physical area}$

$$P_r = \frac{P_t G \sigma}{(4\pi)^2 R^4} \times A_e$$

For maximum range Subs  $P_r = S_{min}$

$$S_{min} = \frac{P_t G \sigma A_e}{(4\pi)^2 R_{max}^4}$$

$$R_{max}^4 = \frac{P_t G \sigma A_e}{(4\pi)^2 S_{min}}$$

$$R_{max} = \left( \frac{P_t G \sigma A_e}{(4\pi)^2 S_{min}} \right)^{1/4}$$

This is known as radar equation.

But

we know that

$$G = \frac{4\pi Ae}{\lambda^2} \quad \text{--- (2)}$$

Subs (2) in (1) we get

$$R_{\max} = \left( \frac{P_t Ae^2 \sigma}{4\pi \lambda^2 S_{\min}} \right)^{1/4} \quad \text{--- (3)}$$

$$P_r = \frac{4\pi Ae \cdot Ae \sigma}{(4\pi)^2 S_{\min}}$$

Rearranging (2) we get

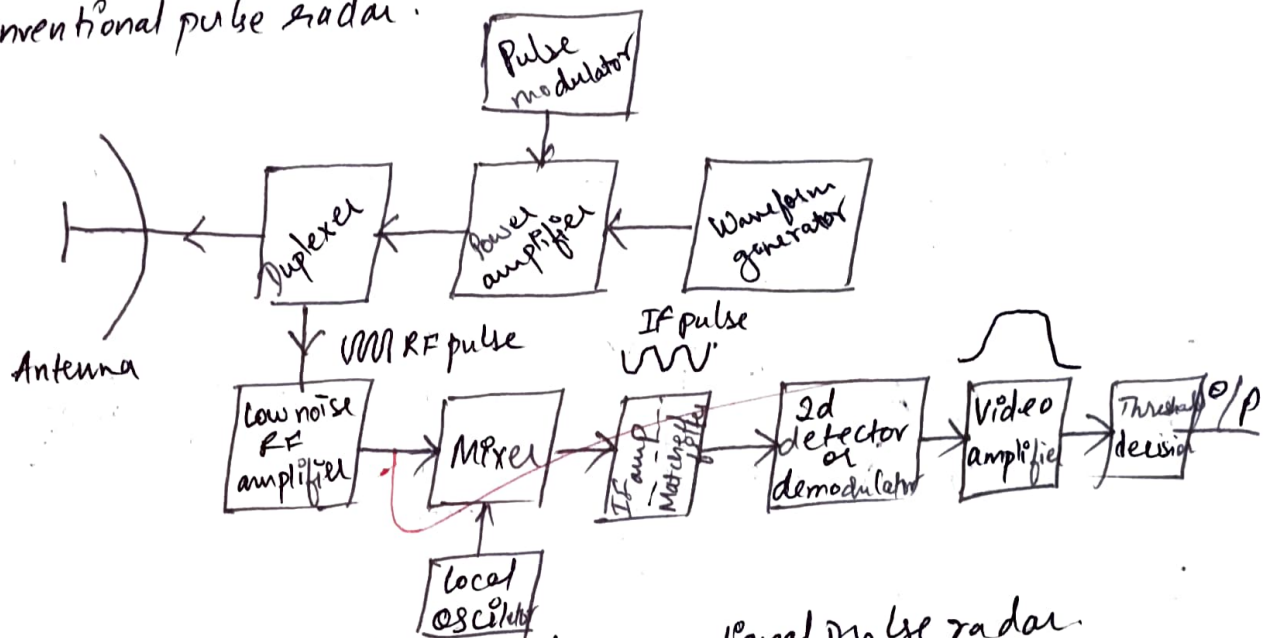
$$Ae = \frac{G \lambda^2}{4\pi} \quad \text{--- (4)}$$

Subs (4) in (1)

$$R_{\max} = \left( \frac{P_t G^2 \lambda^2 \sigma}{(4\pi)^3 S_{\min}} \right)^{1/4} \quad \text{--- (5)}$$

Eq (1) (3) & (5) are the three different forms of radar equation.

(Q2) Conventional pulse radar.

