



#### **INTERNAL ASSESSMENT TEST – II**



## **Answer any 5 full questions**







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#### **Scheme Of Evaluation Internal Assessment Test II – May 2023**





# **Solutions**



generators producing the discrete PAM  
\nsignal,  
\n
$$
x(t) = \sum_{k=-\infty}^{\infty} a_k v (t-kT_b) \dots (1)
$$
  
\nwhere  $v(t)$  denotes the basic pulse.  
\nThe coefficient  $a_k$  depends on the input.  
\ndata and type of signaling used.  
\nThe PAM signal  $x(t)$  passes through a  
\ntransmitted  
\ntransmitted  
\nis an result of transmission through the  
\nchannel of transfers function  $H_c(f)$ .  
\nThe channel may be a coaxial cable or  
\nan optical fiber, where the major sou-  
\nare of signal degradation is dispersi.  
\nWe assume that the channel is noiseless,  
\nbut dispersive.  
\nThe channel output is passed through a  
\naccepting fitter of transfer function  
\n $H_R(f)$ .

The receiving filters output is sampled  
\nat time 
$$
t = iT_b
$$
, i.e., 1, 1, 2, ...  
\neab sample is compared with a thsesho-  
\n1 d value.  
\n1 f the sample value exceeds the thresh-  
\nold, a decision is made in favor of  
\n1 cthencewise in favor of bit 0.  
\nThe receiving filter output may be was  
\n1 fthencewise in favor of bit 0.  
\nThe scaling factor  $\mu$  accounts for the  
\nattention in the channel.  
\n1 fthence the basic pulse at the receive  
\n1 fthence the baseic pulse at the receive  
\n1 fthence the baseic pulse at the negative  
\n2 fthence the baseic pulse at the  $Y = 0$   
\n2 fthence the baseic pulse at the  $Y = 0$   
\n3 fthence the sum  $\mu$  p(o)  $a_i + \mu \leq a_k p(iT_b - kT_b)$   
\n2 fthence the  $k = 0$   
\n3 fthence the sum  $\mu$  p(o)  $a_i$  is due to the  $i$  th  
\ntsansmitted bit:

$$
a_{k} = PAM(b_{k})
$$
\n
$$
= \begin{cases}\n+IV & \text{if } b_{k} = 1 \\
-IV & \text{if } b_{k} = 0 \dots (1)\n\end{cases}
$$
\nThe output of duobinary codes,\n
$$
C_{k} = a_{k} + a_{k-1} \dots (2)
$$
\nWe assume an ideal channel with frequency response,\n
$$
H_{C}(f) = T_{b} , -\frac{P_{b}}{2} = f \leq \frac{P_{b}}{2} \dots (3)
$$
\nThe overall frequency response of duobin\n
$$
A_{C}(f) = [1 + e^{-j2\pi f T_{b}}] H_{C}(f)
$$
\n
$$
H(f) = [1 + e^{-j2\pi f T_{b}}] T_{b} , -\frac{P_{b}}{2} \leq f \leq \frac{P_{b}}{2} \dots (4)
$$
\n
$$
= [1 + e^{-j2\pi f T_{b}}] T_{b} , -\frac{P_{b}}{2} \leq f \leq \frac{P_{b}}{2} \dots (4)
$$
\n
$$
= e^{-j2\pi f T_{b}} [e^{-j2\pi f T_{b}}] T_{b} - \frac{P_{b}}{2} \leq f \leq \frac{P_{b}}{2} \dots (5)
$$



The impulse response of the duobinary system can be found by computing IFT of frequency response given by (4).  $\int H(f) e^{j2\pi f t} df$  $\therefore$   $h(t) =$  $=\int_{0}^{\frac{Rb}{2}} [1+e^{-j2\pi f T_{b}}]T_{b}e^{j2\pi f t}df$ =  $T_{b} \int_{0}^{\frac{R_{b}}{2}} e^{j2\pi ft} df + T_{b} \int_{0}^{\frac{R_{b}}{2}} j2\pi f(t-T_{b}) df$  $= T_{b} \underbrace{\frac{j2\pi ft}{2}}_{j2\pi t} + T_{b} \underbrace{\frac{R_{b}}{2}\cdot T_{f}(t-T_{b})}_{j2\pi (t-T_{b})}$  $-\frac{R_b}{2}$  $-\frac{kb}{a}$  $=\frac{T_b}{j2\pi t}\left[e^{j\pi R_b t}-e^{j\pi R_b t}\right]+$  $\frac{T_{b}}{j2\pi(t-T_{b})}\left[\frac{j\pi R_{b}(t-T_{b})}{c}-\frac{j\pi R_{b}(t-T_{b})}{c}\right]$ =  $\frac{T_{b}}{j2\pi t}$   $2^{3}_{J}sin(TR_{b}t) + \frac{T_{b}}{j2\pi(t-T_{b})}$   $2^{3}_{J}sin(TR_{b}(t-T_{b}))$ =  $\frac{sin(TR_{b}t)}{\pi R_{b}t} + \frac{sin(TR_{b}(t-T_{b}))}{\pi R_{b}(t-T_{b})}$ 

 $\circled{20}$  $= sinc(R_bt) + sinc(R_b(t-T_b))$  ... (6) This is the impulse response of the duobinary system. To plot h(t) v|st.  $Sinc(R_{b}t)$  $Sinc(R_b(t-T_b))$  $\mathbf{I}$  $\circ$  $3T_{b}$  $2T_b$  $-2T_b$  $-316$  $h(t)$ Impulse response of duobinary system.  $-T_{b}$  $2T_b$  $T_{b}$  $\circ$  $3T_b$  $-2Tb$ From (2),  $C_{k} = a_{k} + a_{k-1}$ @ Receiver,

we evaluate,  $\hat{a}_{k} = \hat{c}_{k} - \hat{a}_{k-1} \cdots (7)$ Decision rule:  $b_{k} = \begin{cases} 1 & i \neq 0 \\ 0 & i \neq 0 \end{cases}$   $\hat{a}_{k} = 1$  ...(8) Note that the decision on the current bit depends on previous de cision. : In the detection process, once an esror is made, the error tends to propagate. This can be avoided using a precoder before duobinary coder. Block diagram of duobinary coder with precoder



 $b$ its

Precoder output,  $d_k = b_k + d_{k-1} - (9)^{22}$  $a_k = PAM(d_k)$ =  $\begin{cases} +1V & \text{if } d_{k=1} \\ -1V & \text{if } d_{k=0} \end{cases}$  (10)  $C_{k} = \alpha_{k} + \alpha_{k-1}$  ... (11)  $C_{k} = \begin{cases} \pm 2N & \text{if } b_{k} = 0 \\ 0 & \text{if } b_{k} = 1 \end{cases}$  (12) (see problem#8). Decision sule @ receiver.  $b_{k} = \begin{cases} 0 & \text{if } |c_{k}| > |V| \\ 0 & \text{if } |c_{k}| \leq |V| \end{cases}$ Note that present décision depends only on present amplitude but not on previous : If an error is made, it will, affect de cision. the future decisions. Hence, error propagation can be prevented Note: Duobinary coding is also called Partial Response Signalling