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Fifth Semester B.E. Degree Examination, Dec.2023/Jan.2024 Digital Signal Processing

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Prove that the sampling of Fourier transform of a sequence $x(n)$ results of N point DFT using which both sequence and the transform can be reconstructed. (08 Marks)
- b. Find N point DFT of the sequence $x(n) = \cos(n\omega_0)$ where $\omega_0 = \frac{2\pi K_0}{N}$ (04 Marks)
- c. For $x(n) = \{1, -2, 3, -4, 5, -6\}$, without computing DFT, find
 - i) $\sum_{k=0}^5 x(k)$
 - ii) $x(3)$
 - iii) $\sum_{k=0}^5 |x(k)|^2$
 - iv) $\sum_{k=0}^5 x(k)(-1)^k$ (08 Marks)

OR

- 2 a. Consider the finite length sequence $x(n) = \delta(n) + 2\delta(n-5)$
 - i) Find the 10 point DFT of $x(n)$
 - ii) Find the sequence that has a DFT $y(k) = e^{j\frac{6\pi k}{10}} \times x(k)$, where $x(k)$ is the 10 point DFT of $x(n)$
 - iii) Find the 10 point sequence $y(n)$ that has a DFT $y(k) = x(k)w(k)$ where $x(k)$ is the 10 point DFT of $x(n)$ and $w(k)$ is the 10 point DFT of $w(n)$ given by $w(n) = u(n) - (n-7)$ (12 Marks)
- b. Find the energy of 4 point sequence

$$x(n) = \sin\left(\frac{2\pi}{N}n\right), 0 \leq n \leq 3.$$
 (04 Marks)
- c. The 4 point DFT of a real sequence $x(n)$ is $x(k) (1, j, 1, -j)$. Using the properties of DFT, find the DFT of following sequence:
 - i) $x_1(n) = (-1)^n x(n)$
 - ii) $x_2(n) = x(4-n)$ (04 Marks)

Module-2

- 3 a. A long sequence $x(n)$ is filtered through a filter with impulse response $h(n)$ to yield output $y(n)$. If input $x(n) = \{1, 0, 1, -2, 1, 2, 3, -1, 0, 2\}$ and $h(n) = \{1, -1, 2\}$, compute $y(n)$ using overlap save technique, Use 6 point circular convolution. (08 Marks)
- b. Find 8 point DFT of $x(n) = n + 1$ using DIT-FFT without computing DFT of $y(n)$, find $y(k)$ of $y(n) = x(-n)_8$. (12 Marks)

OR

- 4 a. Determine the output of an LTI system using circular convolution for $x(n) = \{1, 1\}$, $h(n) = \{1, 0, 1\}$. (03 Marks)
- b. For 512 point DFT/FFT computation, determine
 - i) Number of complex multiplications and complex additions in DFT and FFT computation
 - ii) Speed improvement factor
 - iii) Number of real multiplications and additions in DFT computation
 - iv) Number of stages and butterflies needed in FFT computation (07 Marks)

- c. Find the circular convolution of the sequence $x(n) = (2, 3, 2, 2)$, $y(n) = (1, 1, 5, 3)$ using DIF-FFT algorithm. Verify the same using time domain approach. (10 Marks)

Module-3

- 5 a. Convert the lattice structure of FIR filter defined by $K_1 = 0.65$, $K_2 = 0.341$, $K_3 = 0.8$ to direct form structure. Draw both lattice and direct form structure. (10 Marks)
- b. Design a FIR BPF for lower cutoff frequency 2 rad/s upper cutoff frequency 3rad/s and $m = 7$. Use Hamming windows. Find frequency response and $H(z)$. (10 Marks)

OR

- 6 a. Design a linear phase HPF using Hanning window for the following desired frequency

$$\text{response } H(\omega) = \begin{cases} e^{-j5\omega} & \frac{\pi}{4} \leq |\omega| \leq \pi \\ 0 & |\omega| \leq \frac{\pi}{4} \end{cases} \quad (08 \text{ Marks})$$

- b. Obtain the cascade realization of $H(z) = (1 + 2z^{-1} + 5z^{-2} + 5z^{-3} + 2z^{-4} + z^{-5})(2 + z^{-1} + 3z^{-2})$ (04 Marks)
- c. Determine the coefficient $h(n)$ of linear phase FIR filter of length $m = 15$ which has a symmetric unit impulse response and a frequency response that satisfies

$$H_r\left(\frac{2\pi k}{15}\right) = \begin{cases} 1 & K = 0, 1, 2, 3 \\ 0 & K = 4, 5, 6, 7 \end{cases} \quad (08 \text{ Marks})$$

Module-4

- 7 a. Let $H(s) = \frac{1}{s^2 + s + 1}$ represent the transfer function of low pass filter with passband of 1rad/sec. Use frequency transformation to find the transfer function of i) HPF with passband edge frequency of 100 rad/sec ii) BPF with pass band of 10rad/sec and a center frequency of 100 rad/s (04 Marks)

- b. Design a second order digital BPF Butterworth filter with the following specifications
- Upper cutoff frequency = 2.6KHz
 - Lower cutoff frequency = 2.4KHz
 - Sampling frequency = 8000Hz
- (08 Marks)
- c. Find DF-I and DF-II realization of

$$H(z) = \frac{8z^3 - 4z^2 + 11z - 2}{\left(z - \frac{1}{4}\right)\left(z^2 - z + \frac{1}{2}\right)} \quad (08 \text{ Marks})$$

OR

- 8 a. Design a digital IIR Butterworth HPF with frequency specification given by
- Monotonic passband with cutoff frequency 1000Hz
 - Monotonic stopband with edge frequency 350Hz
 - Stopband attenuation ≥ 10 dB
 - Sampling rate 5KHz
- (08 Marks)
- b. Obtain DF-I and DF-II realization for $y(n) = 0.75 y(n-1) - 0.125 y(n-2) + 6x(n) + 7x(n-1) + x(n-2)$. (08 Marks)
- c. Discuss how analog filter is mapped on to digital filter using Bilinear Transformation and comment on its stability. (04 Marks)

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Module-5

- 9 a. Explain the basic architecture of TMS320C3X floating point DSP. (08 Marks)
- b. Given the FIR filter with passband and gain of 2 and input being half of the range develop the DSP implementation equations in Q15 fixed point system
 $y(n) = -0.36 x(n) + 1.6x(n-1) + 0.36 x(n-2)$ (06 Marks)
- c. With block diagram, explain DSP processors based on Harvard architecture. (06 Marks)

OR

- 10 a. Discuss briefly the following special Digital signal processor hardware units
i) Multiplier and Accumulator unit (08 Marks)
ii) Address generators (08 Marks)
- b. Explain the basic architecture of TMS320C54X family DSP with neat diagram. (08 Marks)
- c. i) Find the signed Q15 representation for the decimal number -0.160123
ii) Convert -2.5 to IEEE single precision format. (04 Marks)