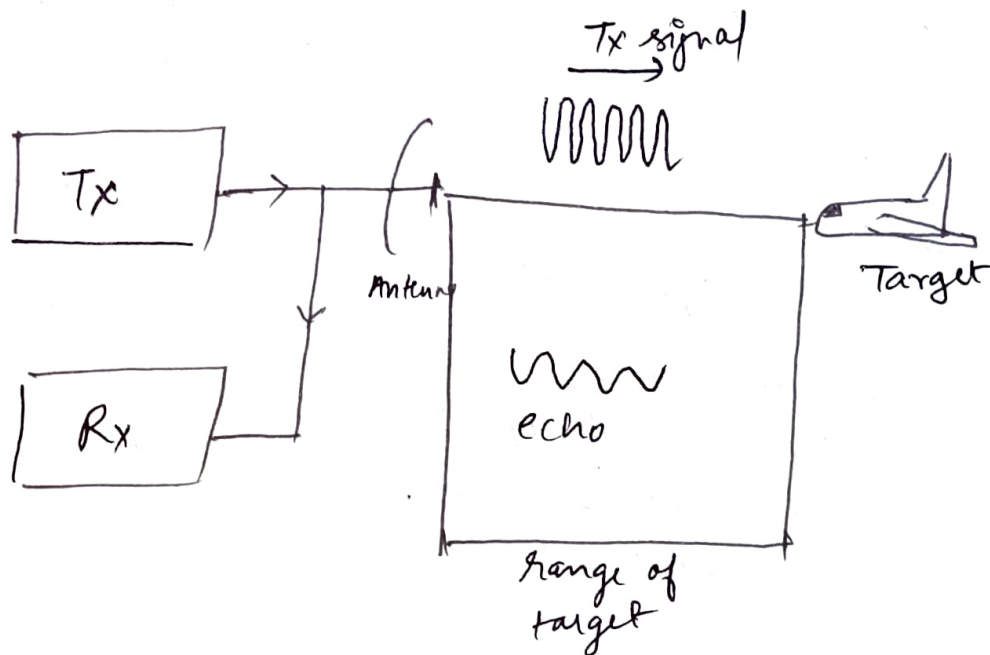


Block diagram of conventional pulse radar.

- \* The Transmitter can be a power amplifier like Klystron
- \* The signal is generated in the waveform generator and passed to the power amplifier for amplification
- \* The pulse modulator turns ON and OFF the transmitter in synchronization with the input pulse to generate a pulse waveform.
- \* The signal is then delivered to the antenna by the means of transmission lines or wave guides.
- \* A duplexer is used so that one ~~sign~~ single antenna can be used for both transmitting and receiving on a time shared basis.
- \* The receiver is almost always a superheterodyne.
- \* The received signal is passed to the Low noise RF amplifier for amplification.
- \* The mixer and local oscillator together convert the RF pulse into an IF pulse.
- \* Then it is passed to the IF amplifier for amplification.

- \* The matched filter attenuates the unwanted noise signals
- \* A 2d detector or demodulator is used to demodulate the received signal.
- \* The IF amplifier, demodulator and the video amplifier together form the envelope detector.
- \* The final decision to predict a target is present or not is done with the help of threshold detector.  
If the ~~trans~~ amplitude of the signal crosses the threshold then a target is present, else target is not there.

(Q4)



Basic block diagram of radar.

- \* RADAR is the combination of the words RADIO Detection And Ranging.
- \* Radar is an electromagnetic system that relies on electromagnetic waves.
- \* The importance of radar is, a radar is used to detect reflective objects like
  - ① Ships
  - ② Planes
  - ③ Cars
  - ④ Pedestrians
- \* The basic principle of radar is that, it emits radiation energy into free space and then detects the echo of the target.
- \* This gives us the location of the target and other target related information.

Eqns.

\* The main benefit of radar is that it can be used in

↳ Darkness

↳ Haze

↳ Fog

↳ Rain

↳ Snow.

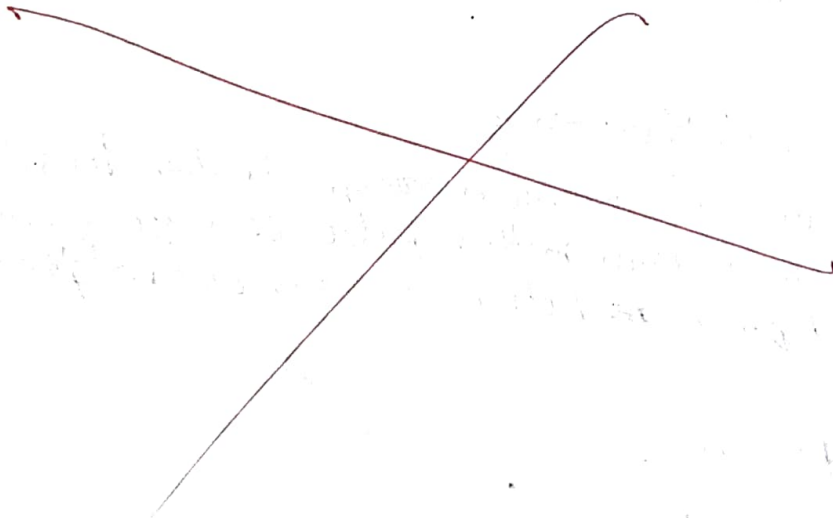
The Advantages of radar is that

- ① It can be used in all types of weather.
- ② It gives a very precise and accurate reading of the targets location.

Applications

- ① Radars are used in planes to navigate in bad weather.
- ② Radars are used in cars for emergency braking

(Explain More)





(Q5)

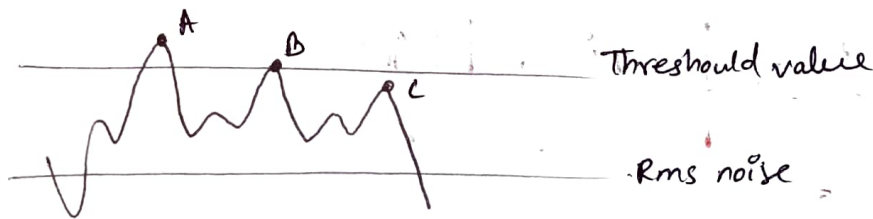
⇒ Minimum detectable signal.

It is the weakest signal that a radar can detect.

If the echo of ~~the~~ has minimum power, then the detection by radar is known as minimum detectable signal.

Therefore if the echo does not have the minimum power limit then the radar will not detect it.

In any practical conditions radars receive signals that have noise. A threshold value is used to determine if a target is present, this is called threshold detection.



A → valid  
 B → valid  
 C → no target.

⇒ Maximum unambiguous range

The Maximum unambiguous range is the longest range upto which a transmitted pulse can go from the radar and back ~~in~~ between consecutive transmitted pulses.

WKT PRF is

$$T_R \propto \frac{1}{PR}$$

Suppose a radar sends a pulse and it returns back in round trip time  $t'$  then.

If  $(t < T)$  the return signal arrives before the next signal pulse is transmitted.

If  $(t = T)$  the return signal arrives just as the next pulse is transmitted.

If  $(t > T)$  the return signal arrives after the next pulse is transmitted (ambiguity).

In the third case the radar is not able to distinguish whether if the <sup>return</sup> pulse is from 1st pulse or 2nd pulse, this causes an ambiguity.

$$R_{un} = \frac{c}{2fr}$$

### IEEE Fredy range of Bands.

#### Band nomenclature

HF	HF (High frequency)
VHF	Very HF
UHF	Ultra HF
L	
S	
C	
X	
Ku	
K	
Ka	
V	
N	
mm	

#### Frequency range.

3 - 30 MHz
30 - 300 MHz
300 - 1000 MHz
1 - 2 GHz
2 - 4 GHz
4 - 8 GHz
8 - 12 GHz
12 - 18 GHz
18 - 27 GHz
27 - 40 GHz
40 - 75 GHz
75 - 110 GHz
110 - 300 GHz

(85)

## (i) Origin of Radar

- \* The first conventional experiment on radar was done by Helrick Hearty in the early years 1885-1888.
- \* Helrick Hearty verified the James Clark Maxwell's theory that was published in 1864.
- \* Helrick Hearty proved that there were similarities between radio waves and light waves but differed in frequency.
- \* The radio waves would reflect off smooth surfaces but would refract through a prism.
- \* H. Hearty's apparatus was similar to the pulse modulator which operated at 45 MHz.
- \* H. Hearty did not conduct any practical experiments, this was done by Christian Heilbrink, a German.
- \* In the 1900's Christian developed an instrument/device that was far better than H. Hearty, which can be compared to the monostable pulse modulators of today.
- \* In 1904 his patent was approved in England and he marketed his device.
- \* His device was used as a ship collision avoidance system.

## (ii) Applications of Radar

Radar is used to detect targets in the air, ground, sea, space and even below the earth's surface.  
Some of the applications of Radar are.

- ① Military
  - \* Radars are used in missile guidance systems.
  - \* Radars are used in air defence systems on military bases.
- ② Remote sensing.
  - \* Radars are used in.
    - \* weather observation.
    - \* planetary observation.
    - \* sea ice observation to map ship routes.
- ③ Air Traffic Control.
  - \* Radars are used for Air Traffic surveillance.
  - \* Radars are used to reroute planes due to bad weather.
- ④ Law Enforcement and Highway Safety.
  - \* The police use radar guns to stop high speeding on highways.
- ⑤ Ship safety.
  - \* Ships use radars to avoid collisions with other ships and ice berge.
- ⑥ Space
  - \* Radars were used to land moon rover.
- ⑦ Aircraft safety.
- ⑧ Radars in Cars for emergency braking.

(106)

3.01

(a)  $\lambda = 3 \text{ cm} = 3 \times 10^{-2} \text{ m}$   
 $G_t = 50 \text{ dB} = 10^{\frac{50}{10}} = 10^5$   
 $P_t = 100 \times 10^3 \text{ W}$   
 $S_{\text{min}} = 10^{-13} \text{ W}$   
 $R_{\text{max}} = 259 \times 10^3 \text{ m}$   
 $\sigma = ?$

50 dB  
 $G = 10 \log(G)$   
 $\frac{G}{10}$   
 (10)

WKT

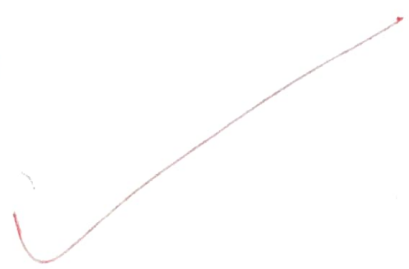
$$R_{\text{max}}^4 = \left( \frac{P_t G^2 \lambda^2 \sigma}{(4\pi)^3 S_{\text{min}}} \right)$$

$$\sigma = \frac{R_{\text{max}}^4 \cdot (4\pi)^3 S_{\text{min}}}{P_t G^2 \lambda^2}$$

$$= \frac{(259 \times 10^3)^4 \cdot (4\pi)^3 \cdot 10^{-13}}{100 \times 10^3 \times (10^5)^2 \times (3 \times 10^{-2})^2}$$

$$\sigma = 0.9921$$

$$\boxed{\sigma \approx 1 \text{ m}^2}$$



Q6

(b) Given

$$P_t = 10 \times 10^6 \text{ Hz} \quad f = 10 \times 10^6 \text{ Hz}$$

$$P_t = 250 \times 10^3 \text{ W}$$

$$\text{PRF} = 1500 \text{ pps}$$

$$\tau = 0.8 \mu\text{s}$$

$$G = 2500$$

$$S_{\text{min}} = 10^{-14} \text{ W}$$

$$A_e = 10 \text{ m}^2$$

$$\sigma = 2 \text{ m}^2$$

$$(i) (R_{\text{un}}) = \frac{c}{2fr} = \frac{3 \times 10^8}{2 \times 1500}$$

$$(R_{\text{un}}) = 100000 \text{ m.}$$

$$\boxed{R_{\text{un}} = 100 \text{ km.}}$$

$$(ii) R_{\text{max}} = \left( \frac{P_t G \sigma A_e}{(4\pi)^2 S_{\text{min}}} \right)^{1/4}$$

$$= \frac{250 \times 10^3 \times 2500 \times 2 \times 10}{(4\pi)^2 10^{-14}}$$

$$= 298278.92 \text{ m}$$

$$\boxed{R_{\text{max}} = 298.27 \text{ km.}}$$

$$(iii) DC = \frac{Z}{T} = Z \cdot f$$

$$= (0.8 \times 10^{-6}) (10 \times 10^9)$$

$$DC = 8000 = 0.8 \times 10^{-6} \times 1500$$

$$DC = 1.2 \times 10^{-3}$$

(iv) Avg power

$$P_{avg} = \frac{P_t Z}{T} = P_t \cdot DC$$

$$= P_t \cdot DC$$

$$= 250 \times 10^3 \times 8000$$

$$= 2000 \times 10^3 \times 10^3$$

$$P_{avg} = 2 \text{ GW}$$

$$= 250 \times 10^3 \times 1.2 \times 10^{-3}$$

$$= 300 \text{ W}$$

$$P_{avg} = 300 \text{ Watts}$$

